

# PARTICLE PHYSICS

COLUMBIA SCIENCE HONORS PROGRAM

WEEK 6

OVERVIEW OF THE STANDARD MODEL

Cristóvão Vilela

# COURSE POLICIES

- Attendance
  - Up to four excused absences
    - Two with notes from parent/guardian
    - shpattendance@columbia.edu
  - Valid excuses:
    - Illness, family emergency, tests or athletic/academic competitions, mass transit breakdowns
  - Invalid excuses:
    - Sleeping in, missing the train...
  - I will take attendance during class
- No cell phones
- Ask questions!

# LECTURE MATERIALS

- <https://twiki.nevis.columbia.edu/twiki/bin/view/Main/ScienceHonorsProgram>
- Questions: cristovao.vilela@stonybrook.edu

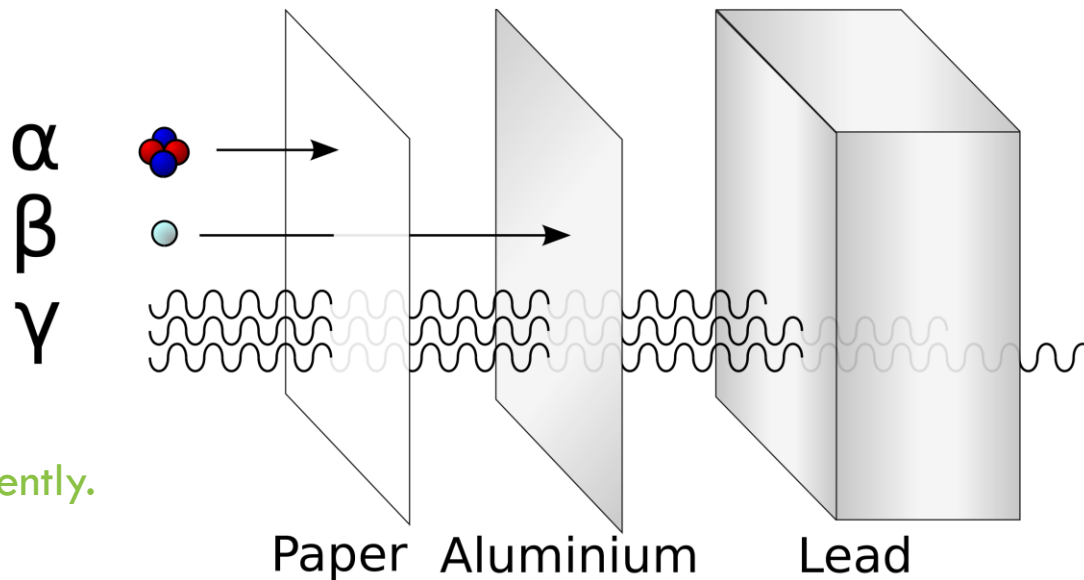
LAST WEEK...

# EXPERIMENTAL METHODS

HOW WE STUDY PARTICLES IN THE LAB

# PASSAGE OF PARTICLES THROUGH MATTER

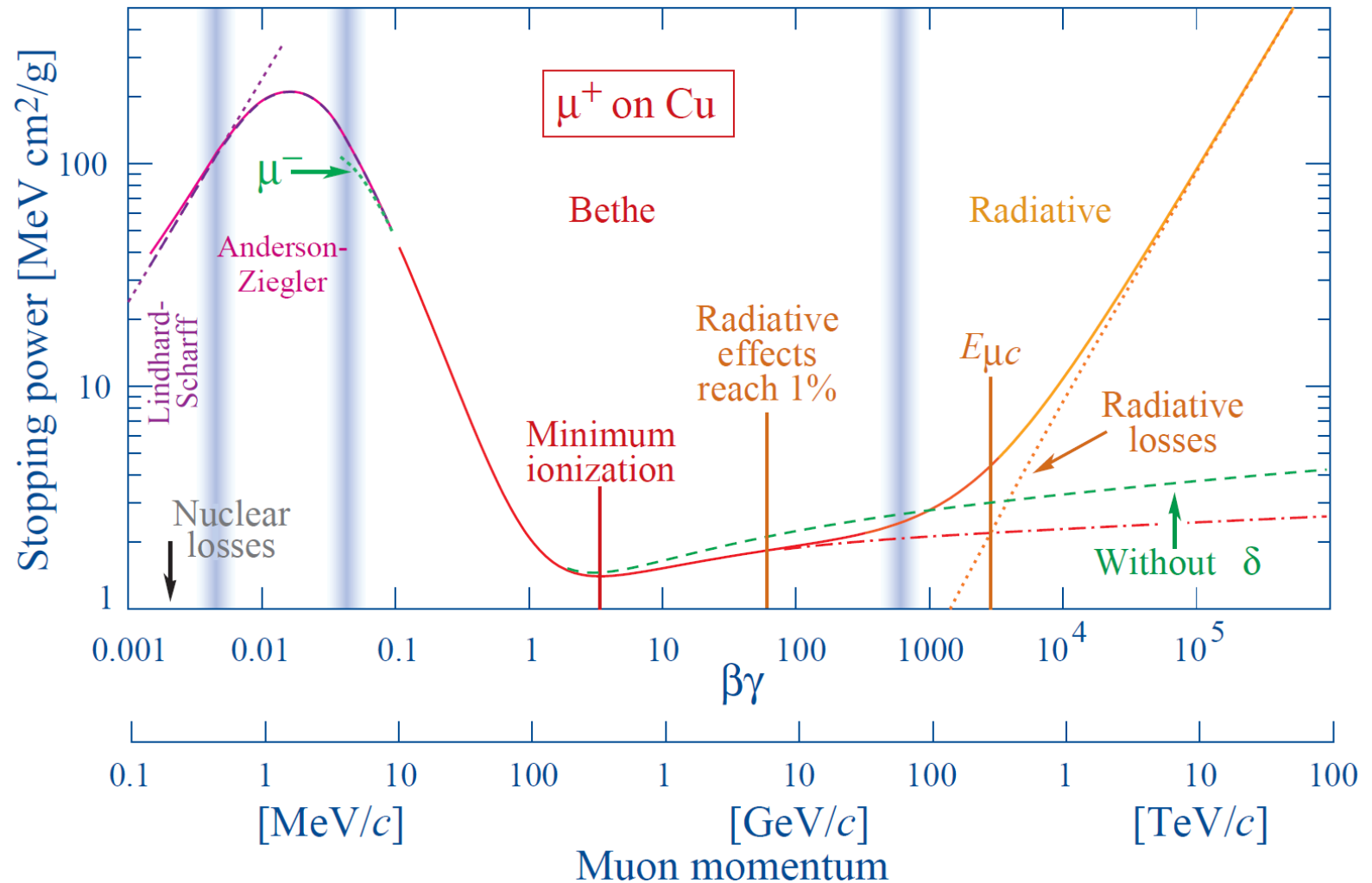
- Alpha, beta, gamma radiation:
  - Classified according to how they bend in a magnetic field.
  - Also differentiated by how easily they can be stopped.



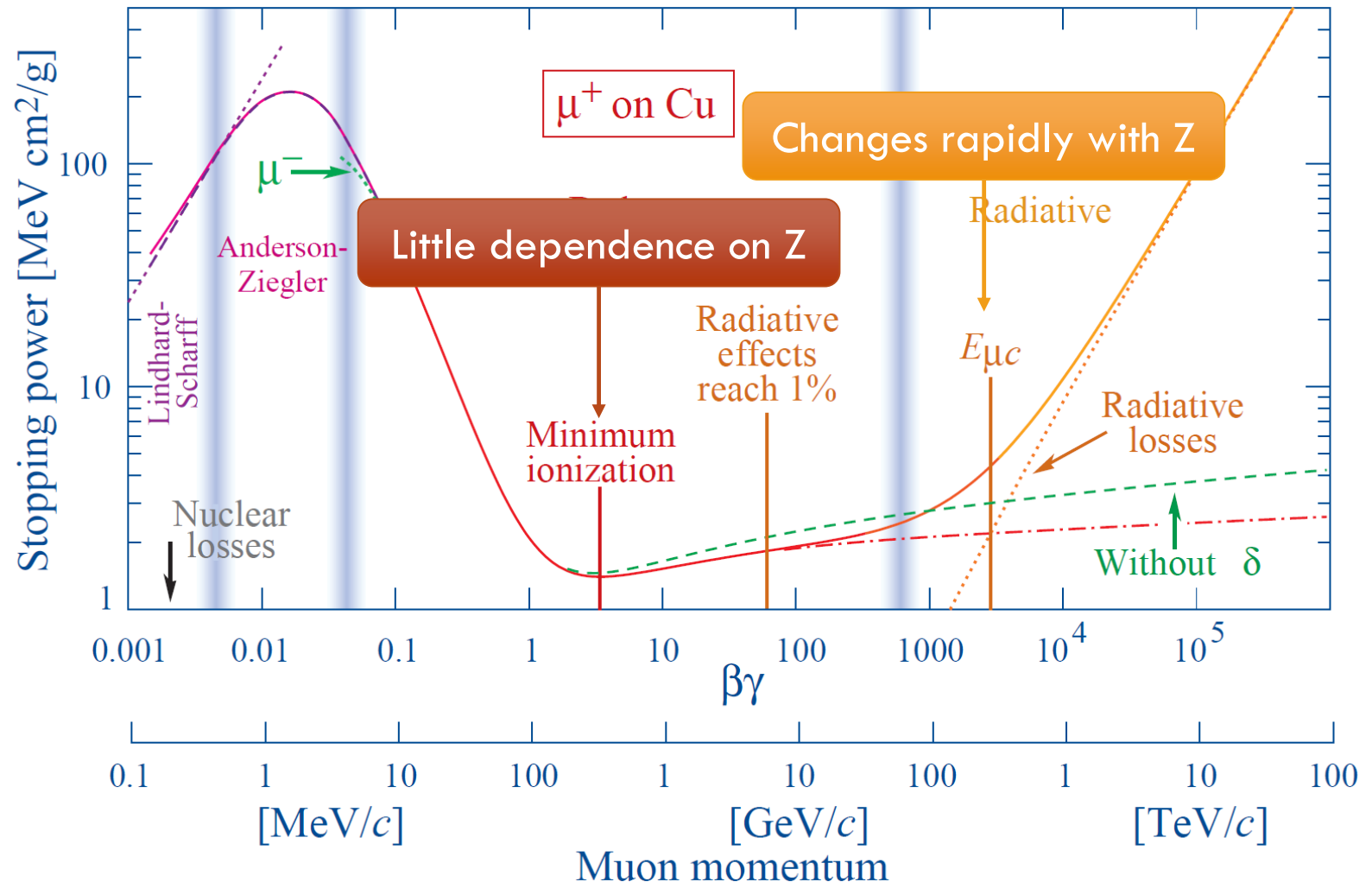
Charged particles interact more frequently. They ionize matter (directly) and lose energy in the process.

Neutral particles interact less often, losing less energy. They ionize matter indirectly.

# STOPPING POWER

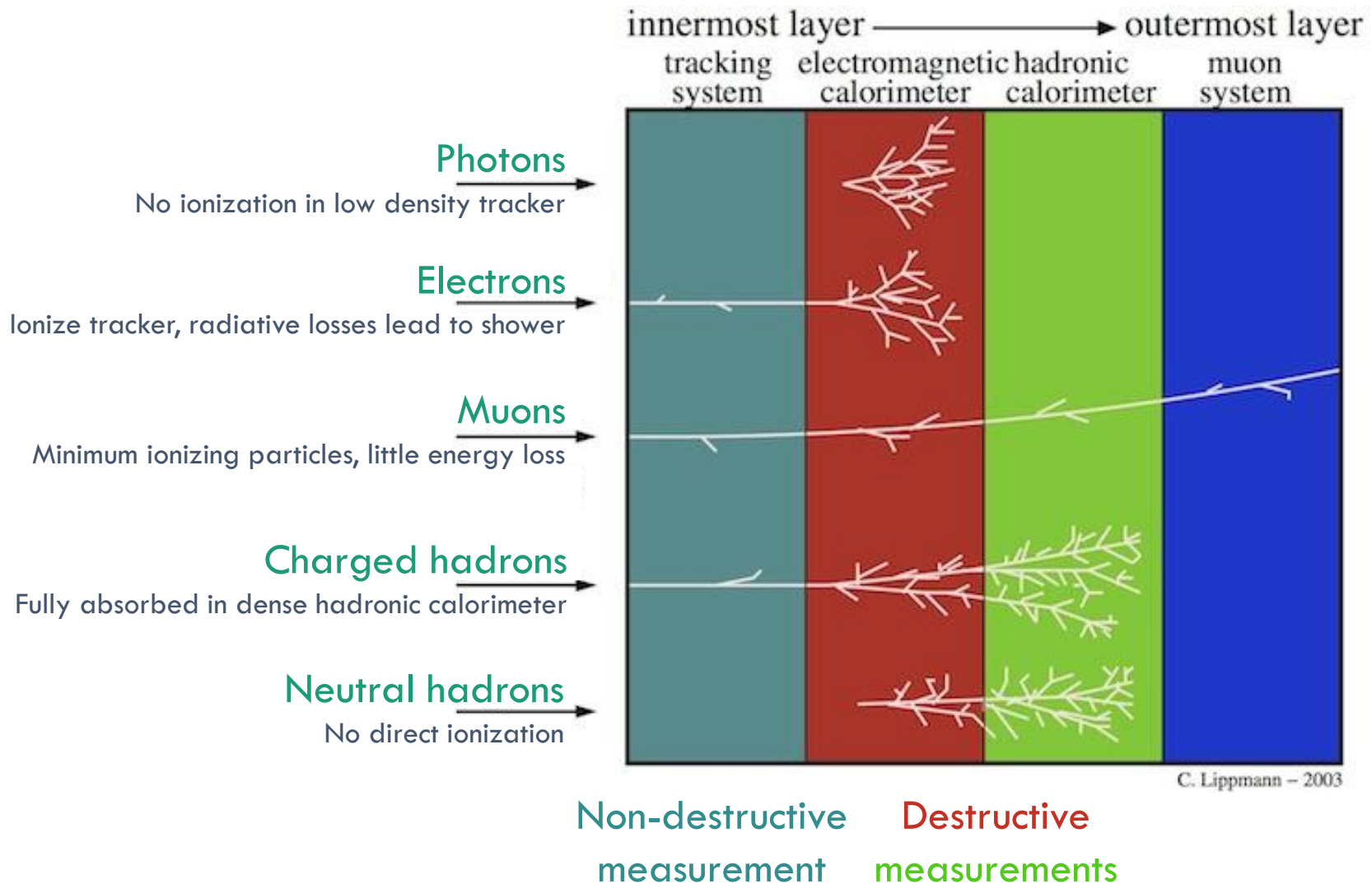


# STOPPING POWER





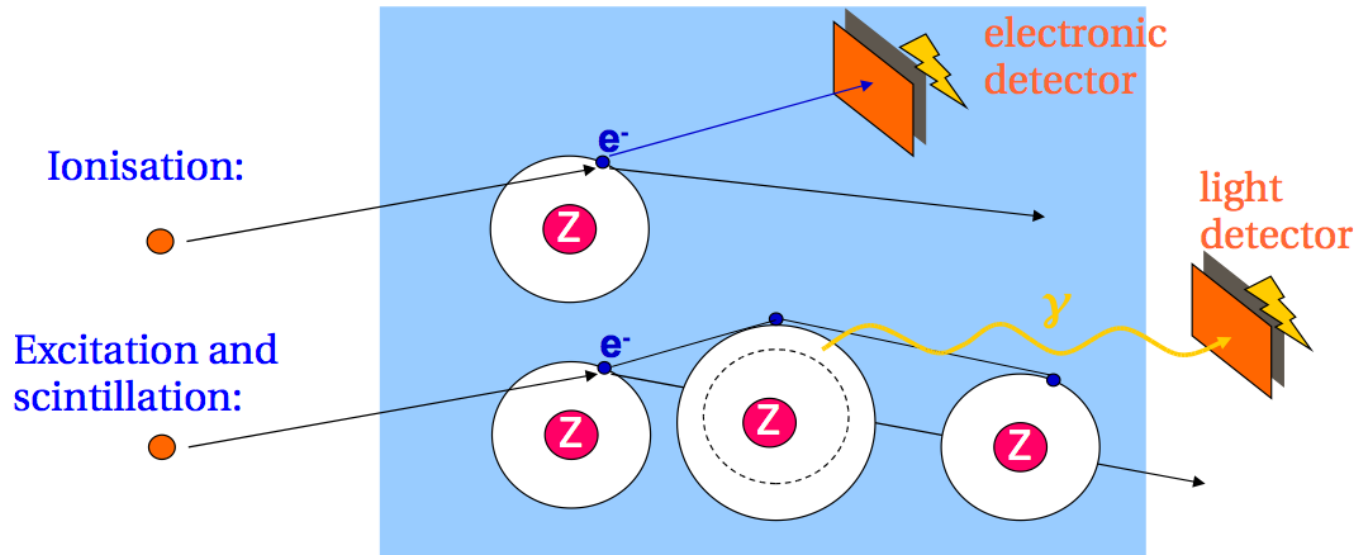
# PARTICLE DETECTION



# PARTICLE DETECTION

- Charged particles will:
  - Ionize the medium:
    - Electron / ion pairs will be produced copiously and can be collected in electrodes and read out as electrical signals.
  - Produce scintillation light:
    - Some detector materials are engineered to produce lots of (low energy) photons as the electrons in their atoms / molecules get kicked to higher energy orbitals and then de-excite.
  - Produce Cherenkov radiation:
    - Charged particles travelling faster than the speed of light in the medium will produce an electromagnetic “sonic boom”.

# PARTICLE DETECTION



# IONIZATION

Bethe energy loss formula

$$-\frac{dE}{dx} = \frac{4\pi}{m_e c^2} \cdot \frac{n z^2}{\beta^2} \cdot \left( \frac{e^2}{4\pi\epsilon_0} \right)^2 \left[ \ln \left( \frac{2m_e c^2 \beta^2}{I \cdot (1-\beta^2)} \right) - \beta^2 \right]$$

$-\frac{dE}{dx}$  Energy loss per distance traveled

$\beta = \frac{v}{c}$  Particle velocity

$z$  Particle charge (in units of electron charge)

$n$  Density of electrons in material

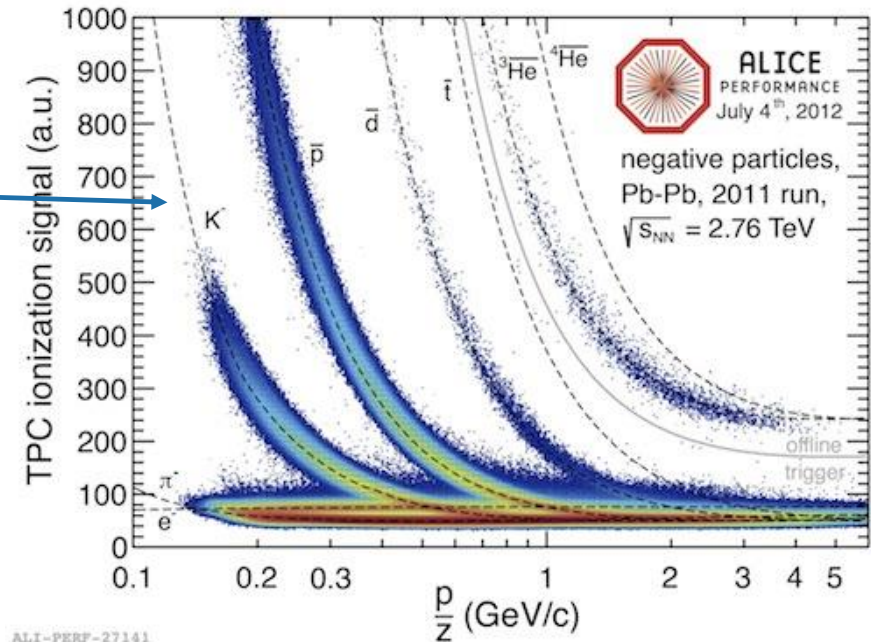
$I$  Mean excitation potential of material

$\epsilon_0$  Vacuum permittivity

$e$  Electron charge

$m_e$  Electron mass

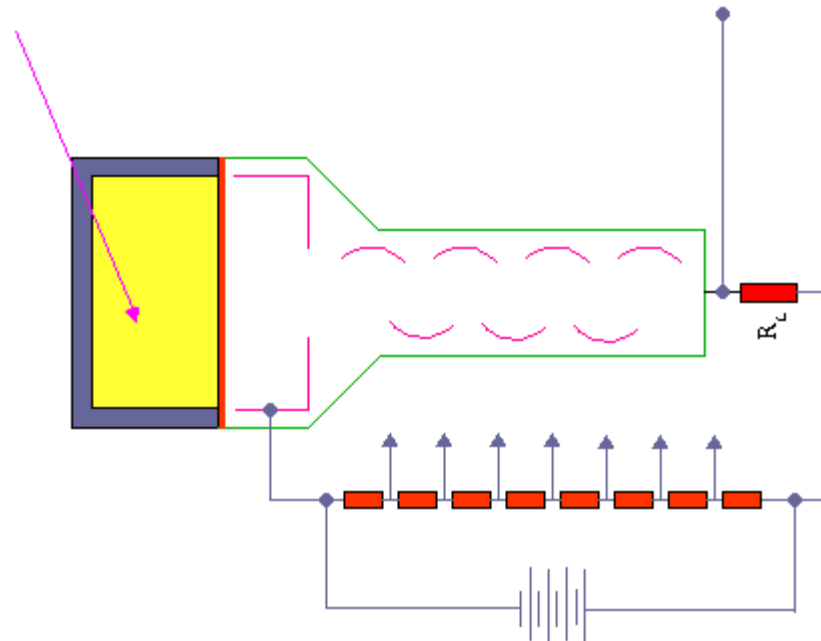
$c$  Speed of light in vacuum



$$p = \frac{v}{\sqrt{1-\beta^2}} m$$

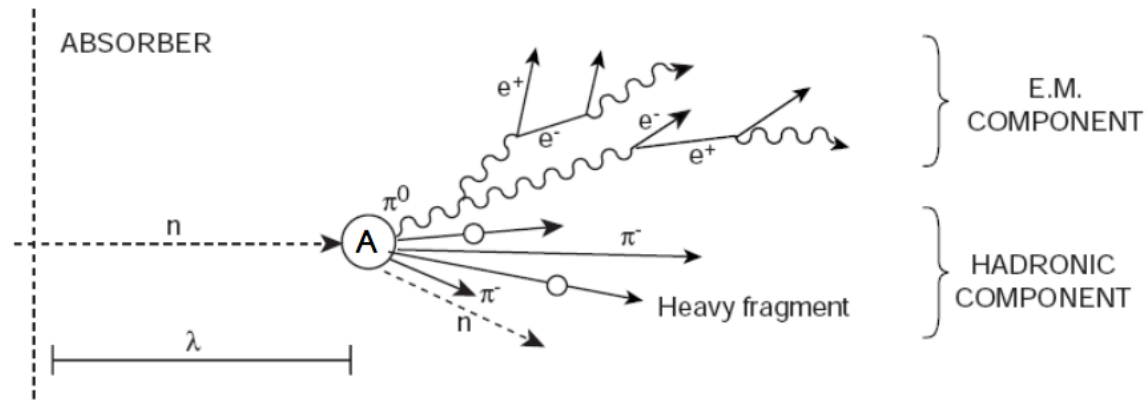
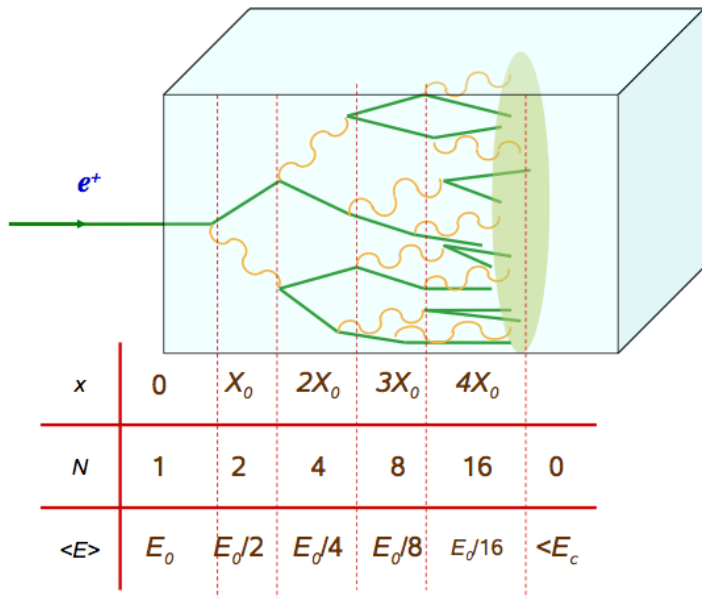
# LIGHT DETECTION

- A **photomultiplier tube** (PMT) is a commonly used instrument for detecting visible photons.
- Basic of operation: photoelectric effect
  - Single photons converted to electrons and multiplied to a measurable electronic signal.

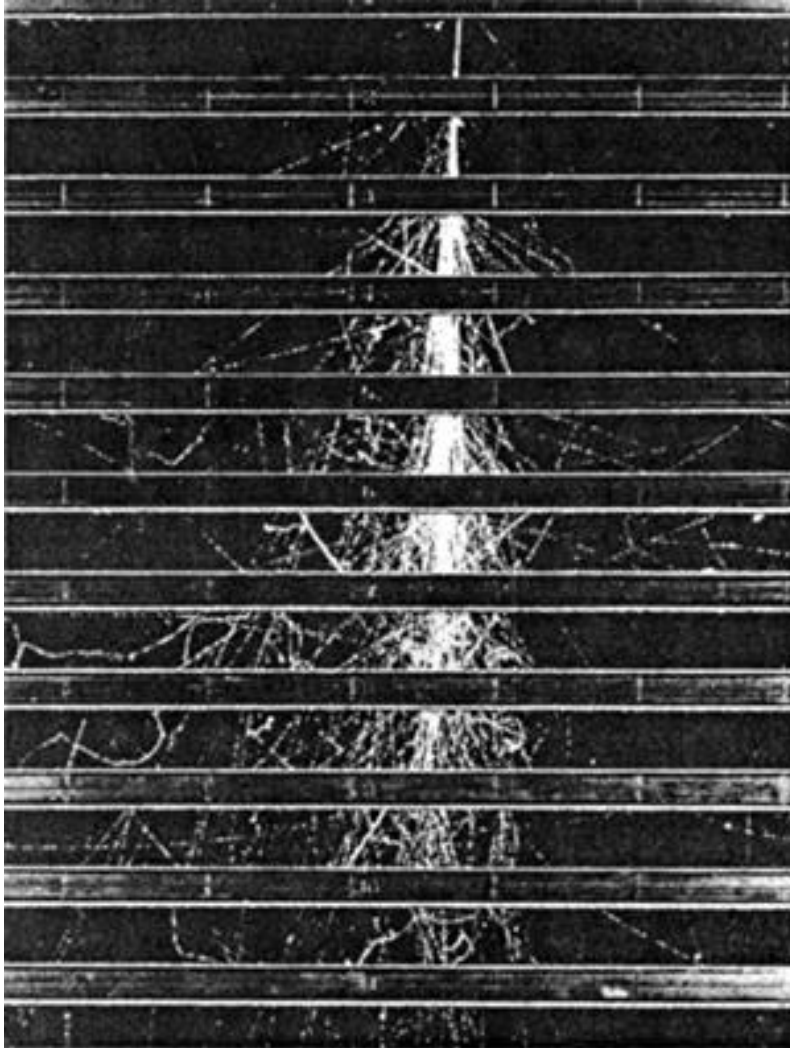


# SHOWERS AND CALORIMETRY

- Placing **dense**, high-**Z**, materials in the path of particles will lead to extensive **radiative** processes.
  - These will produce particle **showers**, with the initial particle's energy being **fully absorbed** in a short length.
    - The large number of particles in the showers will produce a great deal of ionization / scintillation.



# HADRONIC VS EM SHOWERS



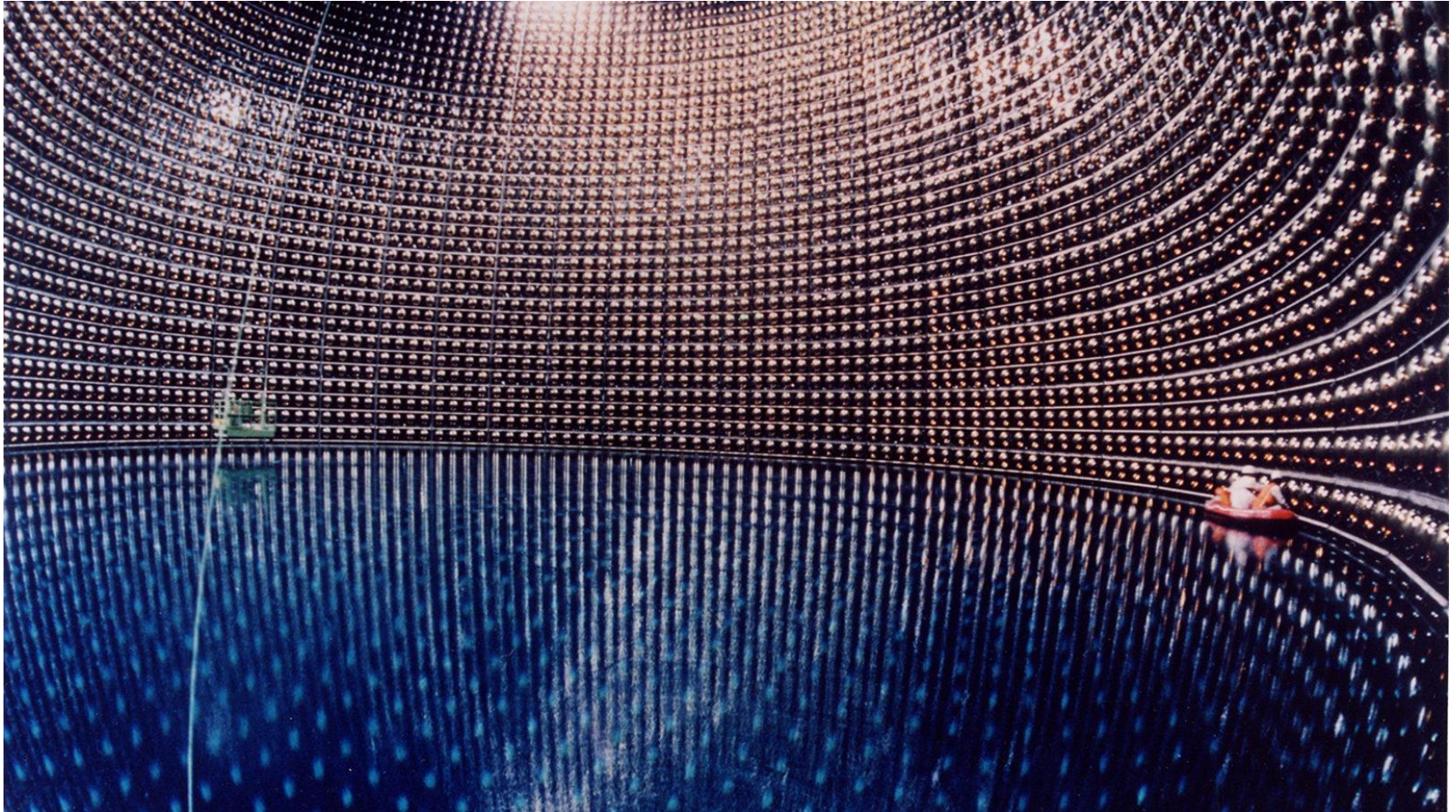
# PARTICLE DETECTORS

- Detectors usually specialize in:
  - Tracking: measuring **positions** / **trajectories** / **momenta** of charged particles, e.g.:
    - Silicon detectors
    - Drift chambers
  - Calorimetry: measuring **energies** of particles:
    - Electromagnetic calorimeters
    - Hadronic calorimeters
- But they can also be a combination.

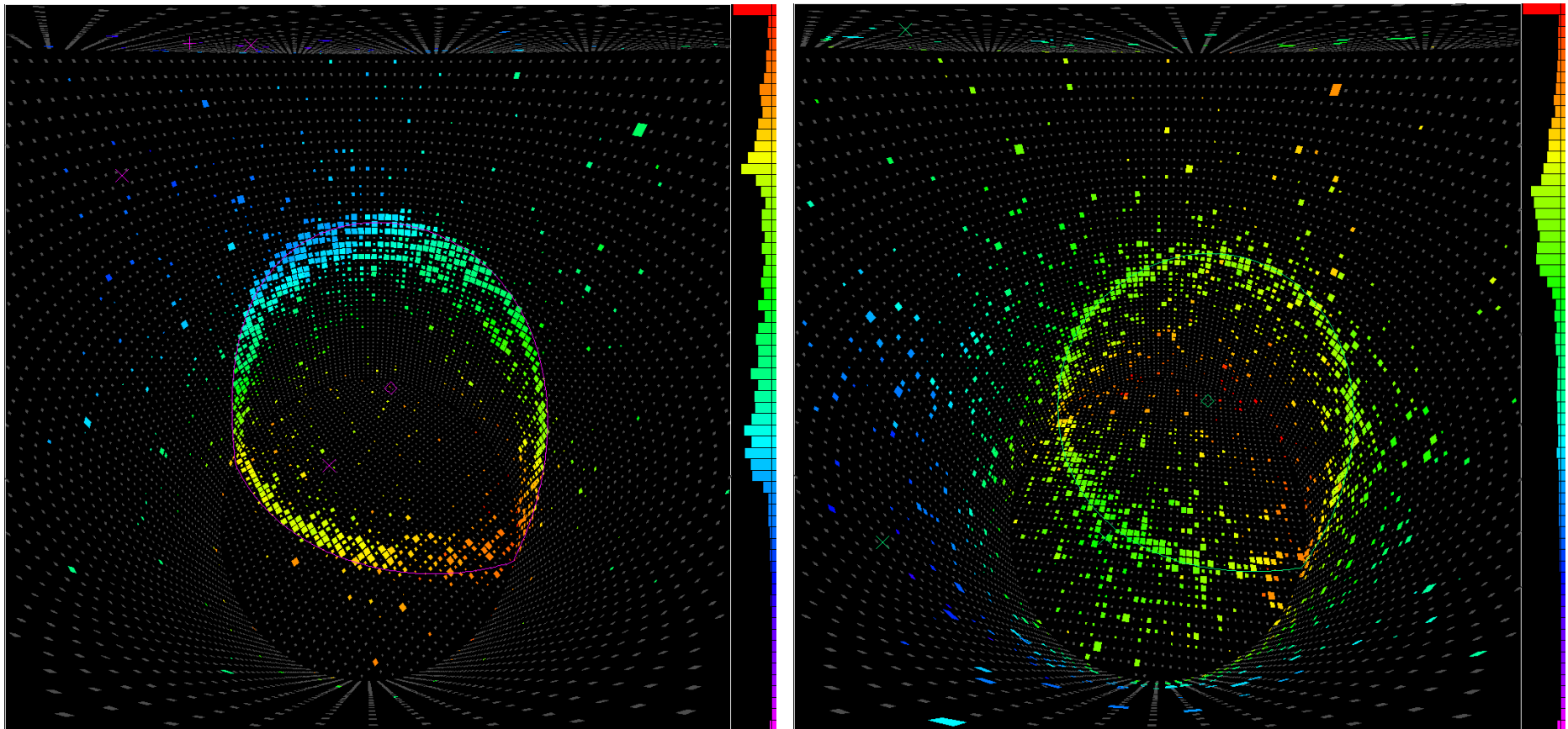


# CHERENKOV DETECTORS

- Super-Kamiokande in Japan

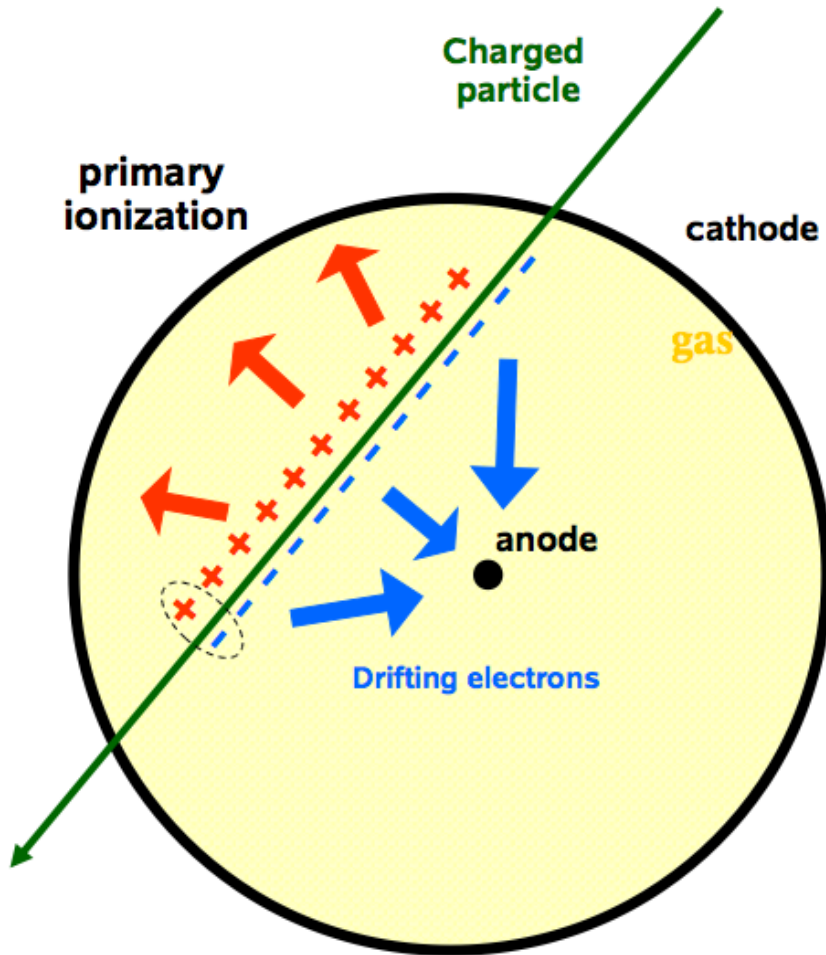


# NEUTRINO DETECTION AT SUPER-K





# IONIZATION DETECTOR

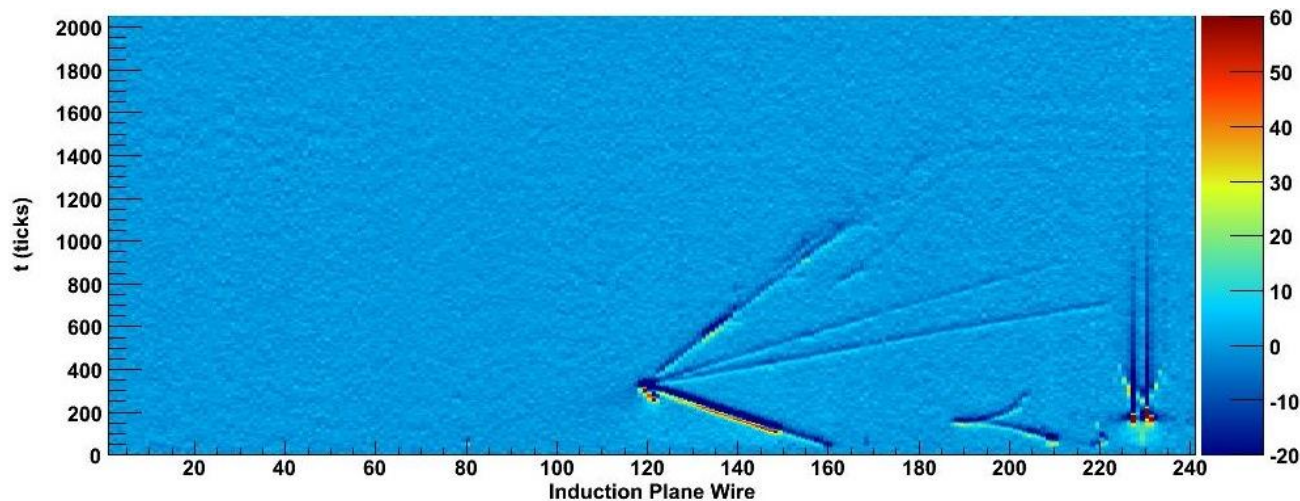


- Drifting electrons should not be trapped:
  - ▶ Use noble gas, e.g. Ar.
- Want large primary ionization yield:
  - ▶ Ar gives 25 ions/cm at normal T, p for a minimum ionizing particle.
- The primary electrons may ionize further atoms:
  - ▶  $\times 3$  or  $\times 4$  increase.
- Xe and/or higher pressure are even better (and more expensive).

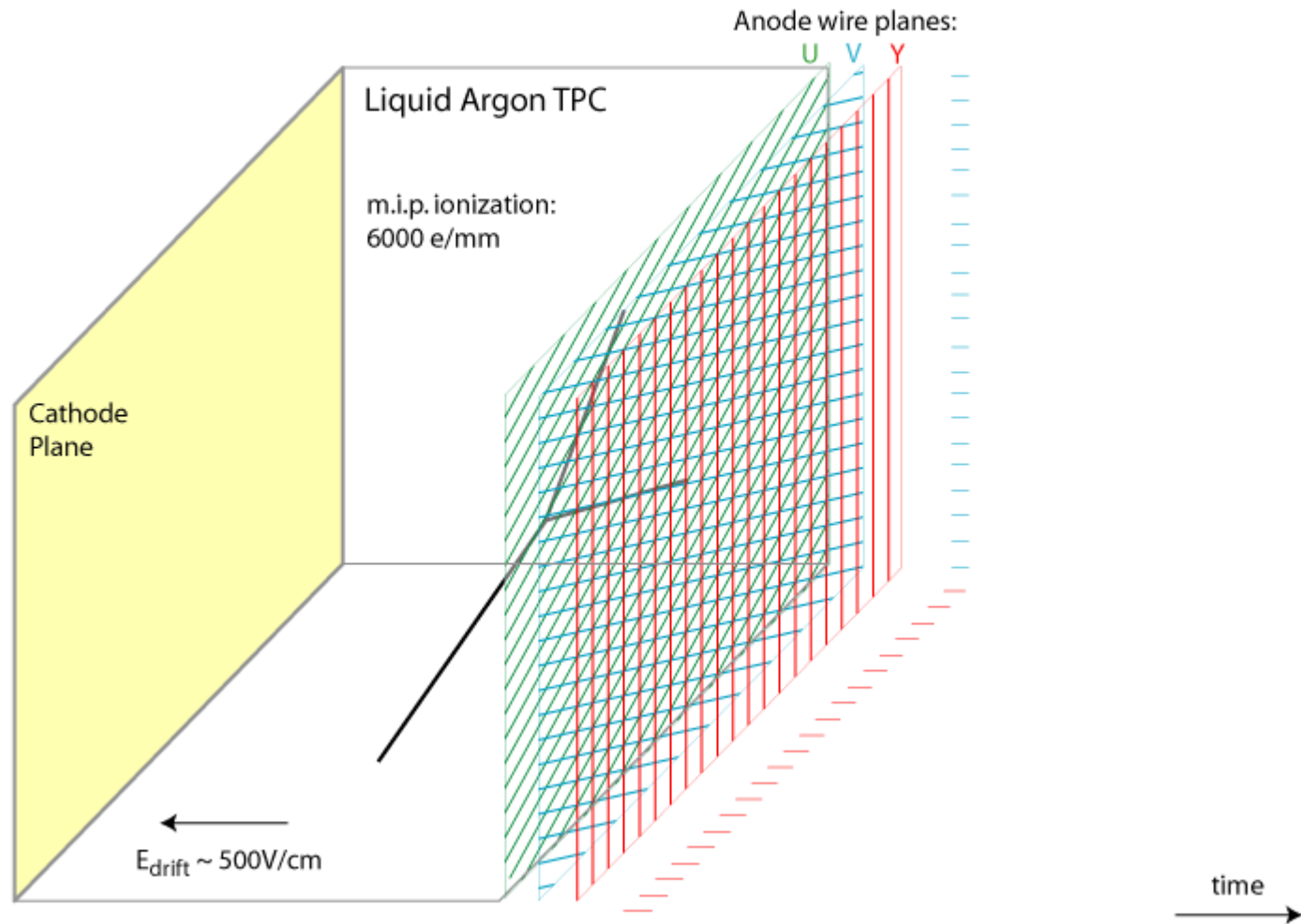
Induced electrical signal on anode can be measured to estimate number of drift electrons:  $E$  lost to ionization.

# TIME PROJECTION CHAMBER

- Exploits **ionization** energy losses of **charged** particles.
- Electrons are **drifted** onto a fine grained **plane of wires**, and the particle **trajectories** can be mapped out, along with their ionization **energy** loss,  $dE/dx$



# TIME PROJECTION CHAMBER

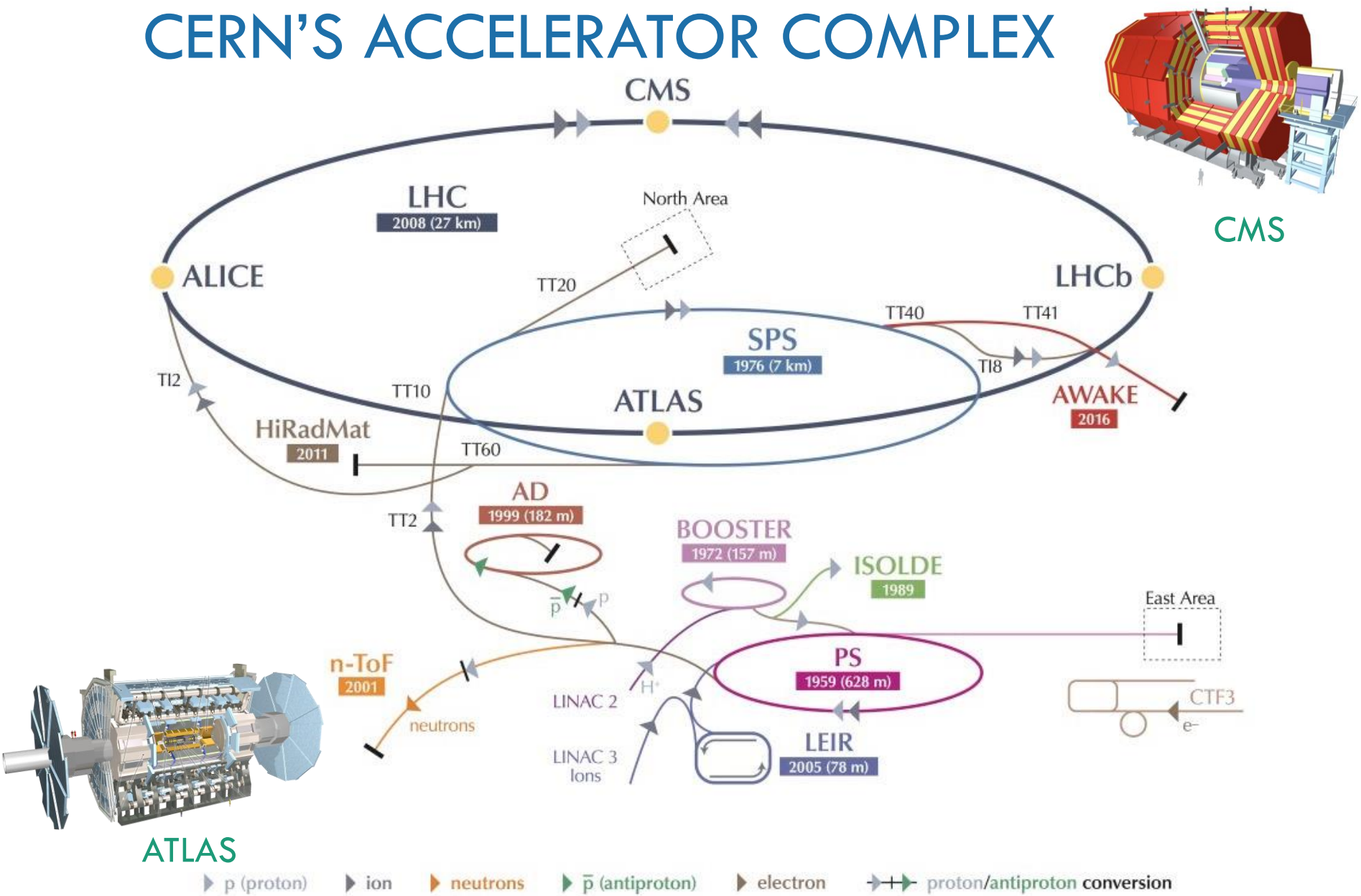


# MODERN EXPERIMENTS

# PARTICLE SOURCES

- Particle physics experiments use different **sources** of particles
- Artificial **beams** produced in accelerators
  - **Colliders** – beams are made to collide against each other.
    - **Highest energy** interactions from artificial sources
  - Beams are aimed at **fixed targets** / detectors
    - Lower energy, but typically more **intense**
- **Natural** sources
  - Particles resulting from **cosmic** ray interaction in the atmosphere
  - **Radioactive** sources
  - **Astrophysical** sources
  - **Dark** matter ?

# CERN'S ACCELERATOR COMPLEX

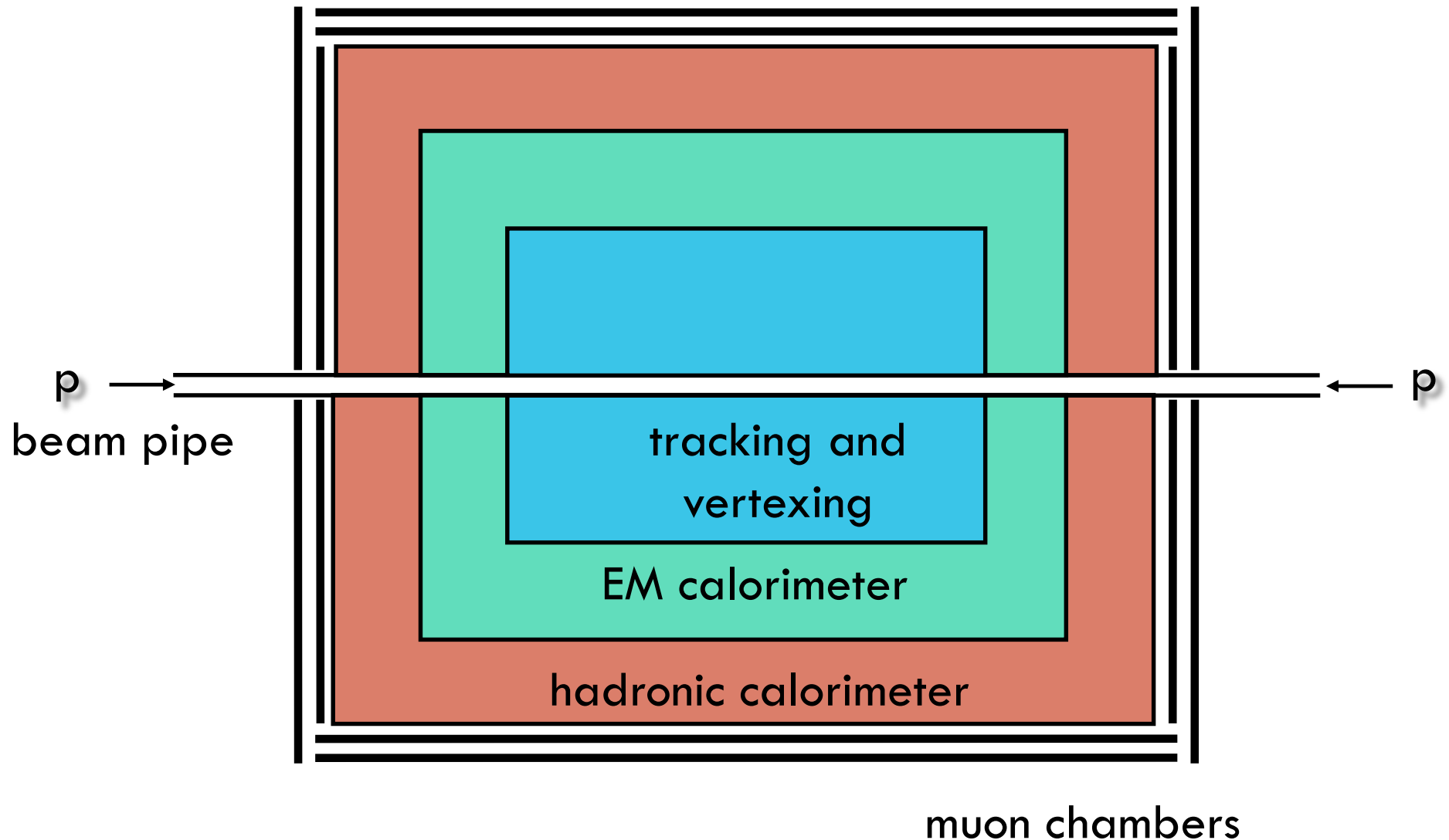


ATLAS

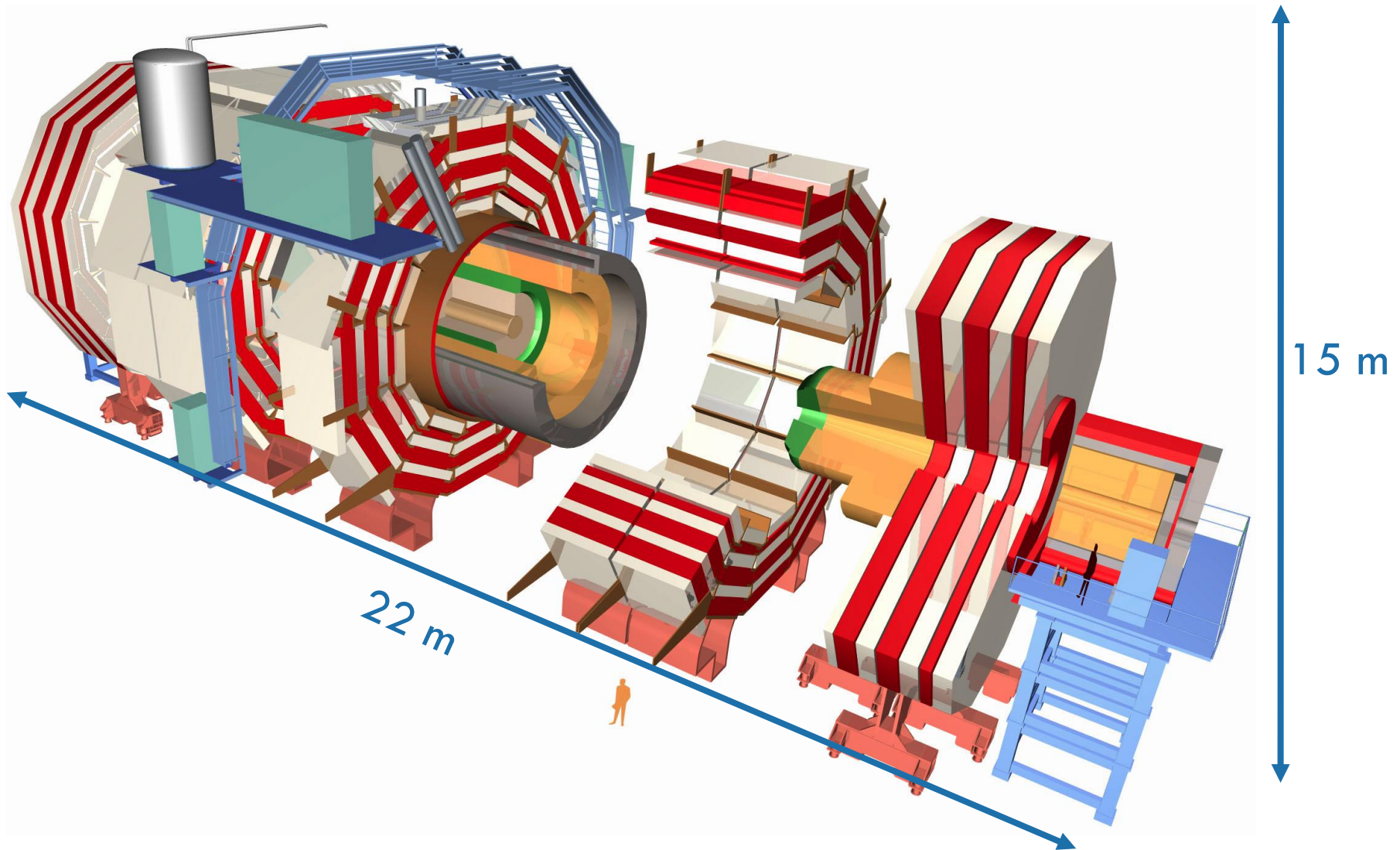
CMS



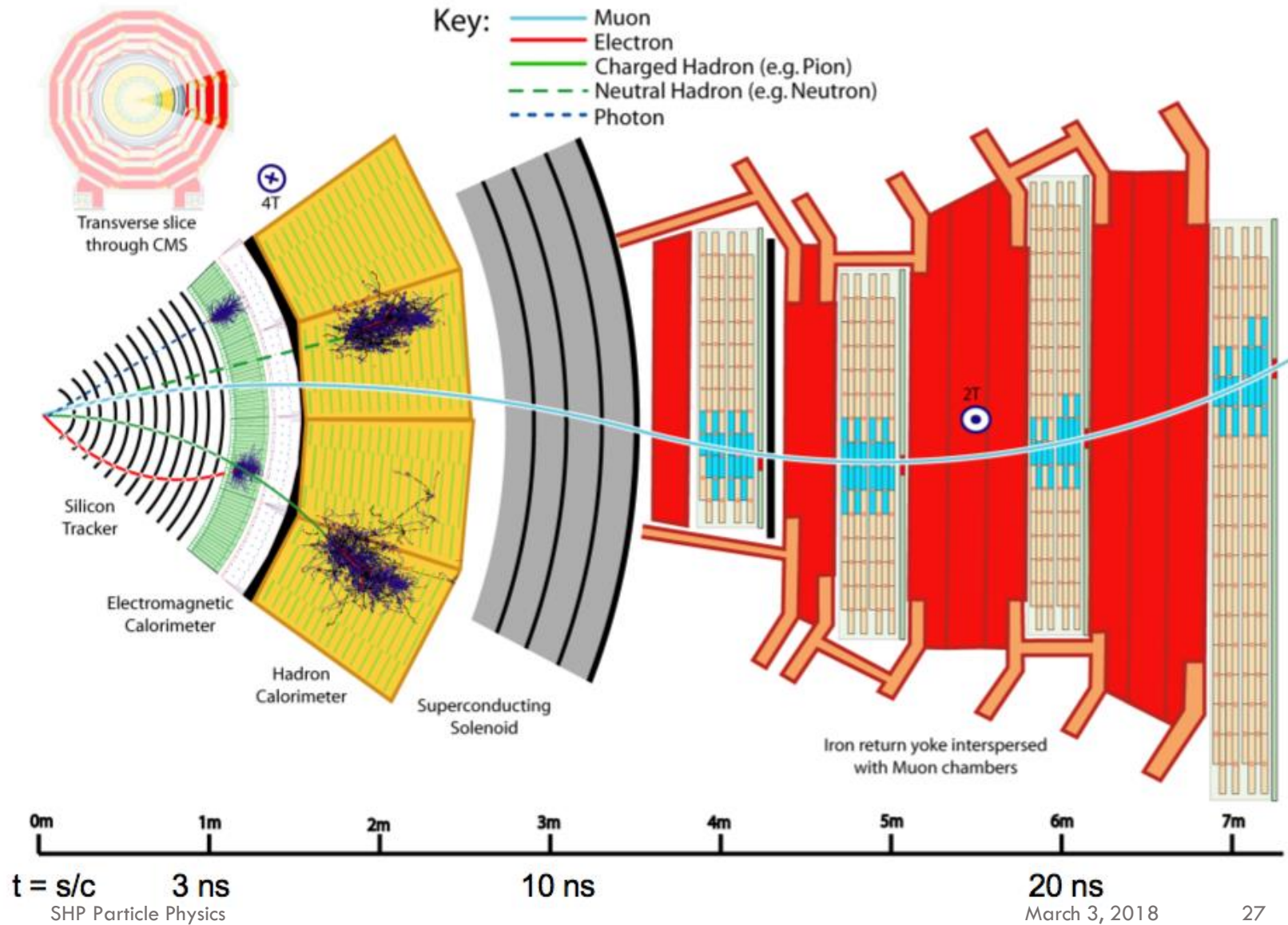
# A GENERAL PURPOSE DETECTOR



# THE CMS DETECTOR



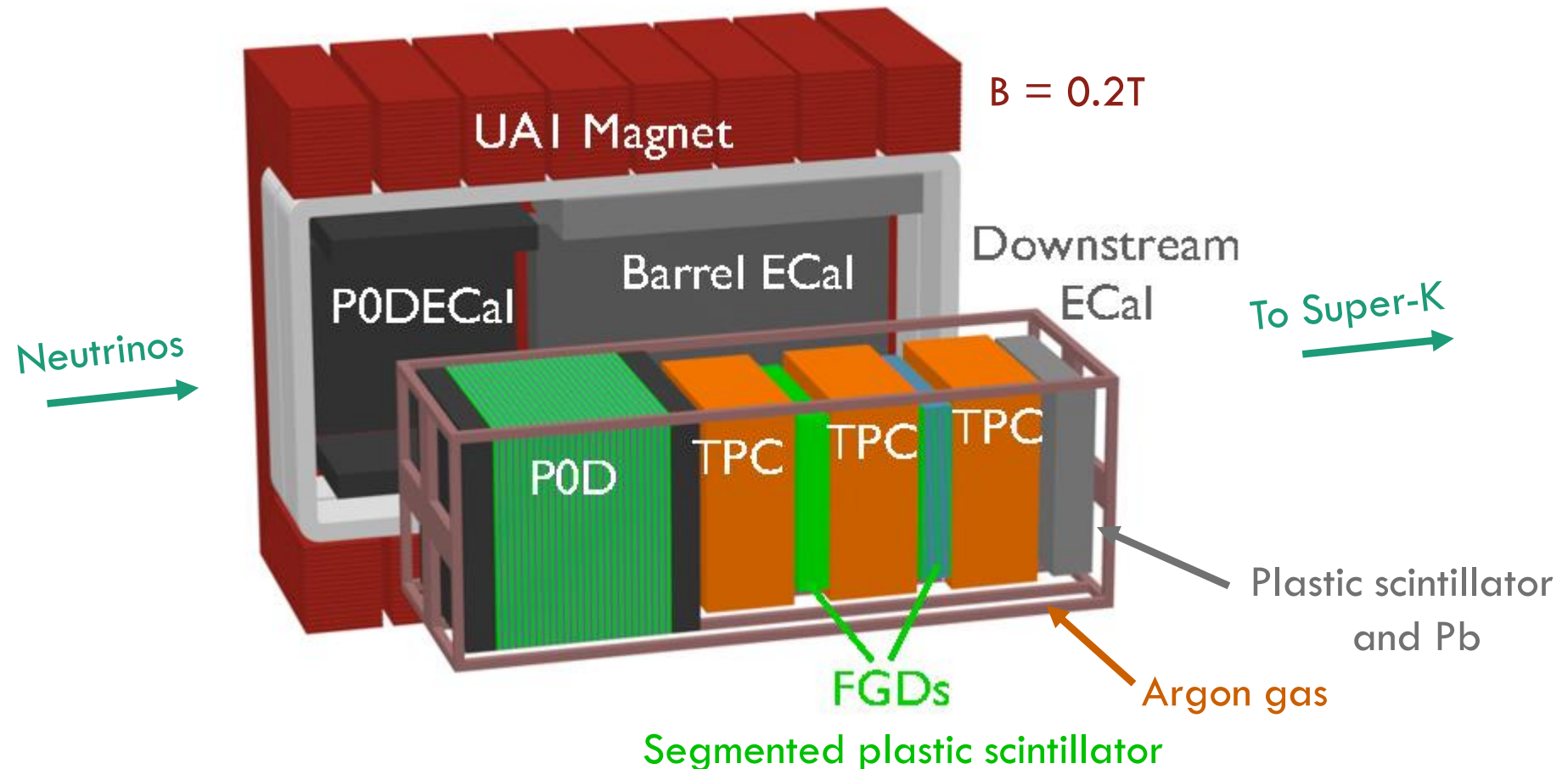
# A SLICE OF CMS



# T2K: ND280

## A GENERAL PURPOSE NEUTRINO DETECTOR

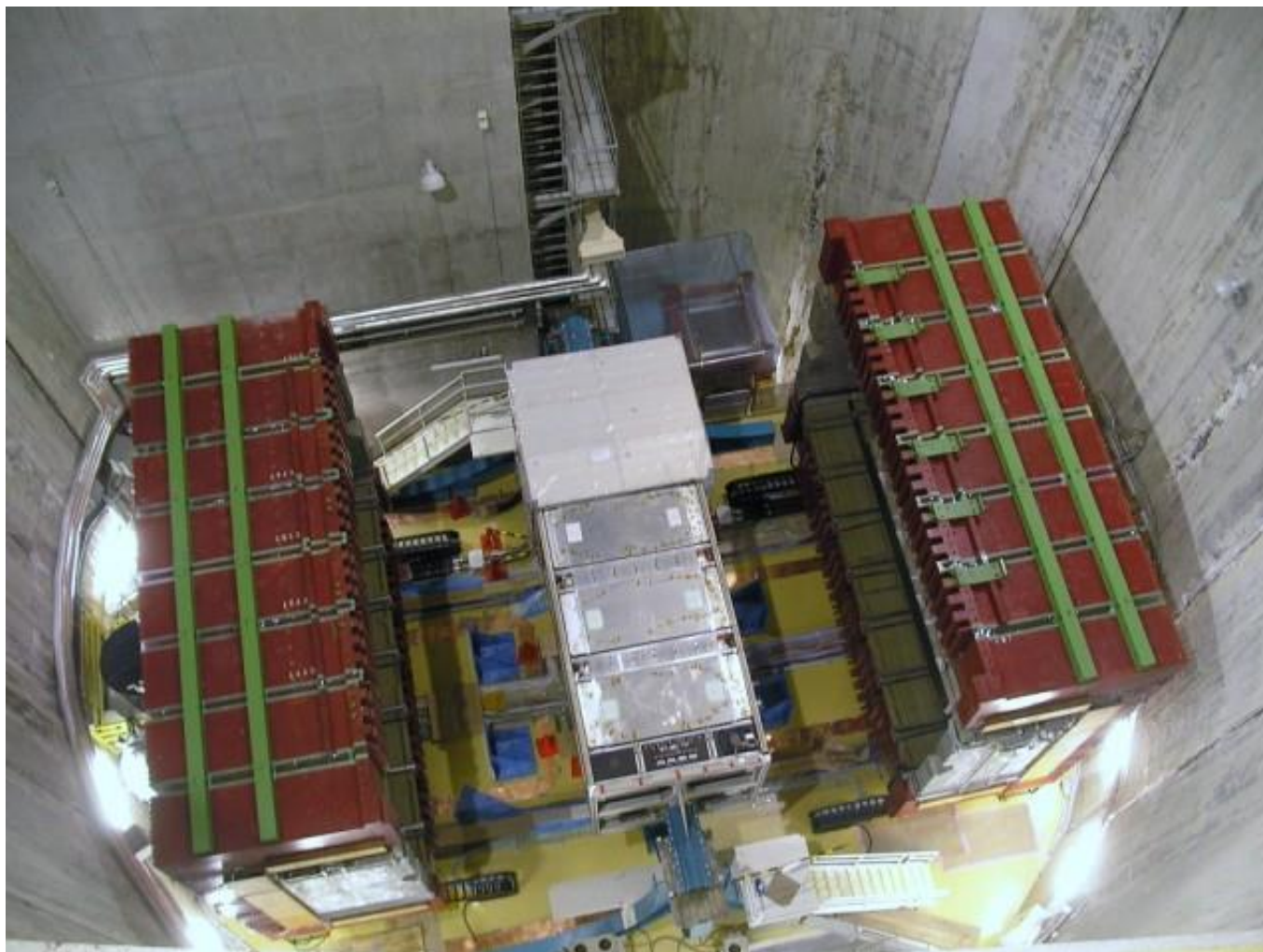
- Beam of neutrinos produced at the J-PARC proton accelerator in Japan



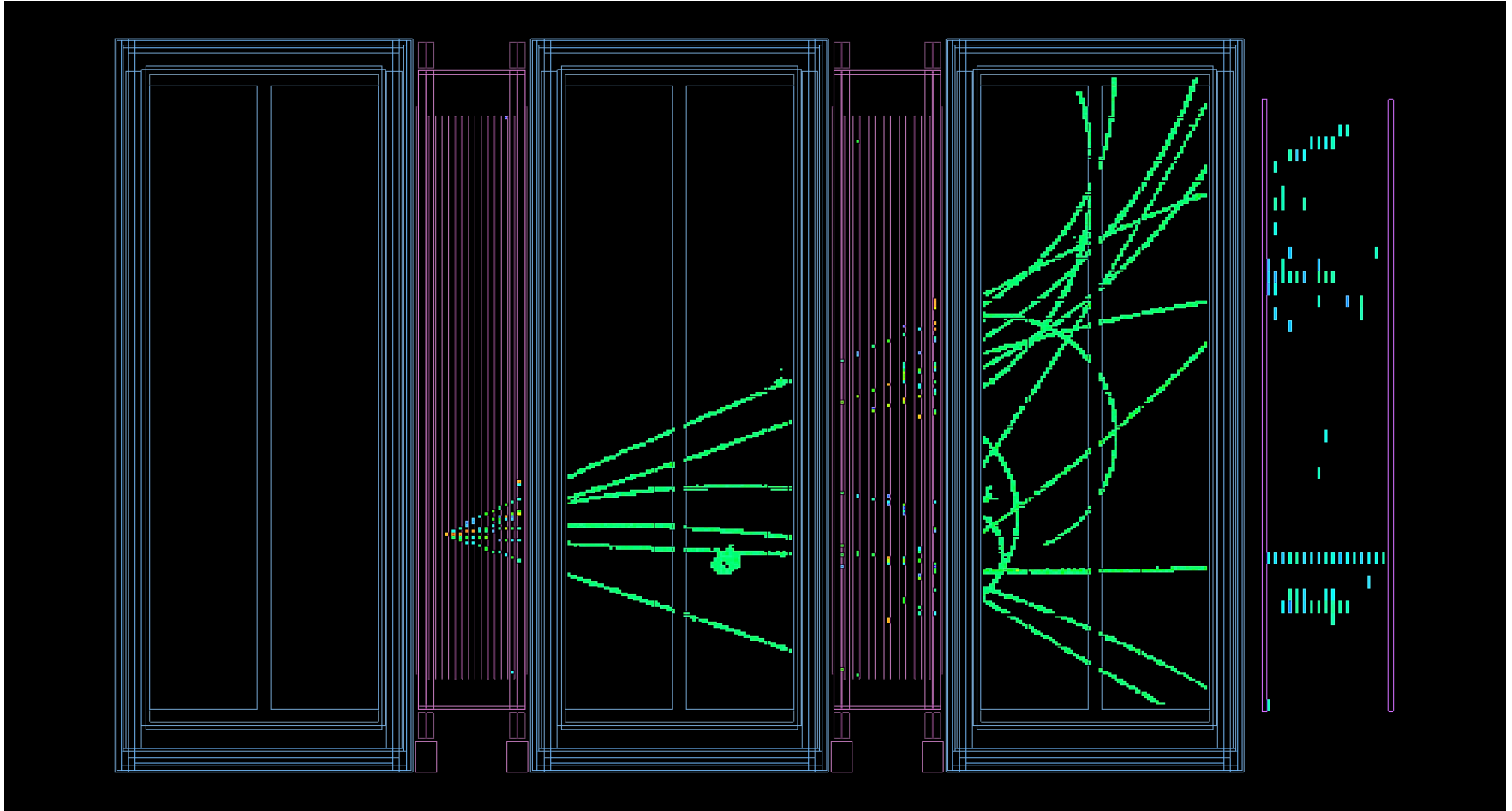


# THE ND280 DETECTOR

## WITH MAGNET OPEN FOR MAINTENANCE



# A NEUTRINO INTERACTION IN ND280

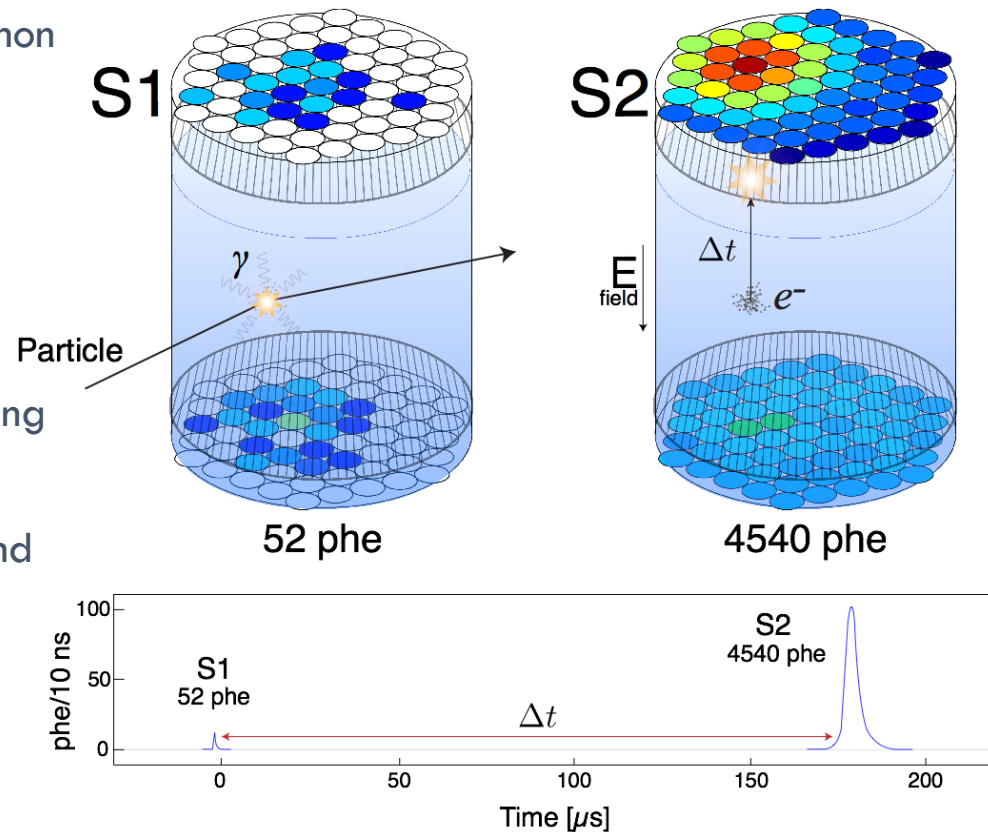


# WHAT ABOUT DARK MATTER?

- Does not interact through weak, electromagnetic, or strong force.
- But it **might interact**, very very weakly.
- We need very “quiet” (cryogenic, deep underground) detectors to see dark matter interactions.
  - Scattering off of nuclei → transfer of kinetic energy.

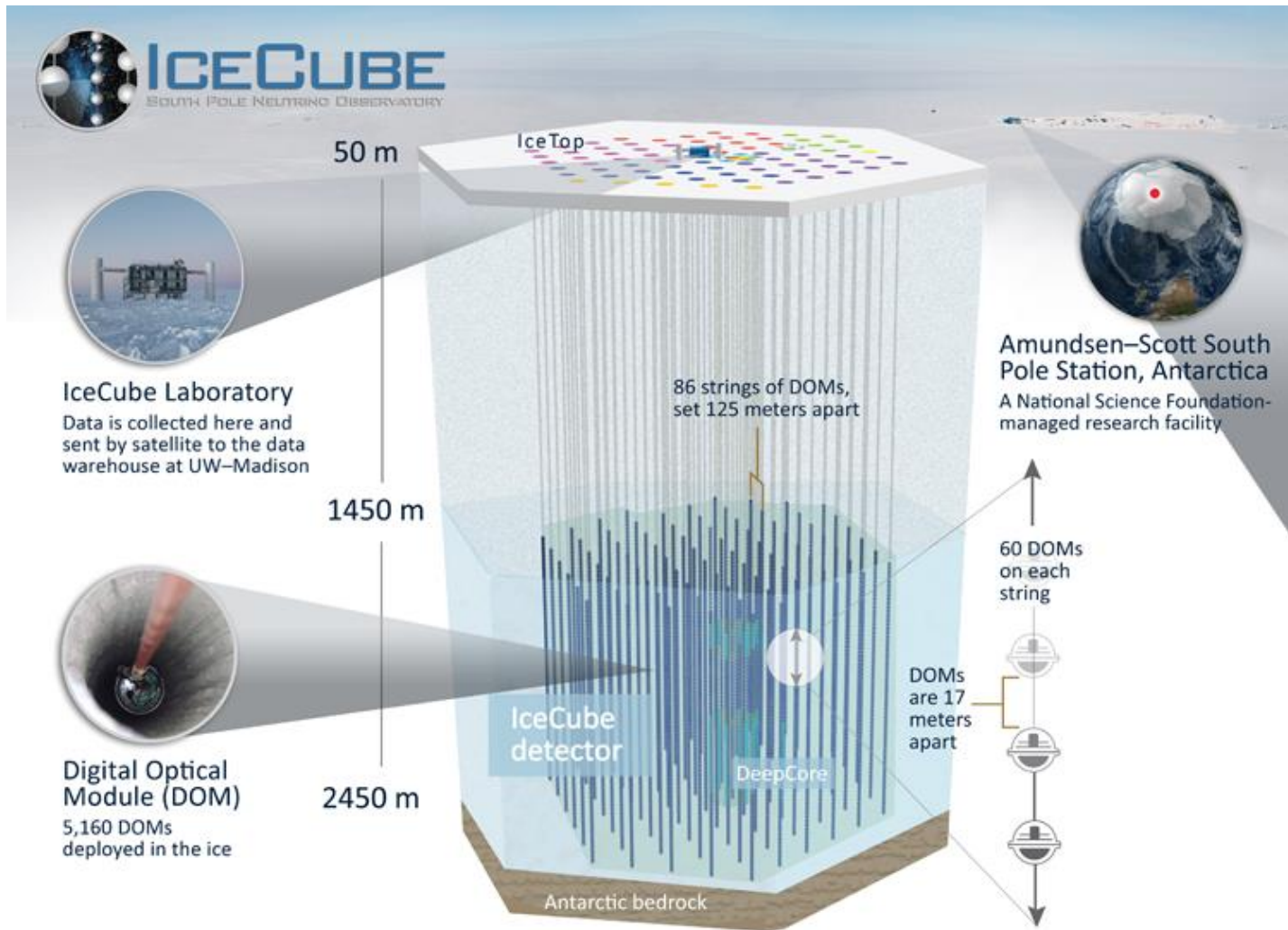
# THE LUX DARK MATTER EXPERIMENT

- The Large Underground Xenon (LUX) and XENON-1t experiments look for evidence of weakly interacting massive particle (WIMP) dark matter interactions.
- A few hundred to a ton of liquid xenon as the TPC medium.
- Aim to directly detect galactic dark matter in underground laboratories about 1 mile deep
- The detectors are shielded from background particles by a surrounding water tank and the earth above.
- This shielding reduces cosmic rays and radiation interacting with the xenon.



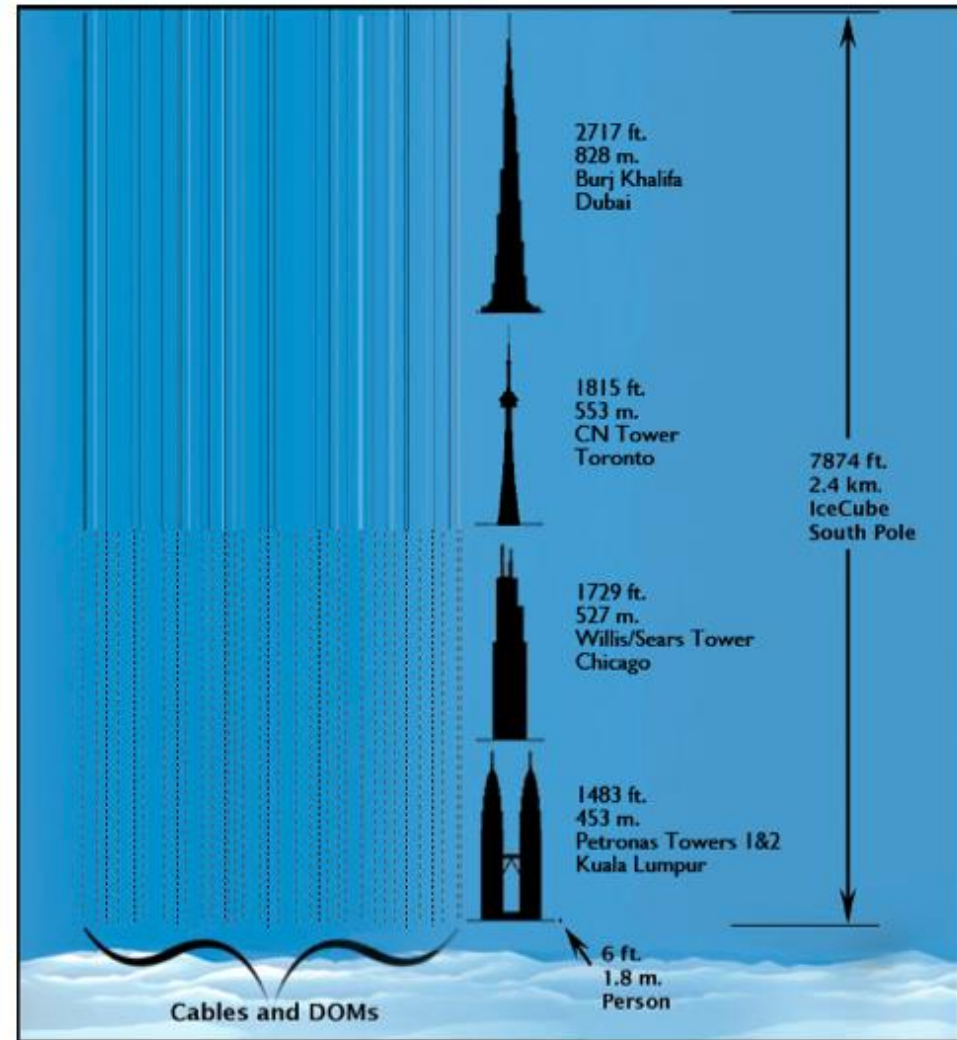


# THE ICECUBE DETECTOR



# ICE FISHING FOR SPACE NEUTRINOS!

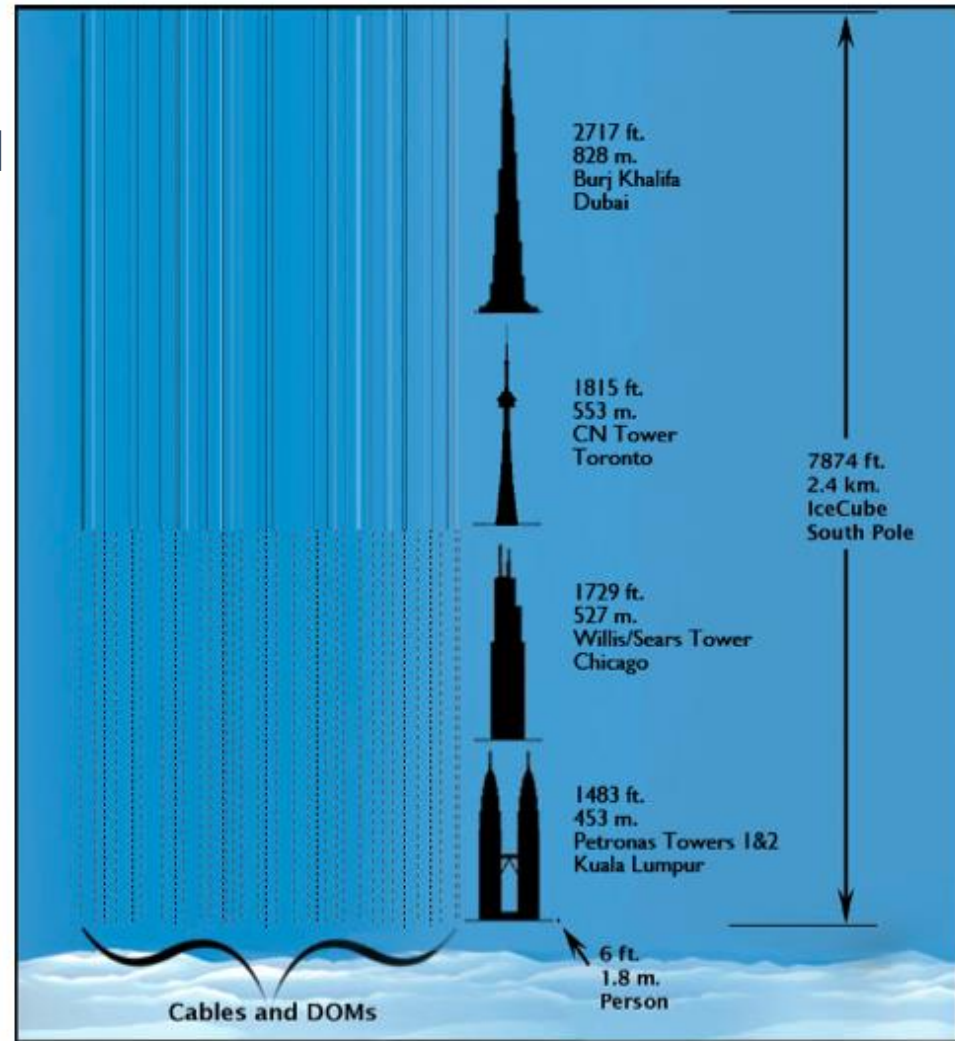
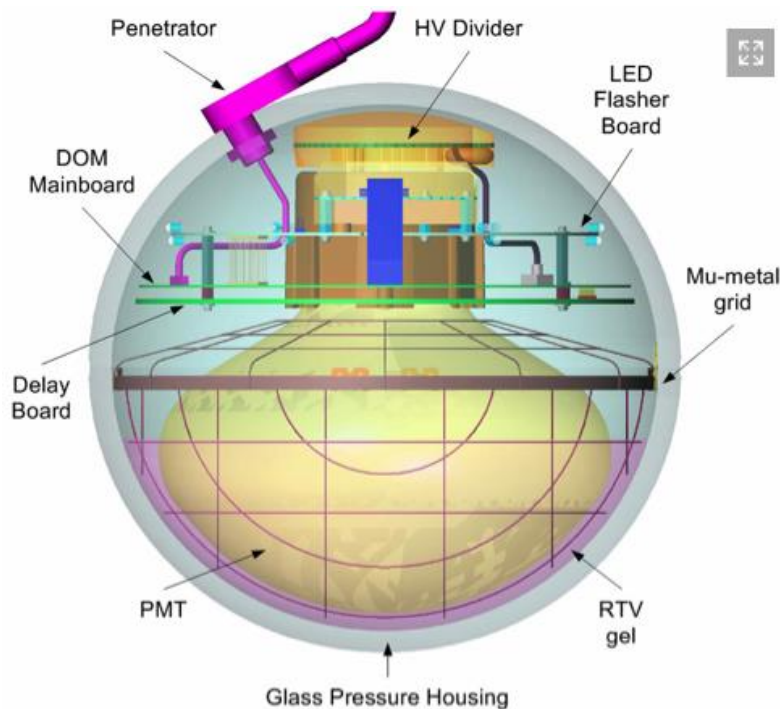
- IceCube detector at the South Pole
  - A neutrino detector: a neutrino telescope.
- Looks for extra-terrestrial sources of neutrinos.
  - Like taking an “X-ray” picture of the Universe.
- Use the Antarctic ice as a **Cherenkov detector!**



*IceCube in Scale: The dashed lines above represent the portion of the cables that have DOMs attached*

# ICE FISHING FOR SPACE NEUTRINOS!

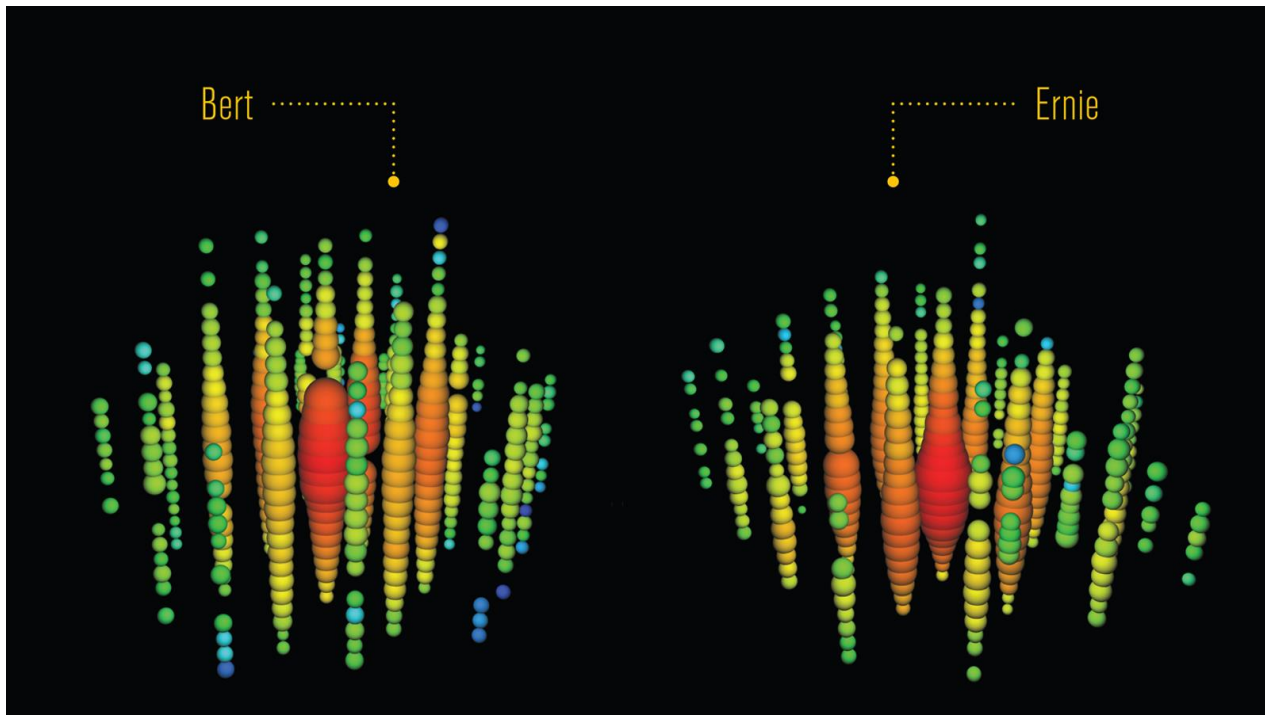
- Made up of strings of thousands of basketball-sized photon detectors
  - Digital Optical Modules



*IceCube in Scale: The dashed lines above represent the portion of the cables that have DOMs attached*

# BERT, ERNIE AND MANY OTHERS

- In 2013, IceCube announced that it had detected 28 neutrinos likely originating from outside the Solar System.
  - These are ultra-high energy (PeV) neutrino events.

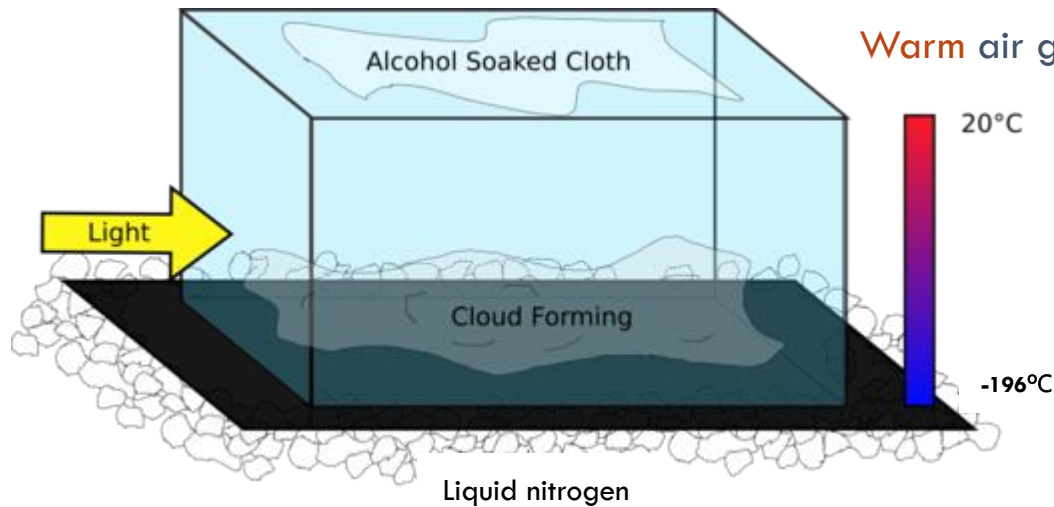


# CLOUD CHAMBER DEMONSTRATION

OLD SCHOOL PARTICLE PHYSICS!



# WHAT'S GOING ON



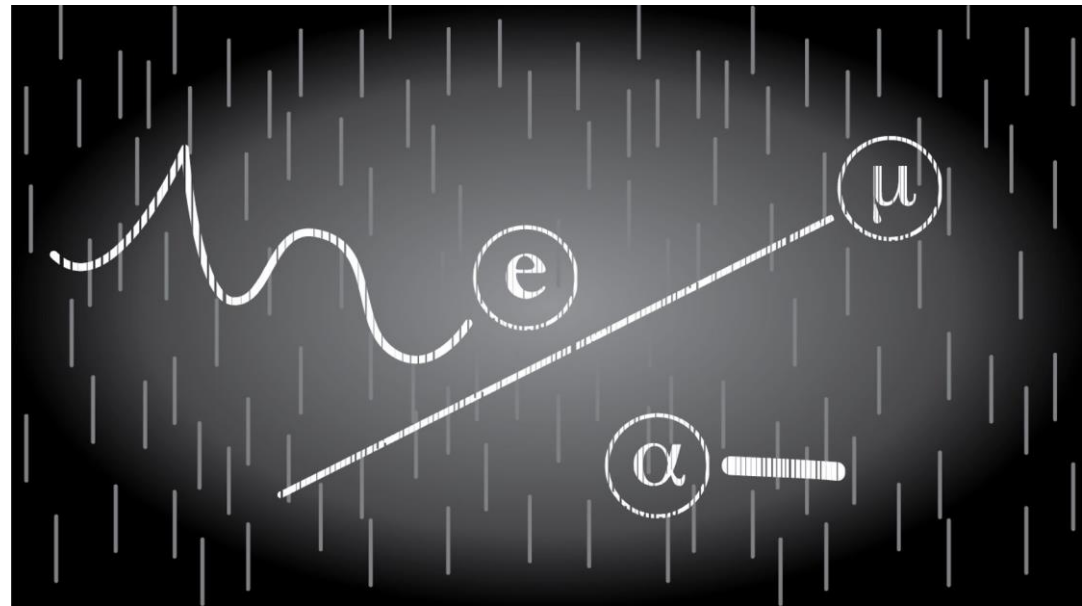
Warm air gets saturated with alcohol



As air + alcohol mix **cools** down, the alcohol vapour really wants to turn to transition to liquid... but has **nowhere** to start.

Charged particles leave **tracks** of **ionized** molecules, **seeding** the formation of "clouds".

**Thickness** of tracks depends on amount of **ionization**.



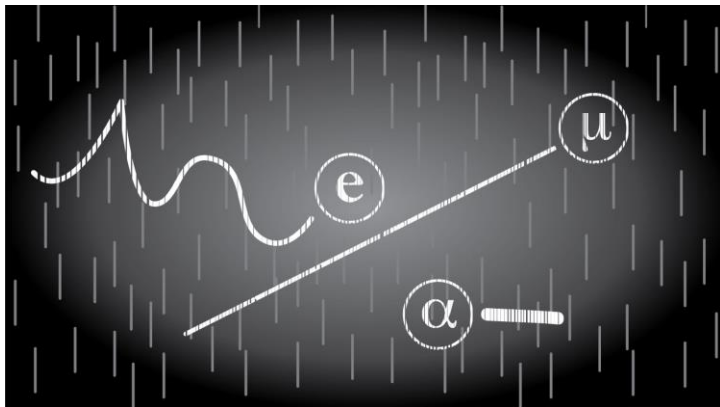
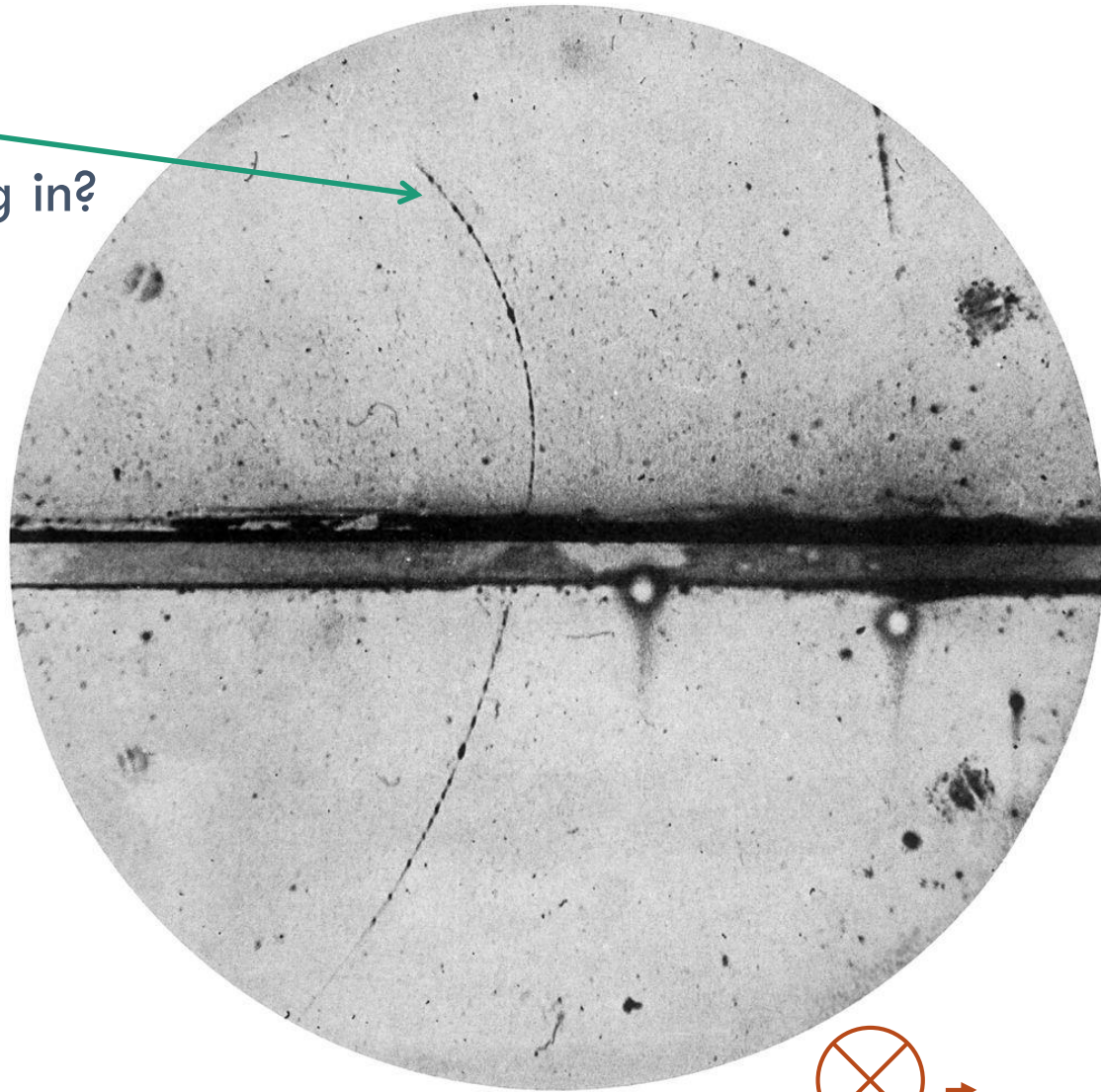


# QUIZ TIME!

What particle is this?

What direction is it travelling in?

What is its charge?





# CLOUD CHAMBER DISCOVERIES

- Positron

- C. Anderson, 1932

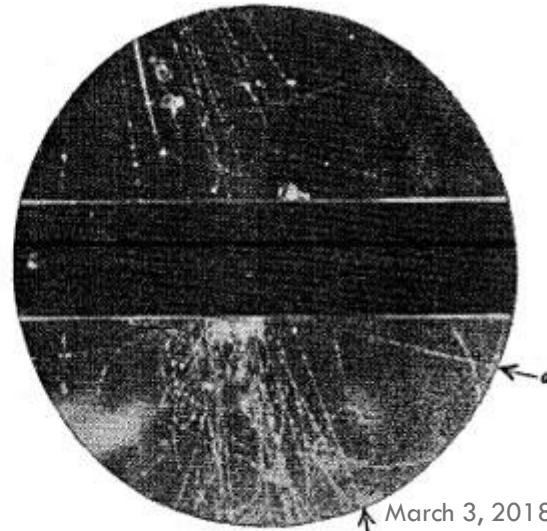
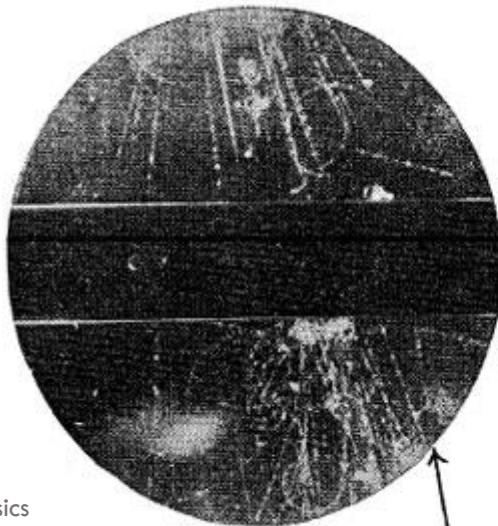
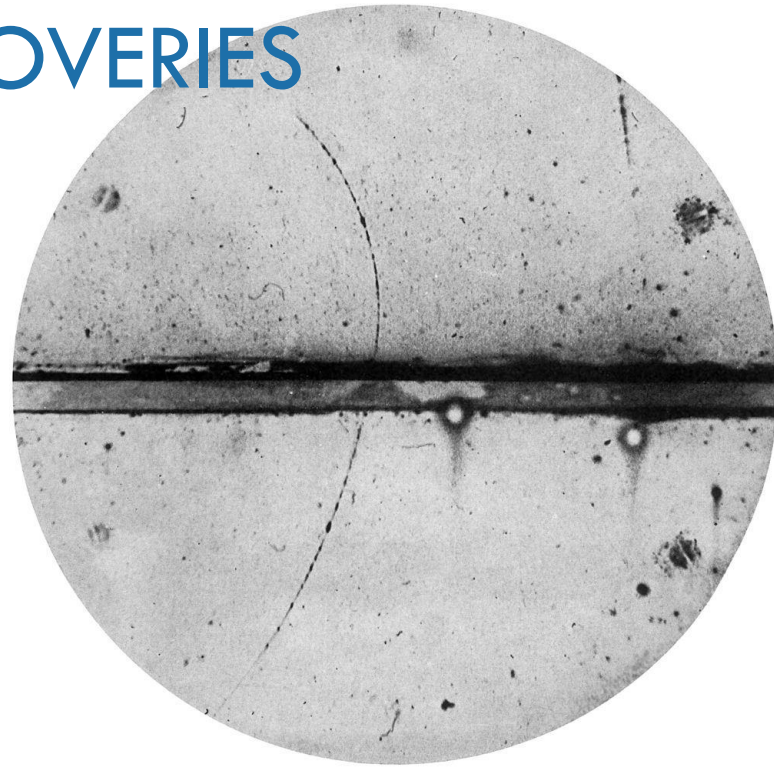


- Muon

- C. Anderson, 1936

- Kaon (meson)

- G. Rochester and C. Butler, 1947



# SCHEDULE

- ~~1. Introduction~~
- ~~2. History of Particle Physics~~
- ~~3. Special Relativity~~
- ~~4. Quantum Mechanics~~
- ~~5. Experimental Methods~~
6. The Standard Model - Overview
7. The Standard Model - Limitations
8. Neutrino Theory
9. Neutrino Experiment
10. LHC and Experiments
11. The Higgs Boson and Beyond
12. Particle Cosmology

# AN OVERVIEW OF THE STANDARD MODEL

# THE STANDARD MODEL

- The theory that attempts to fully describe the **weak**, **electromagnetic**, and **strong** interactions within a **common framework**:
- A theory of “almost everything”... does **not** accommodate:
  - Gravity
  - Dark matter, dark energy...

# THE STANDARD MODEL

- The Standard Model was solidified in the 1970's, with the discovery of quarks
  - Confirmation of theory of strong interactions.
- Under scrutiny for the last 40 years, has managed to survive\* experimental tests
  - All particles predicted by this theory have been found experimentally!
  - \* If you ignore neutrino mass...
- We already know it is incomplete
  - More next week...

# TODAY'S AGENDA

- Historical background (see lecture 2)
- Standard Model particle content
- Standard Model particle dynamics
  - Quantum Electrodynamics (QED)
  - Quantum Chromodynamics (QCD)
  - Weak Interactions
  - Force Unification
- Lagrangian / Field formulation
  - ... maybe



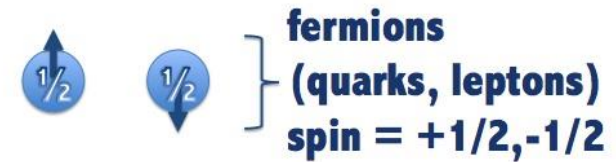
# THE WORLD, ACCORDING TO A PARTICLE PHYSICIST

<div>QUARKS</div>	<div> <div>mass → <math>\approx 2.3 \text{ MeV}/c^2</math></div> <div>charge → <math>2/3</math></div> <div>spin → <math>1/2</math></div> <div>u</div> <div>up</div> </div>	<div> <div>mass → <math>\approx 1.275 \text{ GeV}/c^2</math></div> <div>charge → <math>2/3</math></div> <div>spin → <math>1/2</math></div> <div>c</div> <div>charm</div> </div>	<div> <div>mass → <math>\approx 173.07 \text{ GeV}/c^2</math></div> <div>charge → <math>2/3</math></div> <div>spin → <math>1/2</math></div> <div>t</div> <div>top</div> </div>	<div> <div>mass → 0</div> <div>charge → 0</div> <div>spin → 1</div> <div>g</div> <div>gluon</div> </div>	<div> <div>mass → <math>\approx 126 \text{ GeV}/c^2</math></div> <div>charge → 0</div> <div>spin → 0</div> <div>H</div> <div>Higgs boson</div> </div>
	<div> <div>mass → <math>\approx 4.8 \text{ MeV}/c^2</math></div> <div>charge → <math>-1/3</math></div> <div>spin → <math>1/2</math></div> <div>d</div> <div>down</div> </div>	<div> <div>mass → <math>\approx 95 \text{ MeV}/c^2</math></div> <div>charge → <math>-1/3</math></div> <div>spin → <math>1/2</math></div> <div>s</div> <div>strange</div> </div>	<div> <div>mass → <math>\approx 4.18 \text{ GeV}/c^2</math></div> <div>charge → <math>-1/3</math></div> <div>spin → <math>1/2</math></div> <div>b</div> <div>bottom</div> </div>	<div> <div>mass → 0</div> <div>charge → 0</div> <div>spin → 1</div> <div><math>\gamma</math></div> <div>photon</div> </div>	
	<div> <div>mass → <math>0.511 \text{ MeV}/c^2</math></div> <div>charge → -1</div> <div>spin → <math>1/2</math></div> <div>e</div> <div>electron</div> </div>	<div> <div>mass → <math>105.7 \text{ MeV}/c^2</math></div> <div>charge → -1</div> <div>spin → <math>1/2</math></div> <div><math>\mu</math></div> <div>muon</div> </div>	<div> <div>mass → <math>1.777 \text{ GeV}/c^2</math></div> <div>charge → -1</div> <div>spin → <math>1/2</math></div> <div><math>\tau</math></div> <div>tau</div> </div>	<div> <div>mass → <math>91.2 \text{ GeV}/c^2</math></div> <div>charge → 0</div> <div>spin → 1</div> <div>Z</div> <div>Z boson</div> </div>	<div>GAUGE BOSONS</div>
	<div> <div>mass → <math>&lt; 2.2 \text{ eV}/c^2</math></div> <div>charge → 0</div> <div>spin → <math>1/2</math></div> <div><math>\nu_e</math></div> <div>electron neutrino</div> </div>	<div> <div>mass → <math>&lt; 0.17 \text{ MeV}/c^2</math></div> <div>charge → 0</div> <div>spin → <math>1/2</math></div> <div><math>\nu_\mu</math></div> <div>muon neutrino</div> </div>	<div> <div>mass → <math>&lt; 15.5 \text{ MeV}/c^2</math></div> <div>charge → 0</div> <div>spin → <math>1/2</math></div> <div><math>\nu_\tau</math></div> <div>tau neutrino</div> </div>	<div> <div>mass → <math>80.4 \text{ GeV}/c^2</math></div> <div>charge → <math>\pm 1</math></div> <div>spin → 1</div> <div>W</div> <div>W boson</div> </div>	

# THE STANDARD MODEL PARTICLE CONTENT

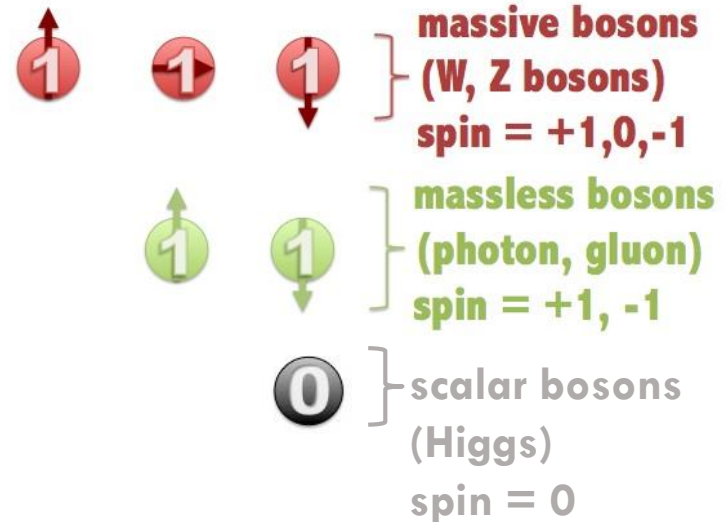
- **Fermions:**

- Quarks and Leptons
- Half-integer spin



- **Bosons:**

- Force mediators and the Higgs
- Integer spin



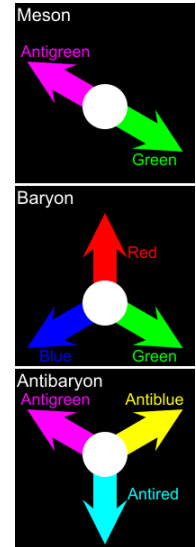
# PARTICLE CHARGES

Electric   Weak   Color

Quarks   ✓   ✓   ✓

- Quarks:

- There are **no** free quarks.
- They form **colorless** composite objects, hadrons;
  - Baryons:  $qqq, \bar{q}\bar{q}\bar{q}$
  - Mesons:  $q\bar{q}, q\bar{q}, q\bar{q}$



Name	Symbol	Mass (MeV/c <sup>2</sup> ) <sup>*</sup>	<i>J</i>	<i>B</i>	<i>Q</i>	<i>I</i> <sub>3</sub>	<i>C</i>	<i>S</i>	<i>T</i>	<i>B'</i>	Antiparticle	Antiparticle symbol
<b>First generation</b>												
Up	u	1.7 to 3.3	1/2	+1/3	+2/3	+1/2	0	0	0	0	Antiup	$\bar{u}$
Down	d	4.1 to 5.8	1/2	+1/3	-1/3	-1/2	0	0	0	0	Antidown	$\bar{d}$
<b>Second generation</b>												
Charm	c	1,270 <sup>+70</sup> <sub>-90</sub>	1/2	+1/3	+2/3	0	+1	0	0	0	Anticharm	$\bar{c}$
Strange	s	101 <sup>+29</sup> <sub>-21</sub>	1/2	+1/3	-1/3	0	0	-1	0	0	Antistrange	$\bar{s}$
<b>Third generation</b>												
Top	t	172,000 ± 900 ± 1,300	1/2	+1/3	+2/3	0	0	0	+1	0	Antitop	$\bar{t}$
Bottom	b	4,190 <sup>+180</sup> <sub>-60</sub>	1/2	+1/3	-1/3	0	0	0	0	-1	Antibottom	$\bar{b}$

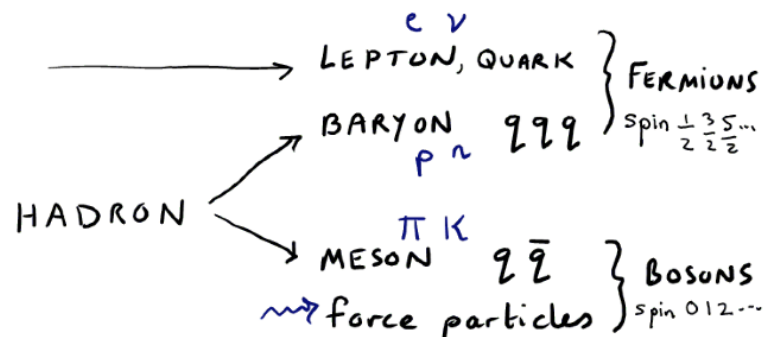
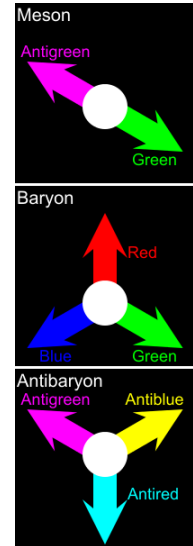
*J* = total angular momentum, *B* = baryon number, *Q* = electric charge, *I*<sub>3</sub> = isospin, *C* = charm, *S* = strangeness, *T* = topness, *B'* = bottomness.

# PARTICLE CHARGES

	Electric	Weak	Color
Quarks	✓	✓	✓

- Quarks:

- There are **no** free quarks.
- They form **colorless** composite objects, hadrons;
  - Baryons:  $qqq, \bar{q}\bar{q}\bar{q}$
  - Mesons:  $q\bar{q}, q\bar{q}, q\bar{q}$



# PARTICLE CHARGES

- Leptons

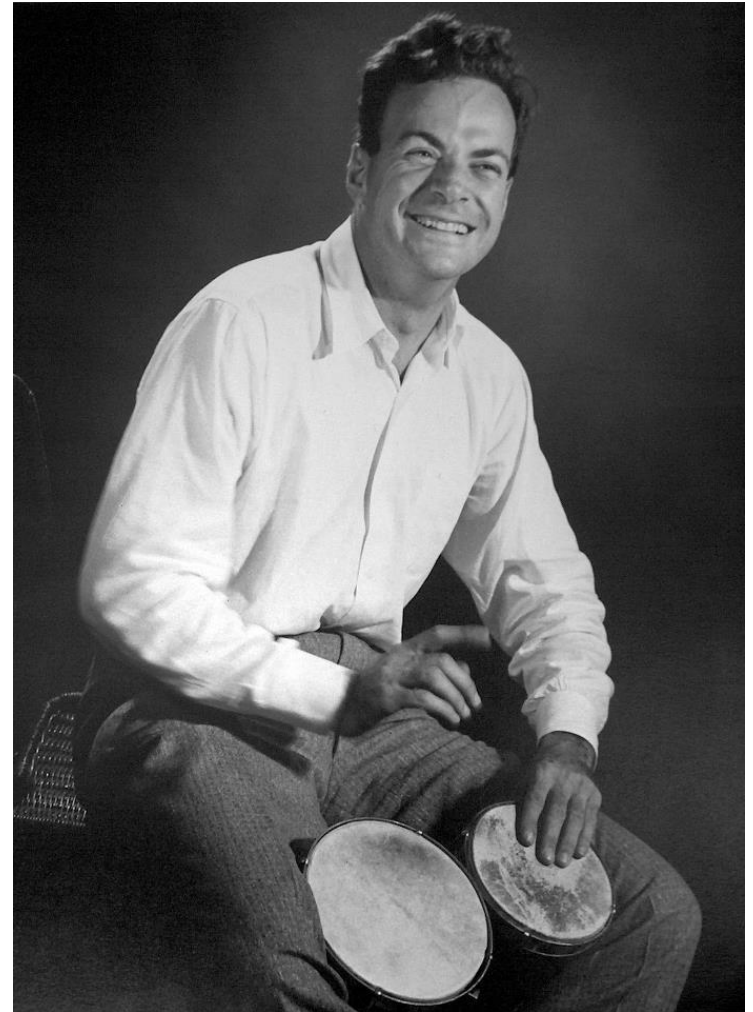
- Exist as **free** particles

	Electric	Weak	Color
Quarks	✓	✓	✓
Leptons			
Charged	✓	✓	✗
Neutral	✗	✓	✗

Particle/Antiparticle Name	Symbol	Q (e)	S	L <sub>e</sub>	L <sub>μ</sub>	L <sub>τ</sub>	Mass (MeV/c <sup>2</sup> )	Lifetime (s)
Electron / Antielectron <sup>[17]</sup>	$e^-/e^+$	-1/+1	1/2	+1/-1	0	0	0.510 998 910(13)	Stable
Muon / Antimuon <sup>[18]</sup>	$\mu^-/\mu^+$	-1/+1	1/2	0	+1/-1	0	105.658 3668(38)	$2.197\,019(21) \times 10^{-6}$
Tau / Antitau <sup>[20]</sup>	$\tau^-/\tau^+$	-1/+1	1/2	0	0	+1/-1	1,776.84(17)	$2.906(10) \times 10^{-13}$
Electron neutrino / Electron antineutrino <sup>[33]</sup>	$\nu_e/\bar{\nu}_e$	0	1/2	+1/-1	0	0	$< 0.000\,0022^{[35]}$	Unknown
Muon neutrino / Muon antineutrino <sup>[33]</sup>	$\nu_\mu/\bar{\nu}_\mu$	0	1/2	0	+1/-1	0	$< 0.17^{[35]}$	Unknown
Tau neutrino / Tau antineutrino <sup>[33]</sup>	$\nu_\tau/\bar{\nu}_\tau$	0	1/2	0	0	+1/-1	$< 15.5^{[35]}$	Unknown

# PARTICLE DYNAMICS: FEYNMAN DIAGRAMS

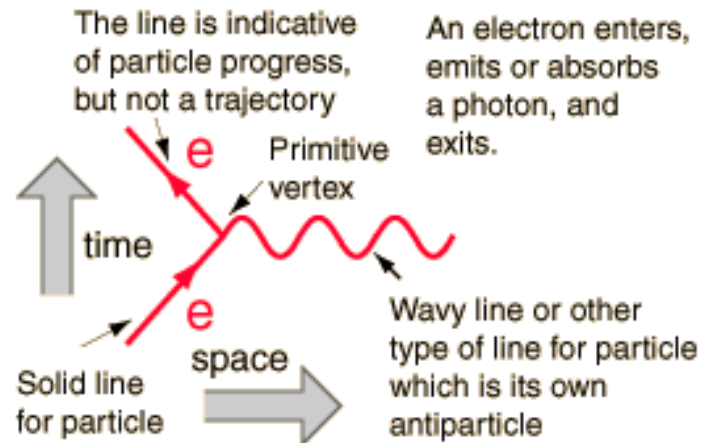
- Feynman Rules!
- 1948: introduced pictorial representation scheme for the mathematical expressions governing the behavior of subatomic particles.
  - Can be used to easily calculate probability amplitudes
  - Other options: cumbersome mathematical derivations





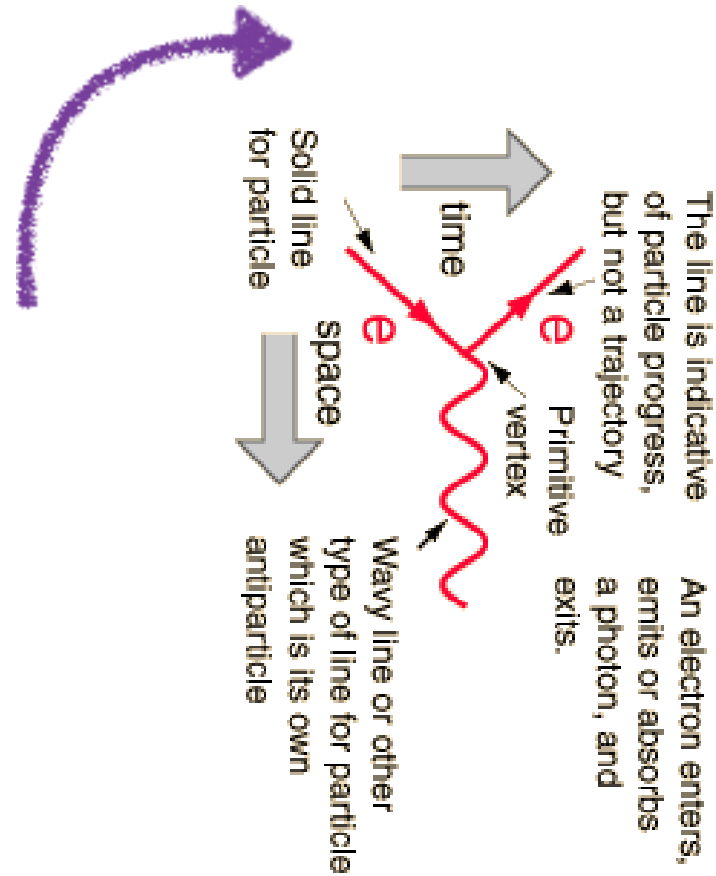
# FEYNMAN DIAGRAMS

- How to read them:



# FEYNMAN DIAGRAMS

- How to read them:

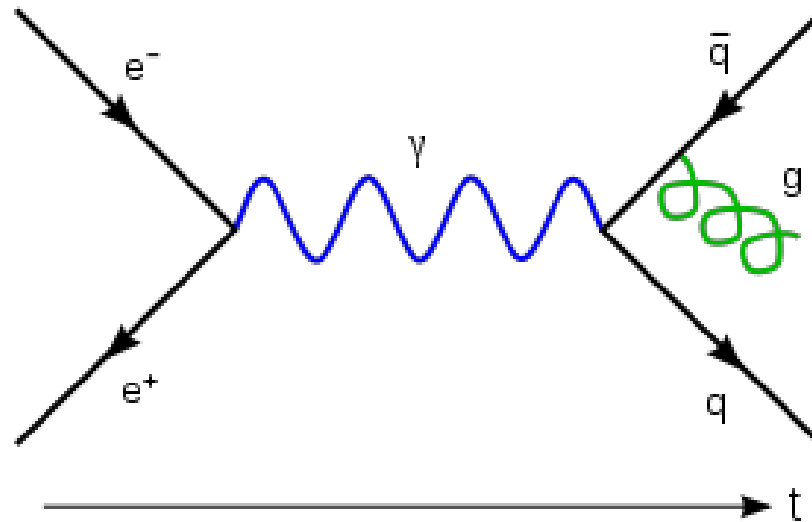


Beware of the time direction!  
(You'll see it used in either way.)

If  $t$  was on  $y$ -axis, this would be a different process.

# FEYNMAN DIAGRAMS

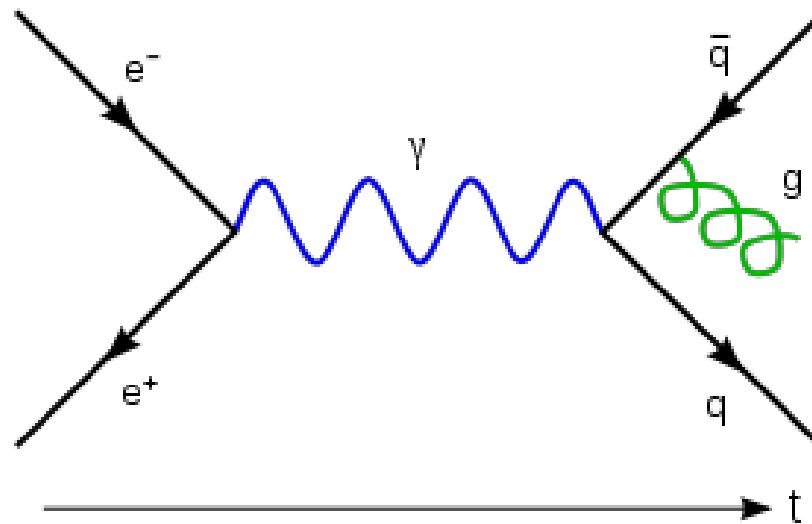
## AN EXAMPLE



1. An electron and a positron **annihilate** into
2. a virtual **photon** that **produces**
3. a quark-antiquark pair, one of which radiates
4. A **gluon**

# FEYNMAN DIAGRAMS

## AN EXAMPLE

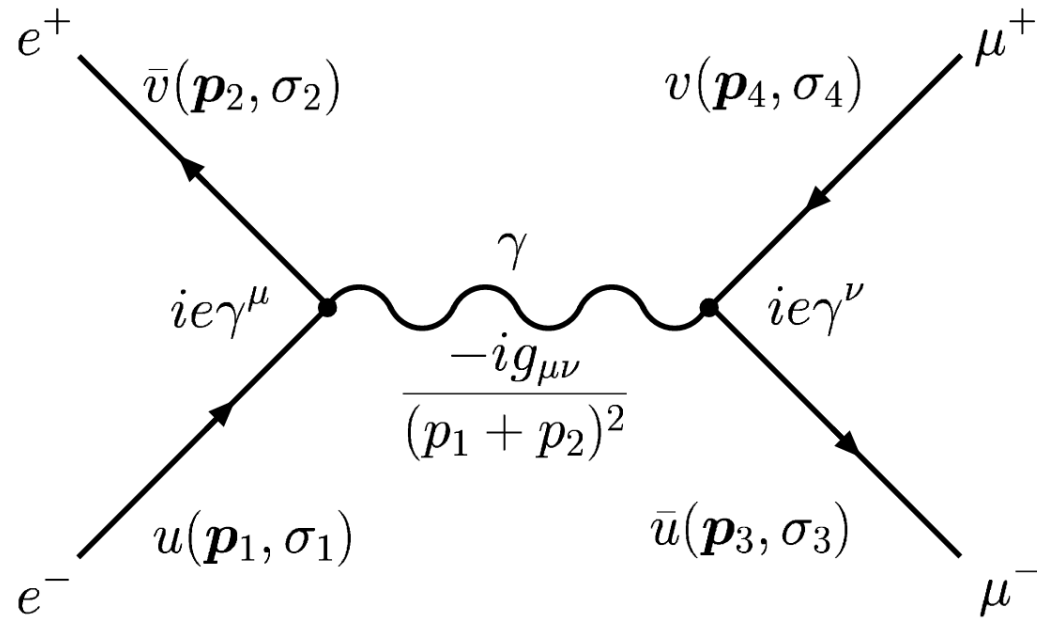


Note, at every vertex:  
Q conservation  
L conservation  
 $L_e$  conservation  
B conservation

1. An electron and a positron **annihilate** into
2. a virtual **photon** that **produces**
3. a quark-antiquark pair, one of which radiates
4. A **gluon**

# FEYNMAN DIAGRAMS

## AN EXAMPLE CALCULATION



$$-i\mathcal{M} = [\bar{u}(\mathbf{p}_3, \sigma_3)(ie\gamma^\nu)v(\mathbf{p}_4, \sigma_4)] \frac{-ig_{\mu\nu}}{(p_1 + p_2)^2} [\bar{v}(\mathbf{p}_2, \sigma_2)(ie\gamma^\mu)u(\mathbf{p}_1, \sigma_1)]$$

# QED, QCD AND WEAK INTERACTIONS



# QUANTUM ELECTRODYNAMICS

## QED

- As you already know, **electromagnetism** is the dominant physical force in your life. All of your daily interactions - besides your attraction to the Earth - are electromagnetic in nature.
- As a theory of electromagnetism, QED is primarily concerned with the behavior and interactions of **charged particles** with **each other** and with **light**.
- As a **quantum theory**, QED works in the submicroscopic world, where particles follow all possible paths and can blink in and out of existence (more later).

# QUANTUM ELECTRODYNAMICS

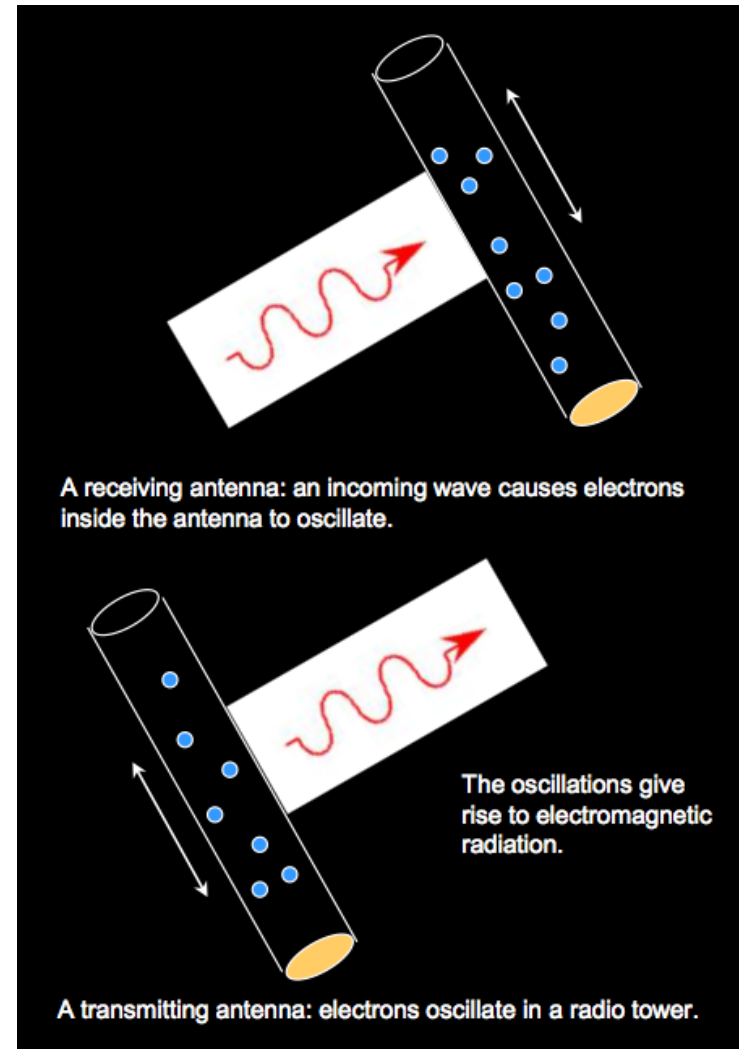
## QED

- In classical EM, light is a **wave**, and **matter** is made up of **charged particles**.
- **Charge** is always **conserved**; particles are never created or destroyed.
- EM **fields interact** with **charges** according to the Lorentz force law:

$$\vec{F} = q \left( \vec{E} + \vec{v} \times \vec{B} \right)$$

- **Accelerating charges** radiate EM waves (Larmor power formula):

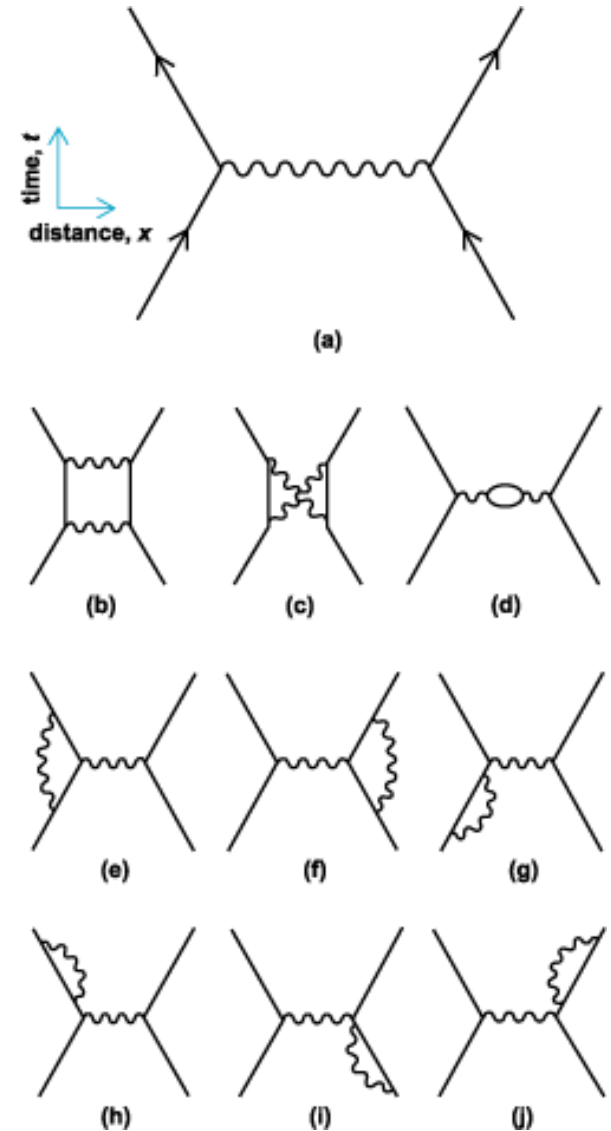
$$P = \frac{2}{3} \frac{q^2 a^2}{c^3}$$



# QUANTUM ELECTRODYNAMICS

## QED

- The **vertices** are **interactions** with the electromagnetic field.
- The **straight lines** are **electrons** and the **wiggly** ones are **photons**.
- Between interactions (vertices), particles **propagate** as free particles.
- The **higher** the number of **vertices**, the **less likely** for the interaction to happen.
  - Higher “order”.



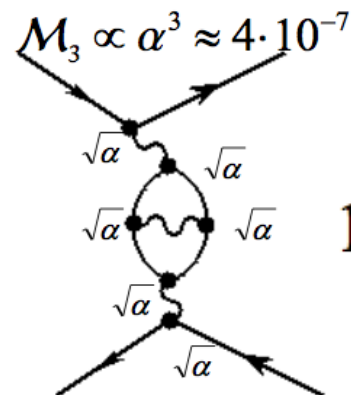
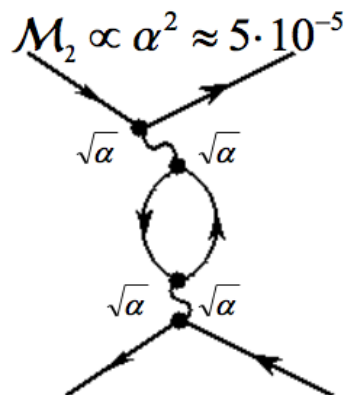
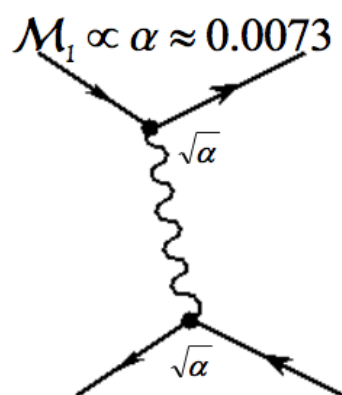
# QUANTUM ELECTRODYNAMICS

## QED

- Each **vertex** contributes a **coupling constant**  $\sqrt{\alpha}$ , where  $\alpha$  is a small dimensionless number:

$$\alpha = \frac{e^2}{\hbar c} \approx \frac{1}{137}$$

- Hence, **higher-order** diagrams get **suppressed** relative to diagrams with fewer vertices.

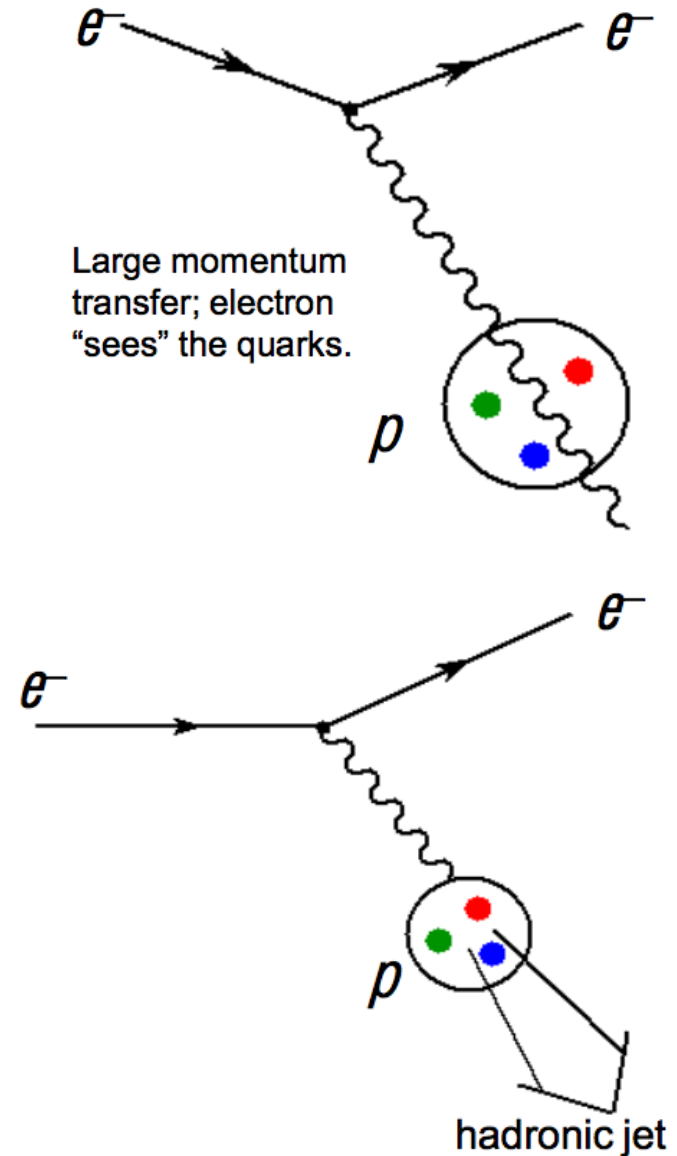


$$\mathcal{M}_1 : \mathcal{M}_2 : \mathcal{M}_3$$

$$18769 : 137 : 1$$

# WHEN QED IS NOT ENOUGH

- Higher energy interactions involving **hadrons** will result in the production of new particles.
- In this type of *inelastic scattering*, in which two colliding particles can form (hundreds of) new **hadrons**.
- QED **cannot** explain phenomena like inelastic scattering.
  - We need an additional theory of particle interactions.



# QUANTUM CHROMODYNAMICS

## QCD

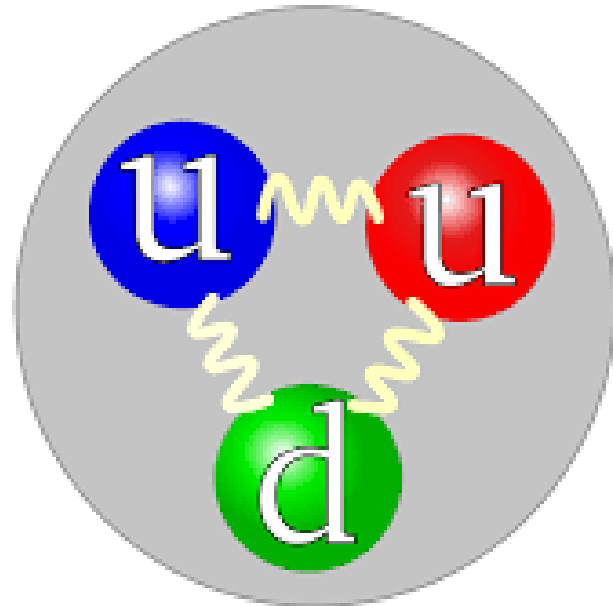
- QCD can explain many phenomena not covered by QED.
- The binding of nucleons in atoms and the phenomena of inelastic scattering are both explained by a single field theory of quarks and gluons: QCD.
- QCD describes the interactions between quarks via the exchange of massless gluons.
- Note: the quark-gluon interactions are also responsible for the binding of quarks into the bound states that make up the hadron zoo ( $\rho$ 's,  $\eta$ 's,  $\Lambda$ ,  $\Xi$ ,  $\Sigma$ 's, ...).
- QCD is conceptually similar to QED, but its calculations are even more complicated. We'll discuss why...



# QUANTUM CHROMODYNAMICS

## QCD

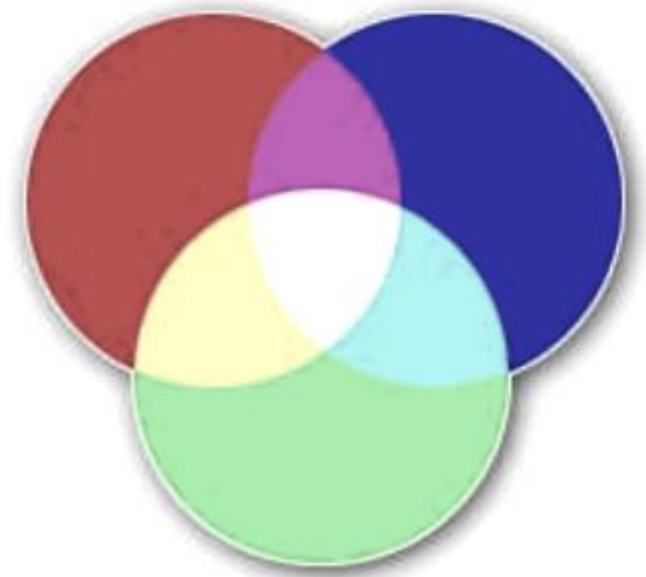
- Quarks and **bound states**:
  - Since quarks are **spin-1/2** particles (fermions), they must obey the **Pauli Exclusion Principle**.
- **Pauli Exclusion Principle**: fermions in a bound state (e.g., the quarks inside a hadron) **cannot** have the **same quantum numbers**.
- Then, how can we squeeze **three** quarks into a baryon?
- Give them an **additional charge**, called color.
- This **removes** the quantum numbers **degeneracy**.



# QUANTUM CHROMODYNAMICS

## QCD

- Quarks and **bound states**:
  - Since quarks are **spin-1/2** particles (fermions), they must obey the **Pauli Exclusion Principle**.
- **Pauli Exclusion Principle**: fermions in a bound state (e.g., the quarks inside a hadron) **cannot** have the **same quantum numbers**.
- Proposal: quark **color** comes in three types: **red**, **green**, and **blue**;
- All free, **observable** particles are **colorless**



Red, blue, and green combine to give white (color-neutral).

# QUANTUM CHROMODYNAMICS

## QCD

- Gluons carry a **color** and an **anti-color**.
- There are **9 possible combinations**, but 1 is white, which is not allowed.
  - **No evidence** for colorless particles exchanging gluons.
- This leaves **8 types of gluon**.

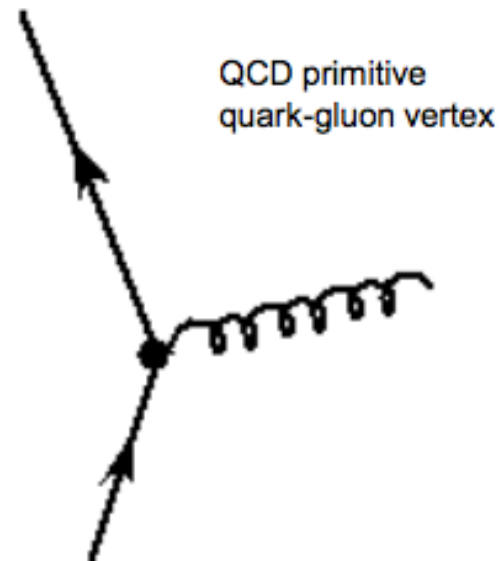
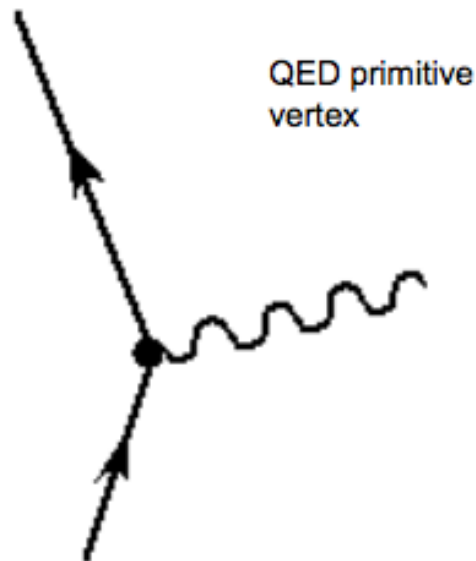
A quark changes color by emitting or absorbing gluons.



# QUANTUM CHROMODYNAMICS

## QCD

- Quarks are **electrically charged**, so they also interact via the electromagnetic force, exchanging **photons**.
- The **strong** interaction is **gluon-mediated**, the Feynman diagram for the **quark-gluon** vertex looks just like the primitive **QED** vertex.



# QCD VS QED

- QCD is **much harder** to handle than QED.
- What makes it so difficult? Let's start with perturbation theory.
- Recall: In QED, each vertex contributes **a coupling constant**  $\sqrt{\alpha}$ , where  $\alpha$  is **a small dimensionless number**:

$$\alpha = \frac{e^2}{\hbar c} \approx \frac{1}{137}$$

- Hence, we saw that **higher-order** diagrams (diagrams with more vertices) **get suppressed** relative to diagrams with fewer vertices.

# PERTURBATION THEORY

## ASIDE

- Use a **power series** in a parameter  $\epsilon$  (such that  $\epsilon \ll 1$ ) - known as perturbation series - as an **approximation** to the full solution.
- For example:

$$A = A_0 + \epsilon A_1 + \epsilon^2 A_2 + \dots$$

- In this example,  $A_0$  is the “**leading order**” solution, while  $A_1, A_2, \dots$  represent higher order terms.
- **Note:** if  $\epsilon$  is **small**, the higher-order terms in the series become successively smaller.
- Approximation:

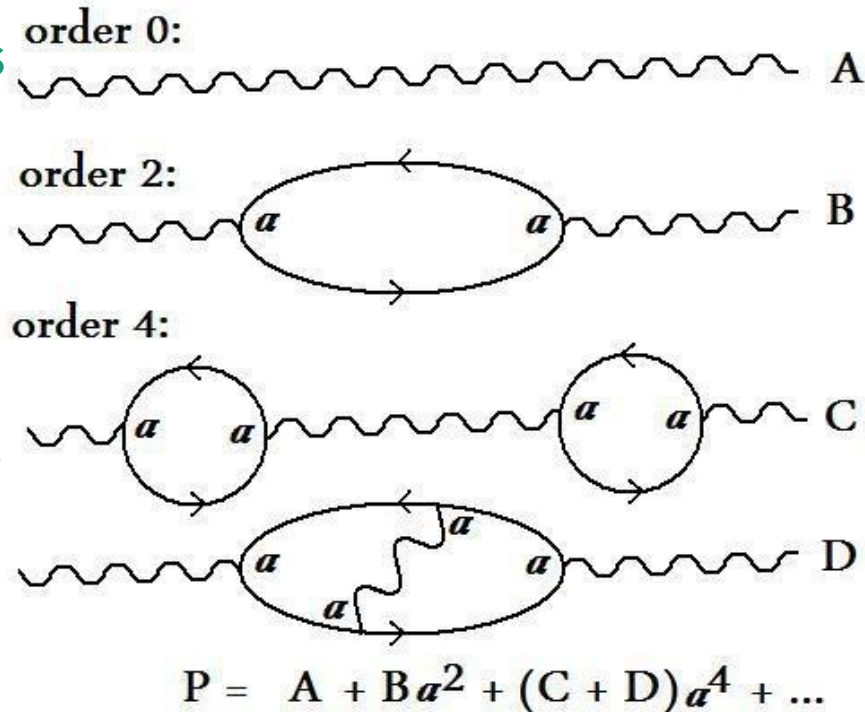
$$A \approx A_0 + \epsilon A_1$$



# PERTURBATION THEORY IN QFT

## ASIDE

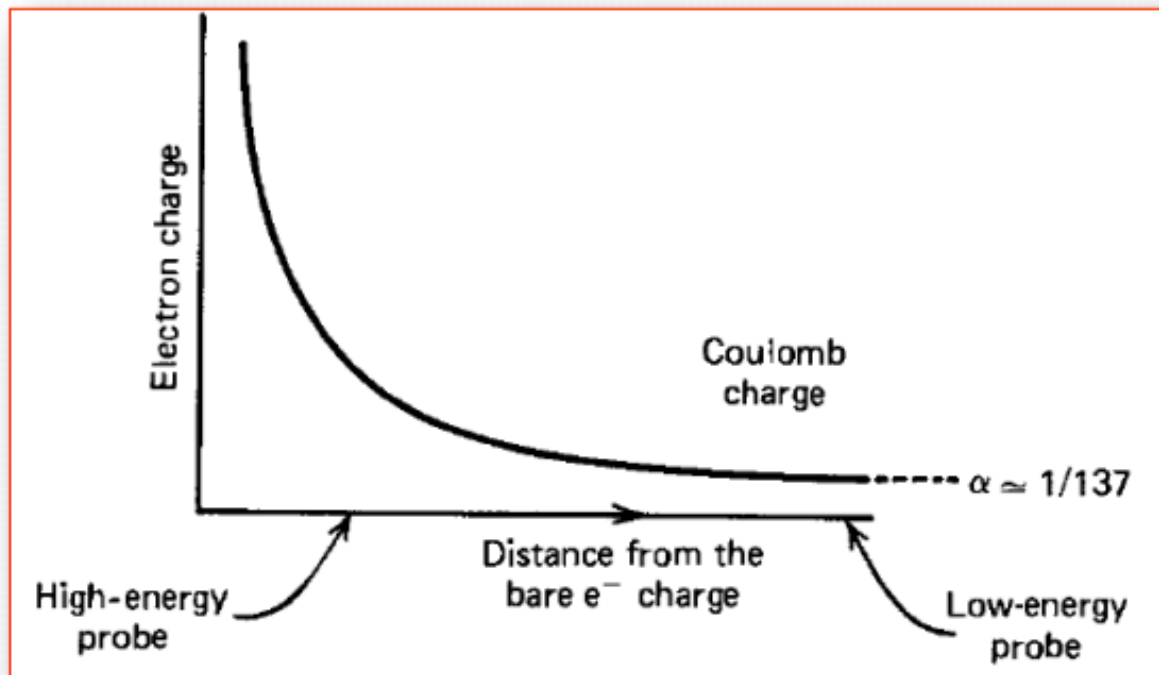
- Perturbation theory allows for well-defined predictions in quantum field theories (as long as they obey certain requirements).
- Quantum electrodynamics is one of those theories.
- Feynman diagrams correspond to the terms in the perturbation series!



Diagrams define a series in  $\alpha$

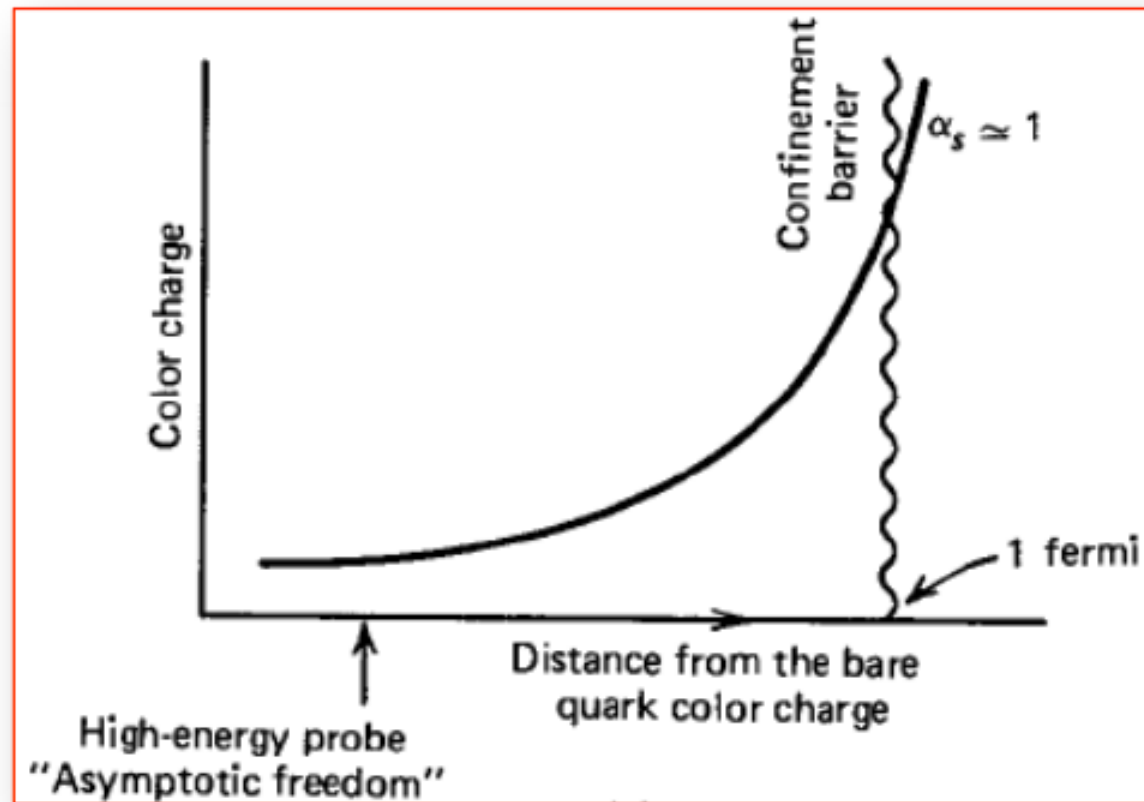
# QCD VS QED

- Recall: In QED, each vertex contributes a **coupling constant**  $\sqrt{\alpha}$ .
- $\alpha$  is not exactly a **constant** though... it “**runs**” with the scale of the interaction.



# QCD VS QED

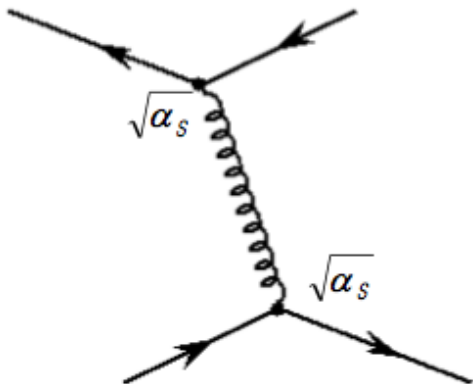
- The coupling constant for QCD,  $\alpha_s$ , “runs” in a different way with energy.



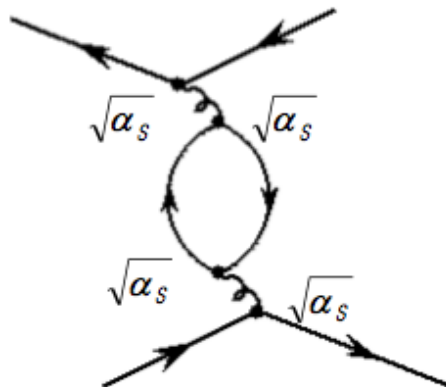
# QCD VS QED

- In QCD, the coupling between quarks and gluons, given by the number  $\alpha_s$ , is **much larger** than  $1/137$  at **low energies**.
- In fact, at low energies,  $\alpha_s \gg 1$ , making **higher-order** diagrams just as **important** as those with fewer vertices!
- This means we can't **truncate** the sum over diagrams.
  - **Perturbation** theory is **not** a good approximation!
- Calculations quickly become **complicated**!

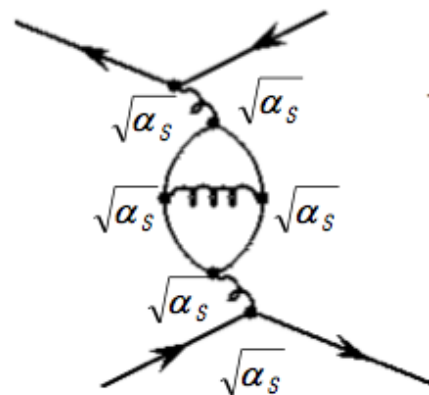
$$\mathcal{M}_1 \propto \alpha_s \approx 1$$



$$\mathcal{M}_2 \propto \alpha_s^2 \approx 1$$



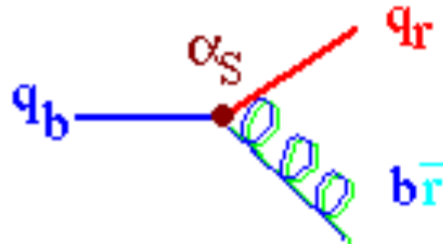
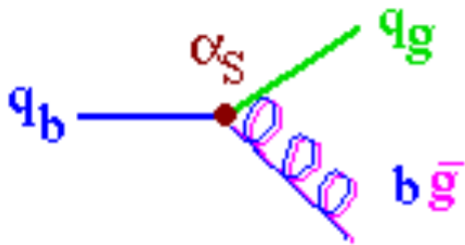
$$\mathcal{M}_3 \propto \alpha_s^3 \approx 1$$



$$\mathcal{M}_1 : \mathcal{M}_2 : \mathcal{M}_3 \\ 1 : 1 : 1$$

# ANOTHER COMPLICATION: GLUON COLOR

- Quark **color changes** at a quark-gluon **vertex**.
- In order to allow this, the **gluons** have to **carry off** “excess” **color**.
- **Color** is **conserved** at the vertex, like **electric charge** is **conserved** in QED.



Color, like electric charge, must be conserved at every vertex. This means that the gluons cannot be color-neutral, but in fact carry some color charge. It turns out that there are 8 distinct color combinations!

- **Gluons** themselves are **not color-neutral**. That's why we **don't observe** them outside the nucleus, where only **colorless** particles exist.
- Hence, **the strong force** is **short-range**.

# GLUON CONFINEMENT

- **Confinement** is the formal name for what we just discussed.
- The long-range interactions between gluons are theoretically **unmanageable**. The math is very complicated and riddled throughout with **infinities**.
- If we assume the massless gluons have **infinite range**, we find that an **infinite amount of energy** would be associated with these **self-interacting** long-range fields.
- The solution is to **assume** that any **physical particle** must be **colorless**: there can be no long-range gluons.

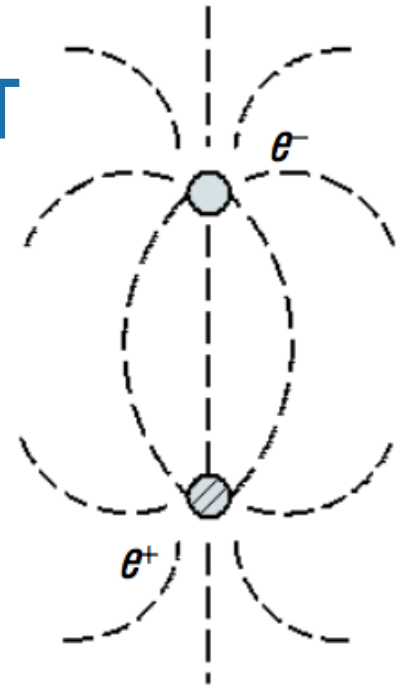
# QUARK CONFINEMENT

- Confinement also applies to quarks. All bound states of quarks must have a color combination such that they are white, or colorless.
- Protons, neutrons, and other baryons are bound states of three quarks of different color.
- The mesons are composed of a quark-antiquark pair with opposite colors (red and anti-red, etc...)
- As a consequence of confinement, one cannot remove just one quark from a proton, as that would create two “color-full” systems.
  - We would need an infinite amount of energy to effect such separation!
- Hence, the quarks are confined to a small region ( $<1$  fm) near one another.

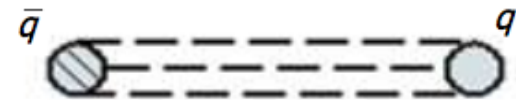


# UNDERSTANDING CONFINEMENT

- The **mathematics** of confinement are **complicated**, but we can **understand** them in terms of a very simple picture.
- Recall, the **Coulomb** field between a  $e^+e^-$  pair looks like  $V(r) \sim 1/r$ .
  - As we **pull** the pair **apart**, the **attraction weakens**.
- Imagine the **color field** between a quark-antiquark pair like Hooke's Law:  $V(r) \sim r$ .
  - As we **pull** the pair **apart**, the **attraction** between them **increases**.
- So, **separating** two quarks by a **large  $r$**  puts a **large amount of energy** into the color field:  
 $V(r) \rightarrow \infty$



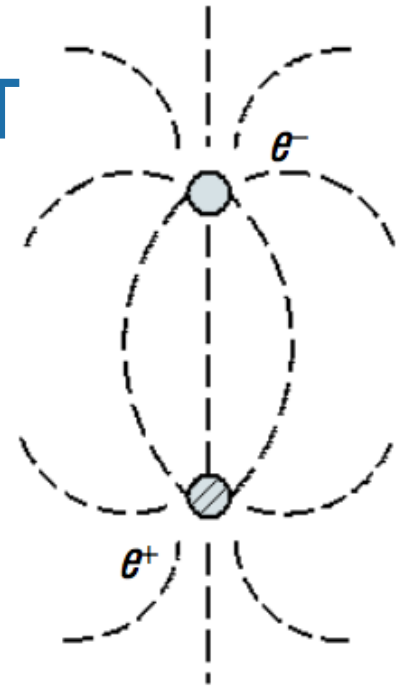
Dipole field for the Coulomb force between opposite electrical charges.



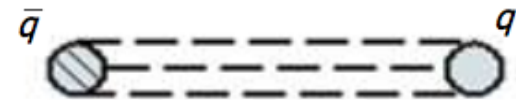
Dipole field between opposite-color quarks.

# UNDERSTANDING CONFINEMENT

- How do we **understand** this picture?
- When a quark and anti-quark **separate**, their color interaction **strengthens** (more gluons appear in the color field).
- Through the interaction of the **gluons with each other**, the color lines of force are **squeezed** into a tube-like region.
- **Contrast** this with the **Coulomb field**: nothing prevents the lines of force from **spreading out**.
  - There is **no self-coupling** of photons to contain them.
- If the color tube has **constant energy density** per unit length  $k$ , the **potential energy** between quark and antiquark will **increase** with separation,  $V(r) \sim kr$ .



Dipole field for the Coulomb force between opposite electrical charges.

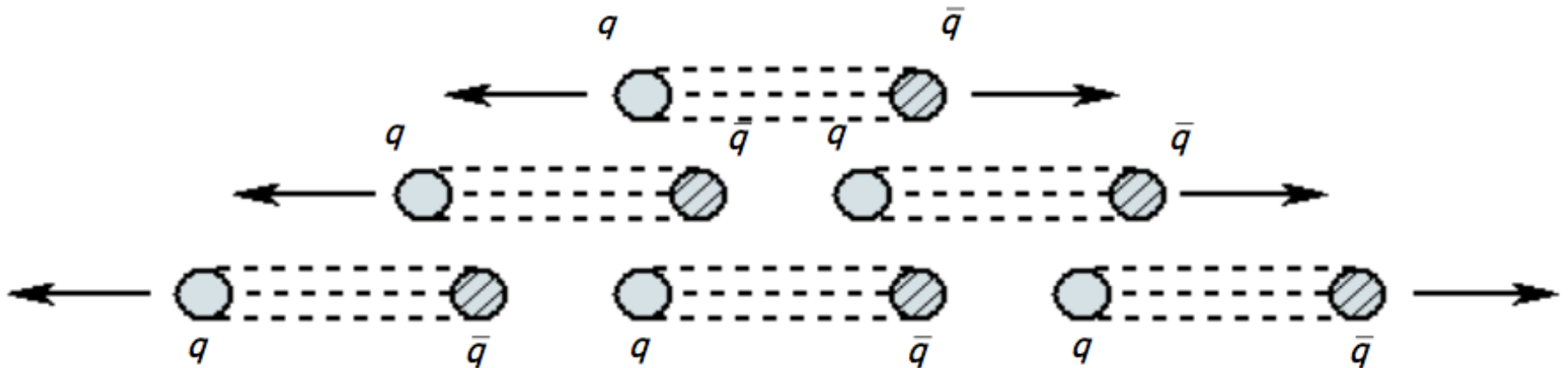


Dipole field between opposite-color quarks.

# COLOR LINES AND HADRON PRODUCTION

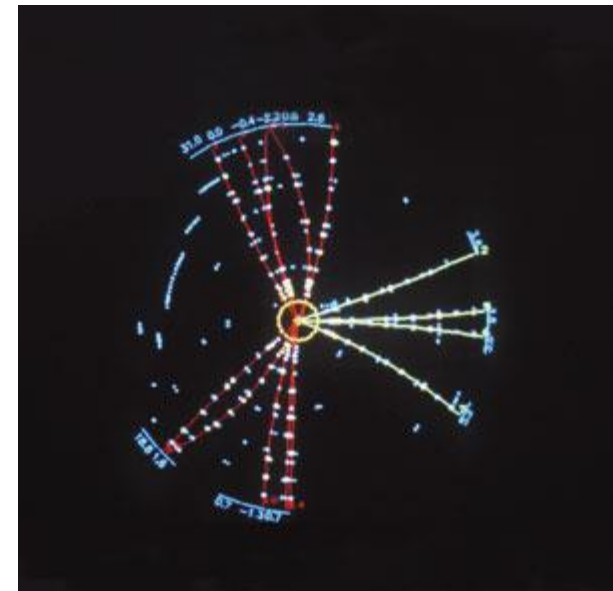
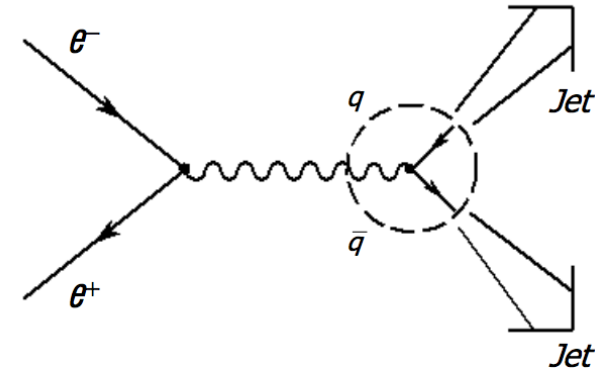
## WHY YOU CAN'T GET FREE QUARKS

- Suppose we have a meson and we try to pull it apart. The potential energy in the quark-antiquark color field starts to increase.
- Eventually, the energy in the gluon field gets big enough that the gluons can pair-produce another quark-antiquark pair.
  - The new quarks pair up with the original quarks to form mesons, and thus our four quarks remain confined in colorless states.
- Experimentally, we see two particles!



# HADRONIC JETS

- The process just described is **observed** experimentally in the form of **hadron jets**.
- In a collider experiment, two particles can annihilate and **form** a **quark-antiquark pair**.
- As the **quarks** move **apart**, the color lines of force are stretched until the potential **energy** can **create** another quark-antiquark **pair**.
- This process **continues** until the quarks' kinetic **energy** is **low** enough that **clusters** of **colorless** particles form.
- The experimentalist then **detects** several “**jets**” of **hadrons**, but **never sees** free **quarks** or **gluons**.



Jet formation at TASSO  
detector at PETRA

# ASYMPTOTIC FREEDOM

- As mentioned earlier, **perturbation** theory can only be applied when the **coupling constant**  $\alpha$  is **small**.
- At these lower energy regimes of jet formation,  $\alpha_s$  is of the **order of unity**, and that means we **can't ignore the many-vertex Feynman diagrams** as we do in **QED** (we can't treat QCD perturbatively!).
- However, as we already saw, the **coupling constant** is actually not a constant at all, and **depends** on the **energy** of the **interaction**.
- As the **energy increases**, the **coupling constant** becomes **smaller**.
- In fact, at **high enough energies**,  $\alpha_s$  gets so **small** that QCD can be dealt with as a **perturbative** theory (e.g. LHC high-energy collisions!)

# ASYMPTOTIC FREEDOM

- Asymptotic freedom: as the **energy** of interactions **goes up**, **QCD asymptotically approaches** a regime in which quarks act like **free** particles.
  - Looking at quarks with **a very high energy probe**.
- D. Gross, H. Politzer, F. Wilczek (1970's): **asymptotic freedom** suggests that QCD can be a **valid theory** of the strong force.



**The Nobel Prize in Physics 2004**

David J. Gross, H. David Politzer, Frank Wilczek



**David J. Gross**

Prize share: 1/3



**H. David Politzer**

Prize share: 1/3



**Frank Wilczek**

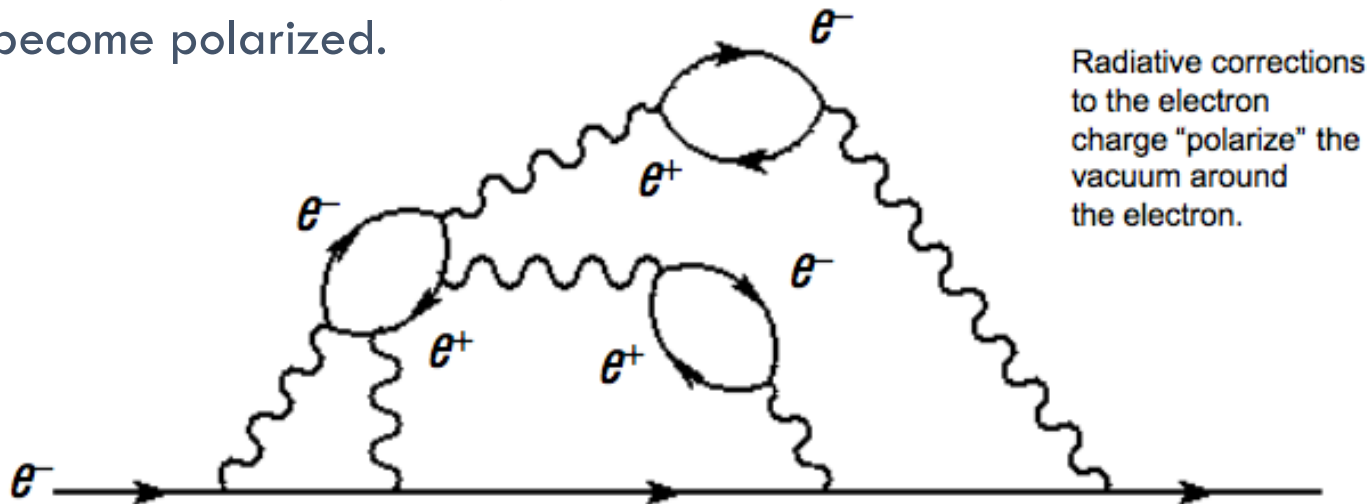
Prize share: 1/3

The Nobel Prize in Physics 2004 was awarded jointly to David J. Gross, H. David Politzer and Frank Wilczek "*for the discovery of asymptotic freedom in the theory of the strong interaction*".

# BACK TO QED

## POLARIZATION OF THE VACUUM

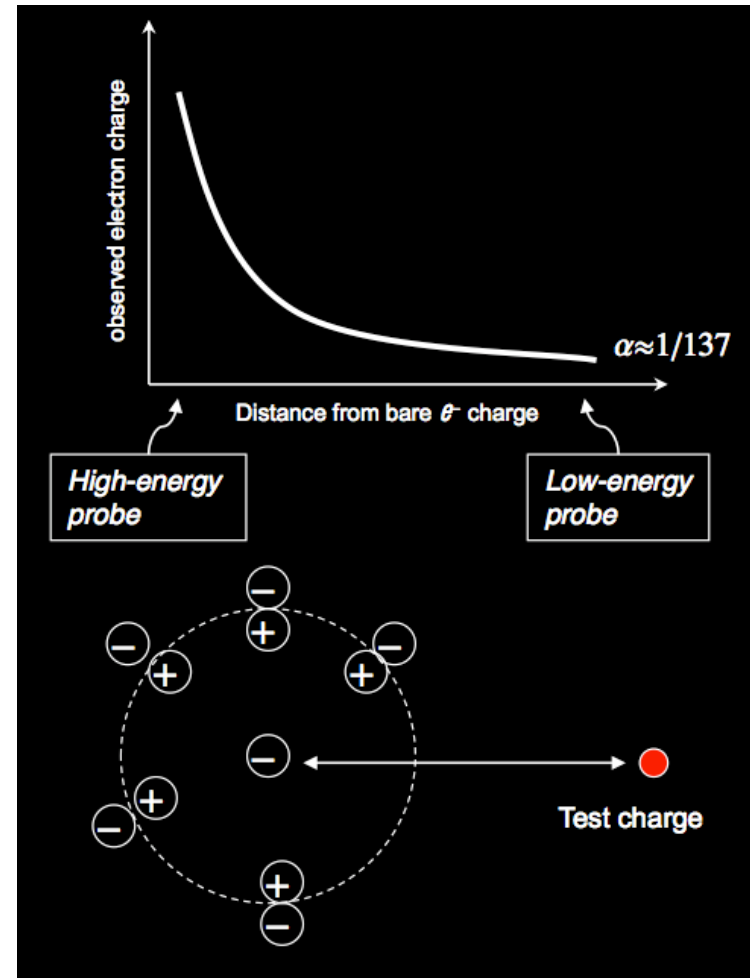
- The **vacuum** around a moving **electron** becomes **populated** with **virtual**  $e^+e^-$  pairs.
  - This is a purely **quantum effect**, and is allowed by Heisenberg's **Uncertainty Principle**.
- Because opposite charges attract, the virtual **positrons** in the  $e^+e^-$  loops will be **closer** to the electron.
- Therefore, the **vacuum** around the electron **becomes polarized** (a net electric dipole develops), just like a dielectric inside a capacitor can become polarized.





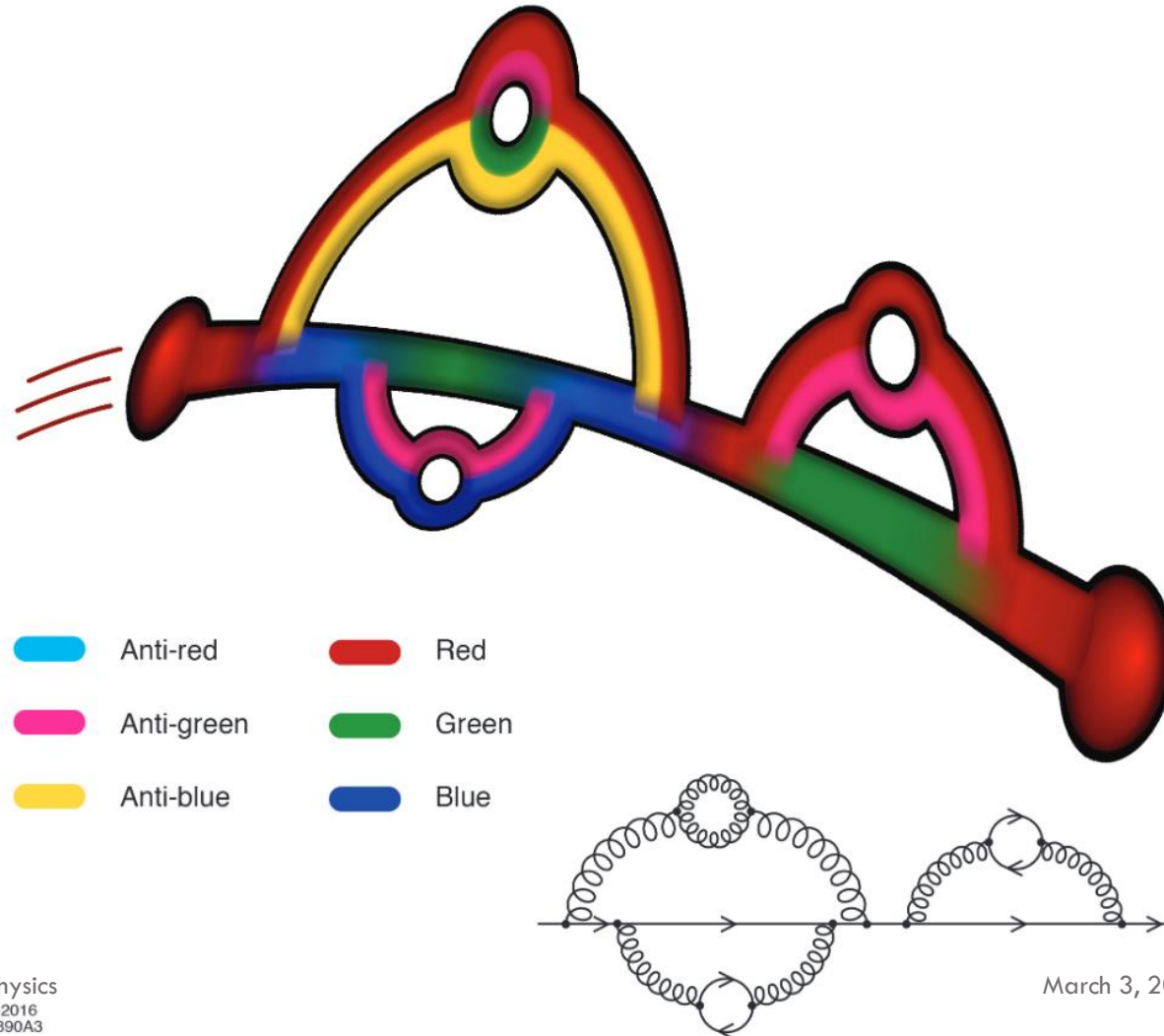
# QED: CHARGE SCREENING

- Now, suppose we want to **measure** the **charge** of the electron by observing the **Coulomb** force experienced by a **test charge**.
- Far away from the electron, its charge is **screened** by a cloud of **virtual positrons and electrons**, so the **effective** charge is **smaller** than its **bare** charge.
- As we move **closer** in, **fewer** positrons are blocking our line of sight to the electron.
- Hence, with **decreasing distance**, the **effective charge** of the electron **increases**.
- **We can think of this as  $\alpha$  increasing with energy.**



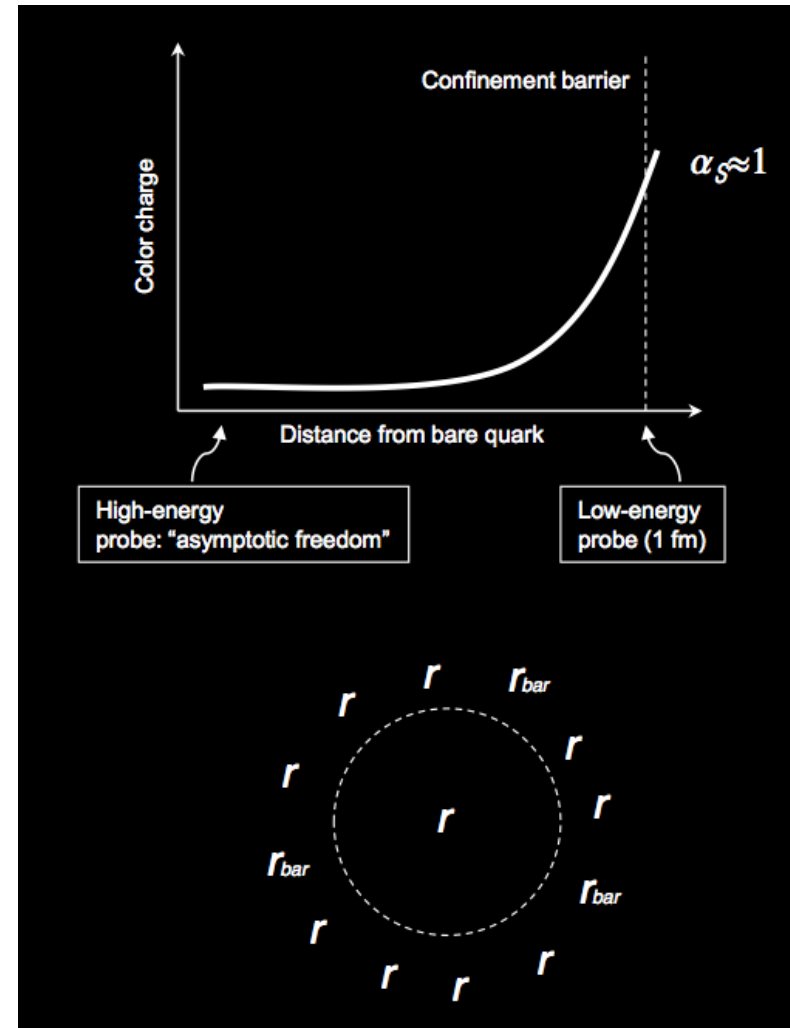
# QCD: CHARGE ANTI-SCREENING

- Gluons **carry color** charge and **self-interact**!
  - Screening in QCD is much more complicated...



# QCD: CHARGE ANTI-SCREENING

- In QCD, the additional gluon loop diagrams reverse the result of QED:
  - A red charge is preferentially surrounded by other red charges.
- By moving the test probe closer to the original quark, the probe penetrates a sphere of mostly red charge, and the measured red charge decreases.
- This is “antiscreening”.
- We can think of this as  $\alpha_s$  decreasing with energy.



# RUNNING CONSTANTS

- As we probe an **electron** at **increasingly higher** energies, its effective **charge increases**.
- This can be **rephrased** in the following way: as **interactions increase in energy**, the QED coupling strength  $\alpha$  between charges and photons **also increases**.
  - This should not really be a surprise; after all, the coupling strength of EM depends directly on the electron charge.
- Since  $\alpha$  is not a constant, but a (slowly-varying) function of energy, it is called a **running coupling constant**.
- In **QCD**, the net effect is that the quark color charge and  $\alpha_s$  **decrease** as the interaction **energy goes up**.

# UNDERLYING CAUSE

## SELF-INTERACTIONS OF THE MEDIATORS

- Gluon self-interaction!
- W and Z (weak force mediators) also self-interact.
  - Similar behavior.
  - The weak coupling constant also decreases as the energy scale goes up.

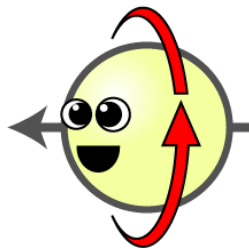
# PARTICLE HELICITY

## ASIDE

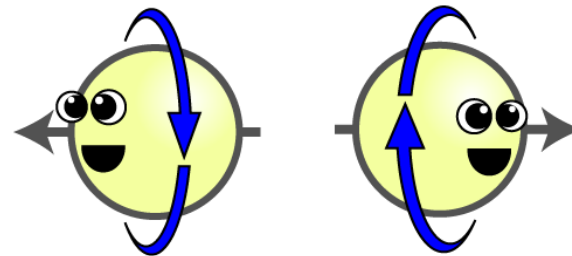
- Given that **angular momentum** is:
  - Conserved
  - Quantized
  - Constrained by yet another Heisenberg relation:
    - **Only one** of the x, y, z components of angular momentum can be measured with arbitrary precision

$$\Delta L_x \Delta L_y \geq \frac{\hbar}{2}$$

- Define **helicity** as the projection of the particle's angular momentum (e.g., spin) on its direction of travel

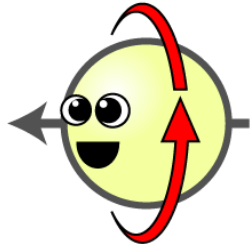


Right-handed:  
Spin in same direction as motion

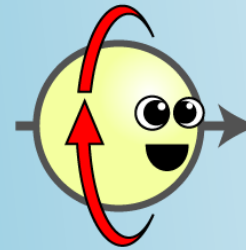


Left-handed:  
Spin in opposite direction to motion

# PARTICLE HELICITY ASIDE



Right-handed:  
Spin in same direction as motion



Left-handed!



MIRROR



- Helicity **flips** when looked at in a mirror
  - Equivalent to inverting one of the space coordinates ( $z \rightarrow -z$ )



# WEAK INTERACTIONS

- Unlike electromagnetism and the strong interaction, the weak interaction is mediated by massive bosons:
  - $m_Z = 91.19 \text{ GeV}$
  - $m_W = 80.39 \text{ GeV}$
- This makes it extremely short-range
- And very weak at low energies
- Only left-handed particles\* participate in weak interactions
  - Nature is different if looked at in a mirror!
  - \* and right-handed anti-particles

$$\Delta E \Delta t \geq \frac{\hbar}{2}$$



# WEAK INTERACTIONS

- Unlike electromagnetism and the strong interaction, the weak interaction is mediated by massive bosons:

- $m_Z = 91.19 \text{ GeV}$
- $m_W = 80.39 \text{ GeV}$

- This makes it e

Neutrinos **only** interact via the weak force: are there **right-handed** neutrinos at all?!

$$\geq \frac{\hbar}{2}$$

- And very weak

- Only left-handed particles\* participate in weak interactions

- Nature is different if looked at in a mirror!
- \* and right-handed anti-particles

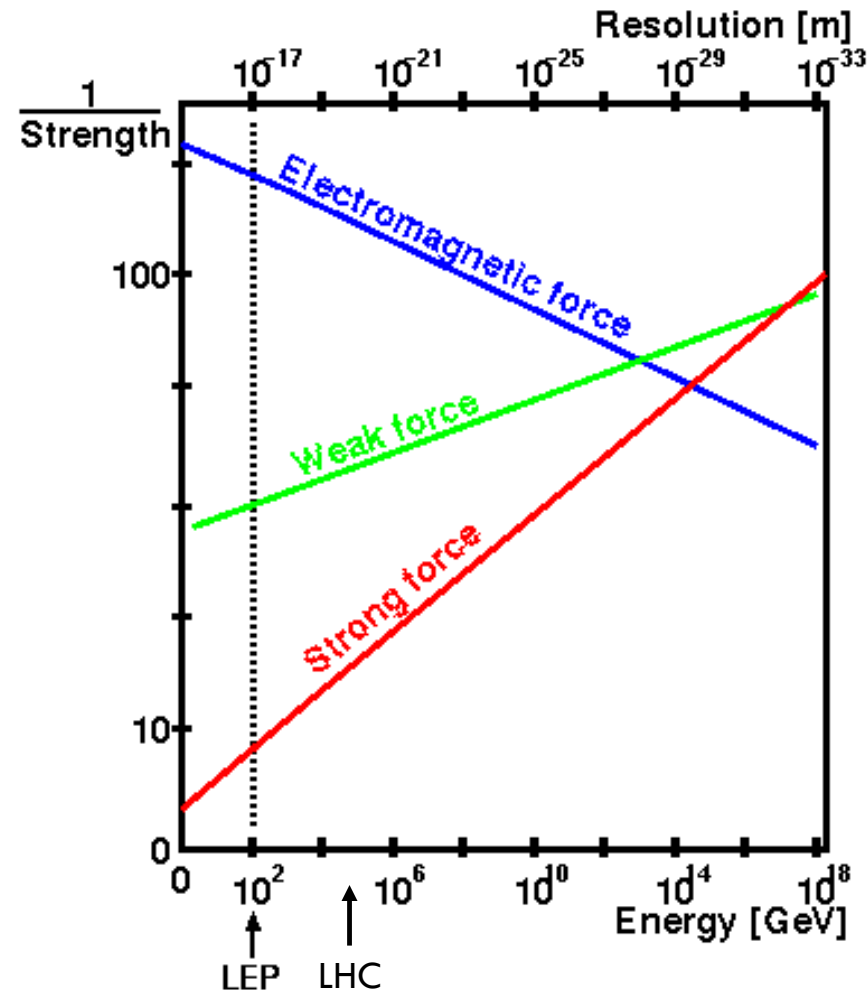


# WEAK INTERACTIONS

- At **low energies**, the effective weak coupling strength is 1000 times **smaller** than the electromagnetic force.
- As interaction energies start to approach the **mass-energy** of the **W** and **Z** particles ( $\sim 100$  GeV), the effective coupling rapidly approaches the **intrinsic strength** of the weak interaction  $\alpha_W$ .
  - At these energies, the **weak** interaction actually **dominates** over **electromagnetism**.
- **Beyond** that, the effective weak coupling starts to **decrease**.

# FORCE UNIFICATION ASIDE

- At laboratory energies near  $M_W$  ( $\sim 100$ ) GeV, the measured values of the coupling constants are quite different.
- However, their “running” trends suggest that they approach a common value near  $10^{16}$  GeV.
- This is an insanely high energy!
- The Standard Model provides no explanation for what may happen beyond this unification scale, nor why the forces have such different strengths at low energies.



# PARTICLE/FIELD FORMULATION

# PARTICLE/FIELD FORMULATION

- In particle physics, we define **fields** like  $\varphi(x,t)$  at every point in spacetime.
- These fields don't just sit there; they **fluctuate** about some minimum energy state.
- The oscillations combine to form **wavepackets**.
- The **wavepackets** move around in the field and interact with each other. We interpret them as elementary particles.
- Terminology: the **wavepackets** are called the **quanta** of the field  $\varphi(x,t)$ .

# PARTICLE/FIELD FORMULATION

- How do we **describe** interactions and fields **mathematically**?
- Classically,

**Lagrangian  $L$**  = kinetic energy - potential energy

- Particle physics:
  - Same concept, using Dirac equation to describe free spin-1/2 particles:

$$L = \bar{\Psi}(i\gamma^\mu\partial_\mu - m)\Psi$$

↑  
Field

$\Psi$  = wavefunction

$m$  = mass

$\gamma^\mu$  =  $\mu^{\text{th}}$  gamma matrix

$\partial_\mu$  = partial derivative



# LAGRANGIAN MECHANICS

- Developed by Euler, Lagrange, and others during the mid-1700's.
- This is an energy-based theory that is equivalent to Newtonian mechanics (a force-based theory, if you like).

$$\frac{\partial \mathcal{L}}{\partial x_i} - \frac{d}{dt} \left( \frac{\partial \mathcal{L}}{\partial \dot{x}_i} \right)$$

- **Lagrangian:** quantity that allows us to infer the dynamics of a system.

# STANDARD MODEL LAGRANGIAN

Free Fields

Interaction

$$\mathcal{L} = \mathcal{L}_0 + \mathcal{L}'$$

# STANDARD MODEL LAGRANGIAN

$$\mathcal{L} = \mathcal{L}_0 + \mathcal{L}'$$

Free Fields

Interaction

$$\mathcal{L}_0 = -\frac{1}{4}F_{\mu\nu}F^{\mu\nu} + i\bar{\psi}\gamma^\mu\partial_\mu\psi$$

Gauge Bosons

Fermions

$$F_{\mu\nu}F^{\mu\nu} = G_{\mu\nu}G^{\mu\nu} + W_{\mu\nu}W^{\mu\nu} + B_{\mu\nu}B^{\mu\nu}$$

# STANDARD MODEL LAGRANGIAN

$$\mathcal{L} = \mathcal{L}_0 + \mathcal{L}'$$

Free Fields
Interaction

$$\mathcal{L}_0 = -\frac{1}{4}F_{\mu\nu}F^{\mu\nu} + i\bar{\psi}\gamma^\mu\partial_\mu\psi$$

Gauge Bosons
Fermions

$$\mathcal{L}' = e\bar{\psi}\gamma^\mu A_\mu\psi$$

Fermion-Boson  
Coupling

$$eA_\mu = \frac{g_s}{2}\lambda_\nu G_\mu^\nu + \frac{g}{2}\vec{\tau} \cdot \vec{W}_\mu + \frac{g'}{2}YB_\mu$$

$$F_{\mu\nu}F^{\mu\nu} = G_{\mu\nu}G^{\mu\nu} + W_{\mu\nu}W^{\mu\nu} + B_{\mu\nu}B^{\mu\nu}$$

# STANDARD MODEL LAGRANGIAN

Free Fields

Interaction

$$\mathcal{L} = \mathcal{L}_0 + \mathcal{L}'$$

Gauge Bosons

$$\mathcal{L}_0 = -\frac{1}{4}F_{\mu\nu}F^{\mu\nu} + i\bar{\psi}\gamma^\mu\partial_\mu\psi$$

Electroweak bosons and interaction

Fermions

$$\mathcal{L}' = e\bar{\psi}\gamma^\mu A_\mu\psi$$

Gluons and strong interaction

Fermion-Boson Coupling

$$eA_\mu = \frac{g_s}{2}\lambda_\nu G_\mu^\nu + \frac{g}{2}\vec{\tau} \cdot \vec{W}_\mu + \frac{g'}{2}Y B_\mu$$

$$F_{\mu\nu}F^{\mu\nu} = G_{\mu\nu}G^{\mu\nu} + W_{\mu\nu}W^{\mu\nu} + B_{\mu\nu}B^{\mu\nu}$$

# SYMMETRIES AND INVARIANCE

- Noether's theorem (1915):
  - Every **symmetry** under some operation corresponds to a **conservation law**

<b>symmetry</b>	<b>invariant</b>
Space translation	momentum
Time translation	energy
Rotation	Angular momentum
Global phase; $\Psi \rightarrow e^{i\theta} \Psi$	Electric charge
Local phase; $\Psi \rightarrow e^{i\theta(x,t)} \Psi$	Lagrangian + gauge field ( $\rightarrow$ QED)



# SYMMETRIES AND INVARIANCE

- There are carefully chosen sets of transformations for  $\Psi$  which give rise to the observable gauge fields:
  - That is how we get electric, color, weak charge conservation!



# QED FROM LOCAL GAUGE INVARIANCE

- Apply **local** gauge symmetry to Dirac equation:

$$\bar{\Psi} \rightarrow e^{i\theta(x,t)} \bar{\Psi}, \quad \Psi \rightarrow e^{-i\theta(x,t)} \Psi$$

This type of transformation leaves quantum mechanical amplitudes invariant.

- Consider very small changes in a field:

$$\Psi \rightarrow \Psi + \delta\Psi = \Psi - i\theta(x,t)\Psi \quad \text{ie. } \delta\Psi = -i\theta(x,t)\Psi$$

- The effect on the Lagrangian is:

$$L = \bar{\Psi}(i\gamma^\mu \partial_\mu - m)\Psi \Rightarrow \delta L = \bar{\Psi} \gamma^\mu \partial_\mu \theta(x,t) \Psi$$



# QED FROM LOCAL GAUGE INVARIANCE

- Apply **local** gauge symmetry to Dirac equation:

$$\bar{\Psi} \rightarrow e^{i\theta(x,t)} \bar{\Psi}, \quad \Psi \rightarrow e^{-i\theta(x,t)} \Psi$$

This type of transformation leaves quantum mechanical amplitudes invariant.

- Consider very small changes in a field:

$$\Psi \rightarrow \Psi + \delta\Psi = \Psi - i\theta(x,t)\Psi \quad \text{ie. } \delta\Psi = -i\theta(x,t)\Psi$$

- The effect on the Lagrangian is:

$$L = \bar{\Psi}(i\gamma^\mu \partial_\mu - m)\Psi \Rightarrow \delta L = \bar{\Psi} \gamma^\mu \partial_\mu \theta(x,t) \Psi$$

For the Lagrangian to remain invariant:  $\delta L = 0$

# QED FROM LOCAL GAUGE INVARIANCE

- To satisfy  $\delta L=0$ , we “engineer” a mathematical “trick”:

1. Introduce a gauge field  $A_\mu$  to interact with fermions,  
and  $A_\mu$  transform as:  $A_\mu + \delta A_\mu = A_\mu + 1/e \partial_\mu \theta(x,t)$
2. In resulting Lagrangian, replace  $\partial_\mu \rightarrow D_\mu = \partial_\mu + ieA_\mu$

- In that case,  $L$  is redefined:

$$L = \bar{\Psi}(i\gamma^\mu D_\mu - m)\Psi$$

The new Lagrangian is invariant under local gauge transformations.

# QED FROM LOCAL GAUGE INVARIANCE

## ONE MORE THING...

- Need to add kinetic term for field (field strength):

Define  $F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu$

Add term  $-\frac{1}{4}F_{\mu\nu}F^{\mu\nu}$  (Lorentz invariant, matches  
Maxwell's equations)

# QED FROM LOCAL GAUGE INVARIANCE

## ONE MORE THING...

- Need to add kinetic term for field (field strength):

Define  $F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu$

Add term  $-1/4 F_{\mu\nu} F^{\mu\nu}$  (Lorentz invariant, **matches**  
**Maxwell's equations**)

**Final lagrangian (for QED!):**

$$\mathcal{L} = -1/4 F_{\mu\nu} F^{\mu\nu} + \bar{\Psi}(i\gamma^\mu D_\mu - m)\Psi$$

- **No mass** term is allowed for  $A_\mu$ , otherwise the Lagrangian is **not** gauge **invariant**
  - The gauge field is **massless**!

# QED FROM LOCAL GAUGE INVARIANCE

## ONE MORE THING...

- Need to add kinetic term for field (field strength):

Define  $F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu$

Add term  $-\frac{1}{4}F_{\mu\nu}F^{\mu\nu}$  (Lorentz invariant, **matches Maxwell's equations**)

**Final lagrangian (for QED!):**

$$\mathcal{L} = -\frac{1}{4}F_{\mu\nu}F^{\mu\nu} + \bar{\Psi}(i\gamma^\mu D_\mu - m)\Psi$$

- No mass term for photon → photon  
is not gauged → photon is massless
- The gauged fermion is a Dirac fermion

We have mathematically engineered a lagrangian for a quantum field that couples to fermions, obeys Maxwell's equations and is massless!

# QED FROM LOCAL GAUGE INVARIANCE

## ONE MORE THING...

- Need to add kinetic term for field (field strength):

Define  $F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu$

Add term  $-1/4 F_{\mu\nu} F^{\mu\nu}$  (Lorentz invariant, **matches Maxwell's equations**)

**Final lagrangian (for QED!):**

$$\mathcal{L} = -1/4 F_{\mu\nu} F^{\mu\nu} + \bar{\Psi}(i\gamma^\mu D_\mu - m)\Psi$$

- **No mass** Lagrangian
- is **not** gauge invariant
- The gauge boson is **The photon!**

# NEXT WEEK:

THE HIGGS MECHANISM

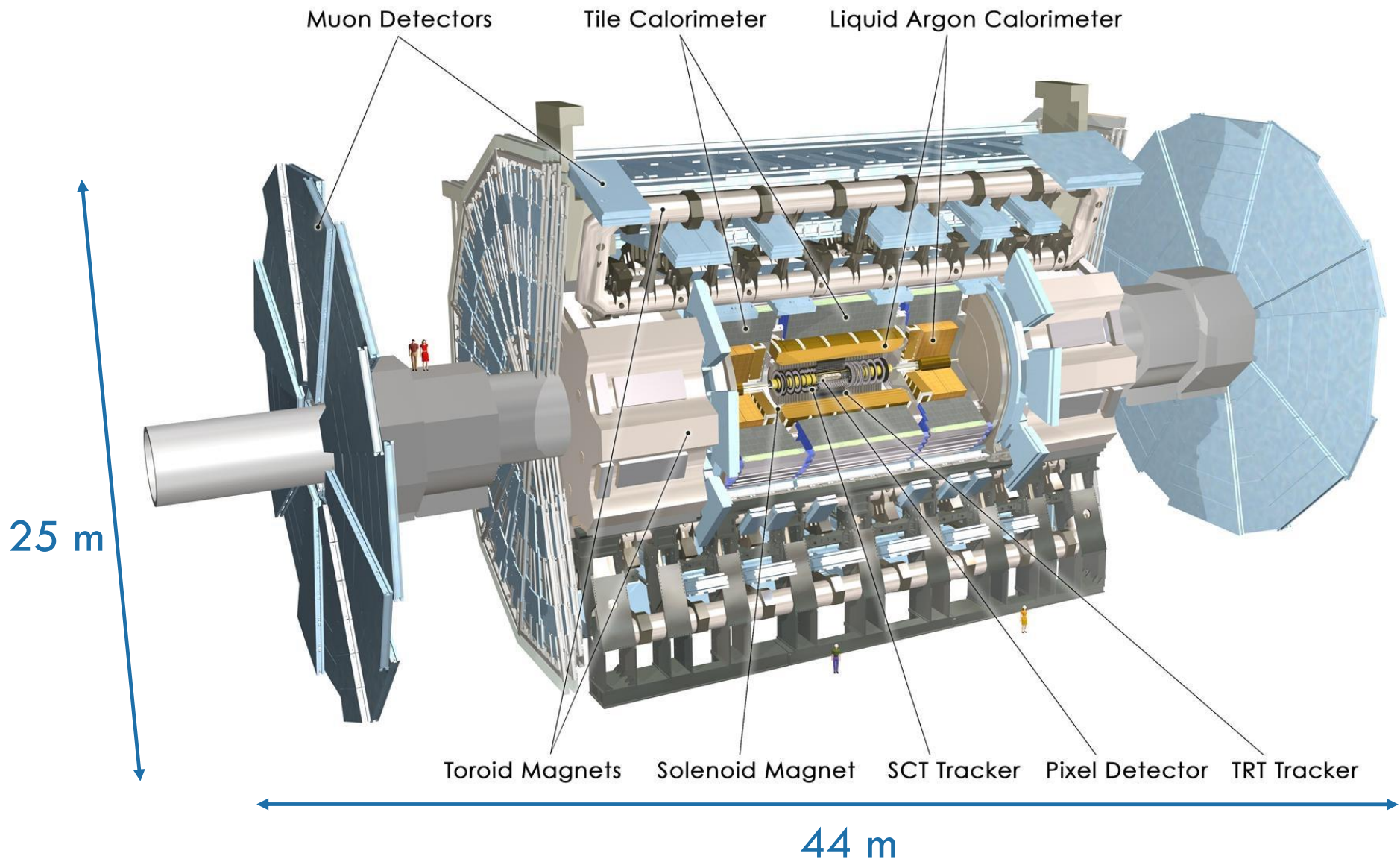
TESTS AND PREDICTIONS OF THE STANDARD MODEL

LIMITATIONS OF THE STANDARD MODEL

BONUS



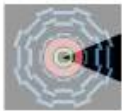
# THE ATLAS DETECTOR



# A SLICE OF ATLAS

## ATLAS

animation



☐ display instantly

Energy [GeV]:

1 5 10 15 25



Electron



Proton



Neutrino



Photon



Positron



Anti-proton



Jets



Muon

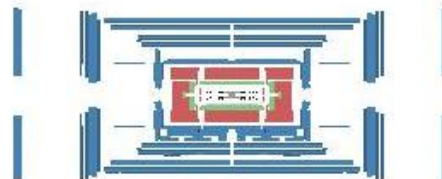
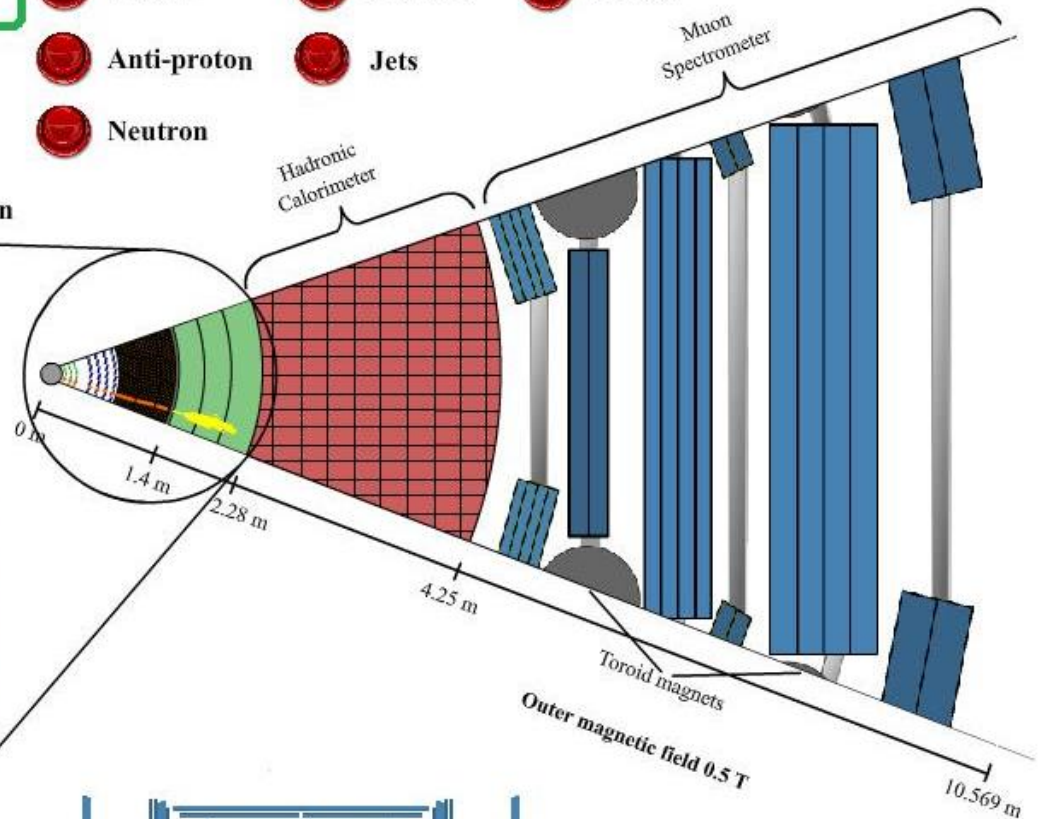
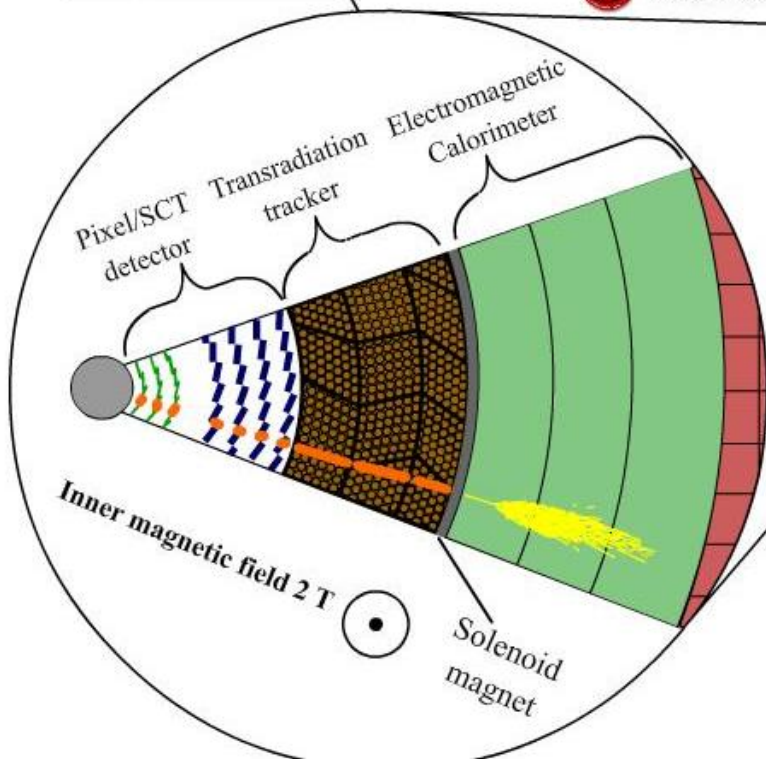


Neutron



Anti-muon

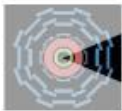
Magnification 3x



# A SLICE OF ATLAS

## ATLAS

animation



☐ display instantly



Electron



Proton



Neutrino



Photon



Positron



Anti-proton



Jets



Muon

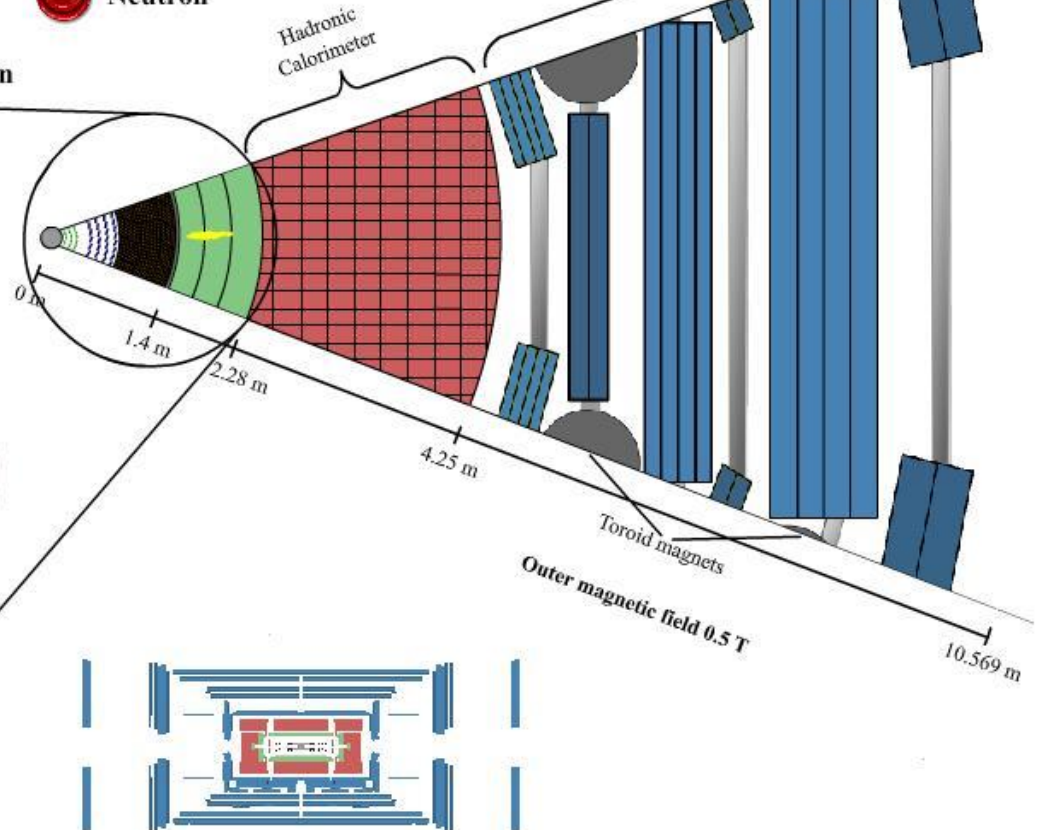
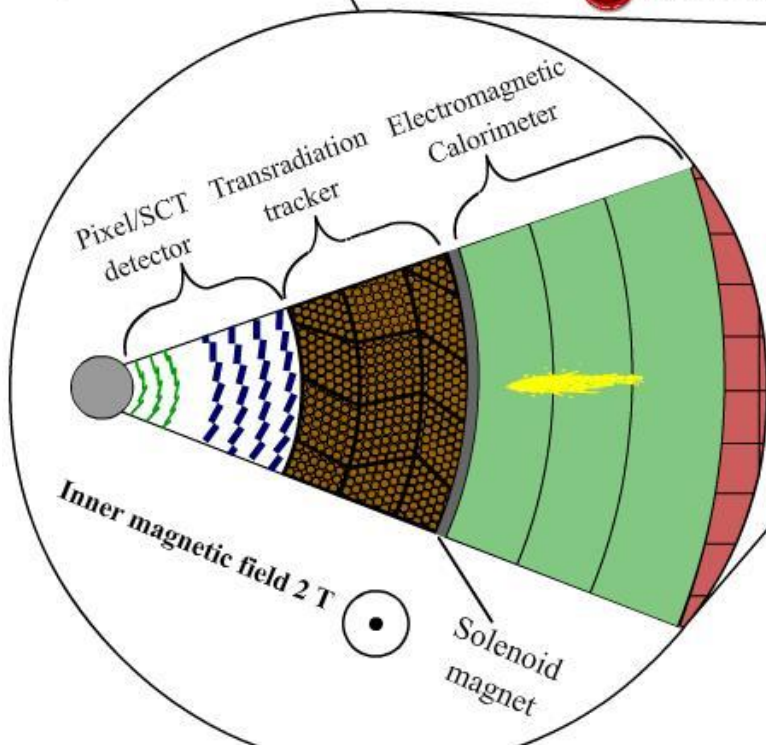


Neutron



Anti-muon

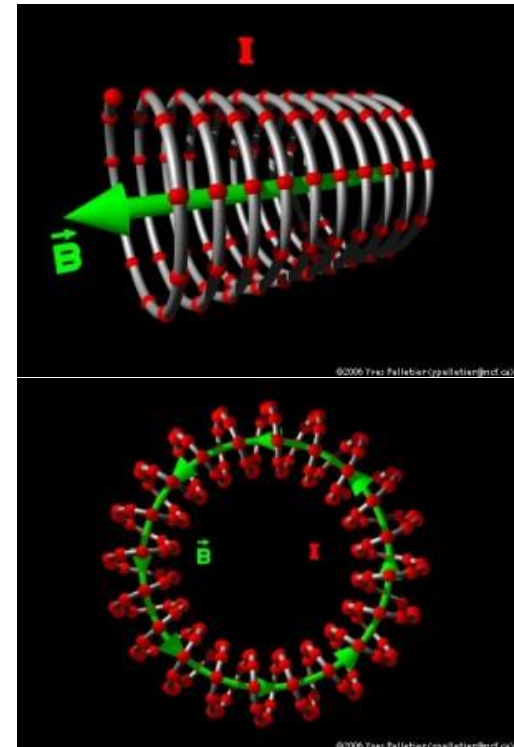
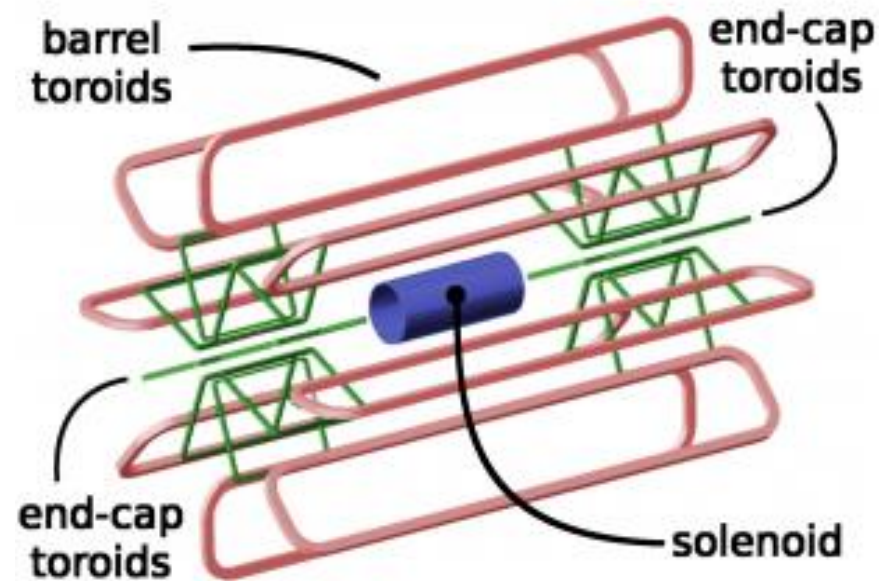
Magnification 3x



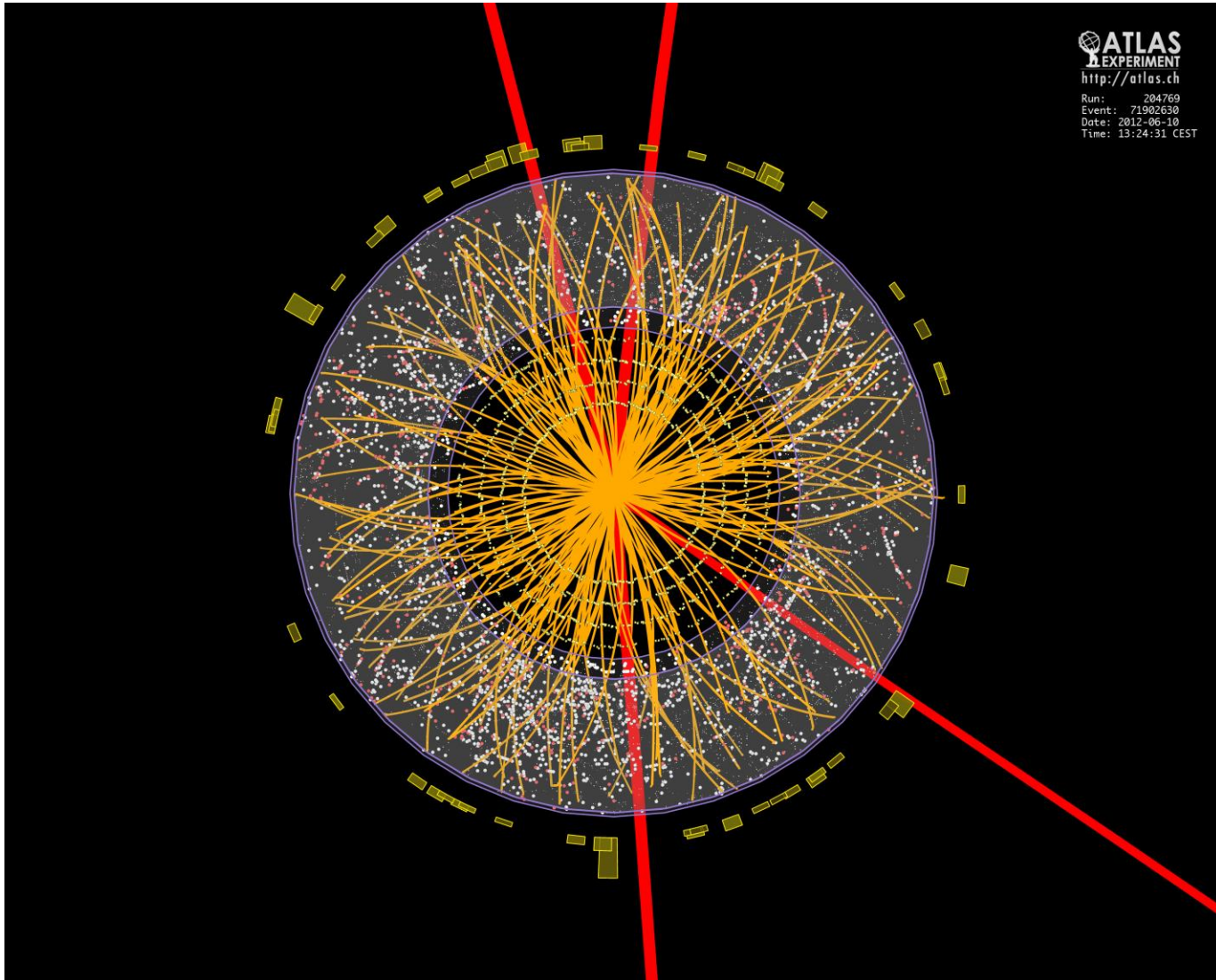


# MAGNET SYSTEMS

- Solenoid and toroidal magnets.
- Solenoid coils in CMS and ATLAS:
  - Field direction along beam axis.
  - Homogenous field inside the coil.
  - e.g. CMS superconducting magnet
    - $I = 20 \text{ kA}$ ,  $B = 4 \text{ T}$
    - Temperature  $4\text{K}$ .
- For comparison, Earth's magnetic field at surface is  $\sim 50 \mu\text{T}$ .



# A REAL EVENT



# STANDARD MODEL LAGRANGIAN

- Encompasses **all** theory.
  - From the Lagrangian to **cross-section predictions**:

$$\sigma \sim \langle f | \mathbf{S} | i \rangle^2$$

Inelastic  
**Cross Section**  
[for  $|i\rangle \neq |f\rangle$ ]

[Def. :  $|t = +\infty\rangle \equiv \mathbf{S}|t = -\infty\rangle$ ]

## Time Evolution

From Schrödinger-Equation  
[Dirac picture]

$$|t\rangle = |t_0\rangle - i \int_{t_0}^t dt' \mathbf{H}'(t') |t'\rangle$$

$$\mathbf{H}'(t) = - \int \mathcal{L}'(x, t) d^3x$$

Lagrangian  
of Interaction

$$\langle f | \mathbf{S} | i \rangle \cong \delta_{fi} - i \int_{-\infty}^{\infty} dt' \langle f | \mathbf{H}'(t') | i \rangle$$

→ Feynman rules

# INTEGRAL OVER “ALL POSSIBLE PATHS”

- Where does the integral notion come from?
- Recall, QM picture of free particle motion: there is some amplitude for a free electron to travel along any path from the source to some point  $p$ . Not just the straight, classical trajectory!
  - The word “path” here doesn’t only refer to a  $x(y)$  path in space, but also the time at which it passes each point in space.
  - In 3D, a path (sometimes called worldline) is defined by three functions  $x(t)$ ,  $y(t)$  and  $z(t)$ . An electron has an amplitude associated with a given path.
- The total amplitude for the electron to arrive at some final point is the sum of the amplitudes of all possible paths. Since there are an infinite number of paths, the sum turns into an integral.

# THE QUANTUM MECHANICAL AMPLITUDE

- *Feynman: Each path has a corresponding probability amplitude. The amplitude  $\psi$  for a system to travel along a given path  $x(t)$  is:*

$$\psi[x(t)] = \text{const.} \cdot e^{iS[x(t)]/\hbar}$$

where the object  $S[x(t)]$  is called the **action** corresponding to  $x(t)$ .

- The total amplitude is the sum of contributions from each path:

$$\sum_{\text{over all paths}} \psi[x(t)]$$



# THE QUANTUM MECHANICAL AMPLITUDE

$$\psi[x(t)] = \text{const.} \cdot e^{iS[x(t)]/\hbar}$$

1. What is  $e^{iS[x(t)]/\hbar}$ ?
2. What is the action  $S[x(t)]$ ?

# UNDERSTANDING THE PHASE

- You may not have seen numbers like  $e^{i\theta}$ , so let's review.
- Basically,  $e^{i\theta}$  is just a fancy way of writing sinusoidal functions; from Euler's famous formula:

$$e^{i\theta} = \cos \theta + i \sin \theta$$

- Note: those of you familiar with complex numbers (of the form  $z=x+iy$ ) know that  $e^{i\theta}$  is the phase of the so-called polar form of  $z$ , in which  $z=re^{i\theta}$ , with:

$$r = \sqrt{x^2 + y^2}$$

$$\theta = \tan^{-1}\left(\frac{y}{x}\right)$$

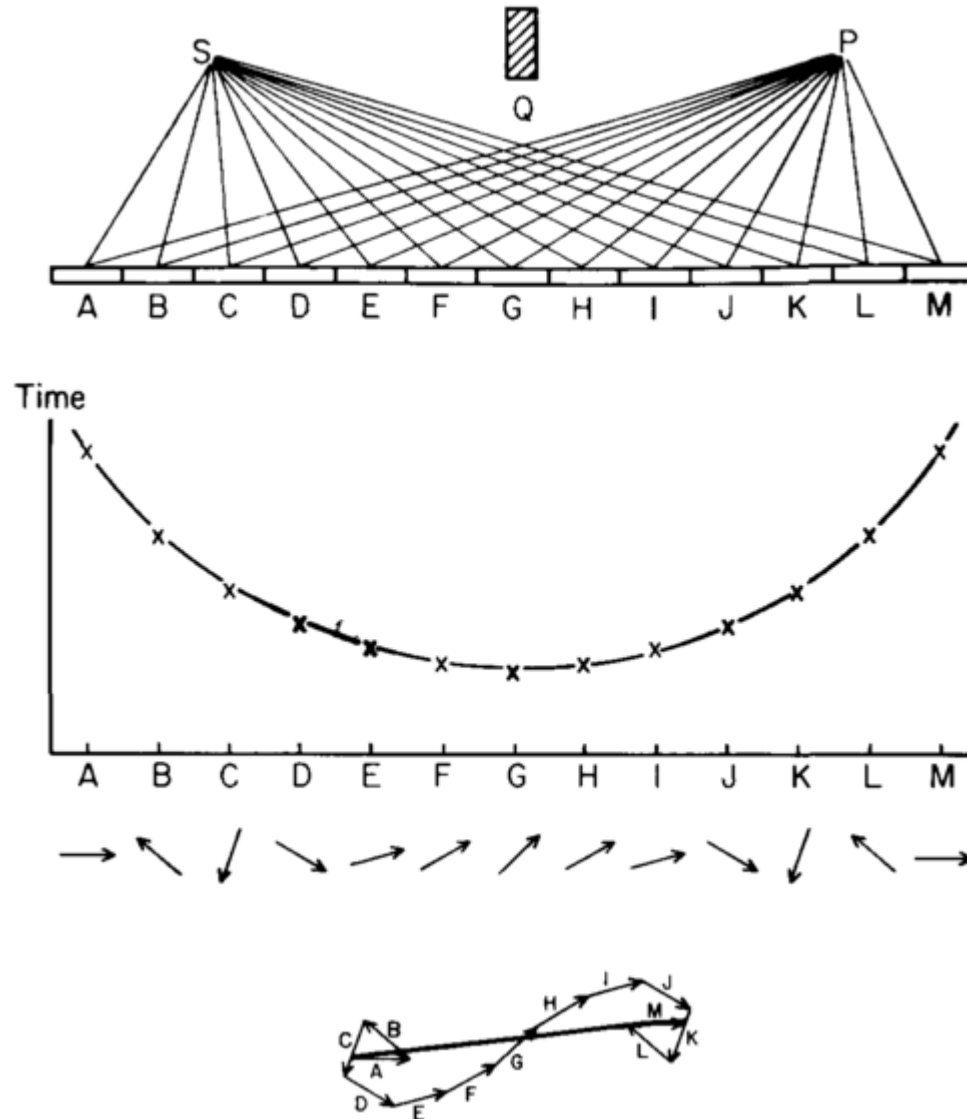
# COMMENTS ON THE AMPLITUDE

- Now we can understand the probability amplitude  $\psi[x(t)] \sim e^{iS[x(t)]/\hbar}$  a little better.
- The amplitude is a sinusoidal function – a wave – that oscillates along the worldline  $x(t)$ . The frequency of oscillation is determined by how rapidly the action  $S$  changes along the path.
- The probability that a particle will take a given path (up to some overall multiplication constant) is:

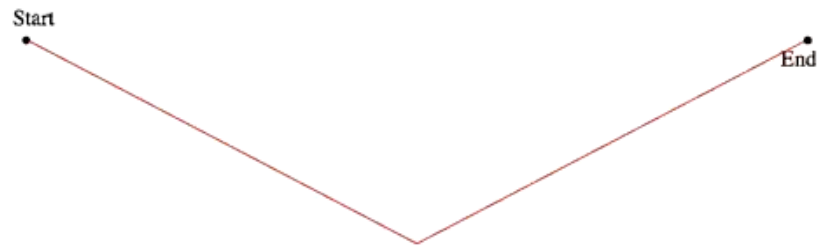
$$\begin{aligned} P &\propto |\psi|^2 = \psi^* \psi \\ &\propto e^{-iS[x(t)]/\hbar} e^{iS[x(t)]/\hbar} \\ &= e^{iS[x(t)]/\hbar - iS[x(t)]/\hbar} = e^0 \\ &= 1 \end{aligned}$$

- This is the same for every worldline. According to Feynman, the particle is equally likely to take any path through space and time!
  - Contributions from “crazy” paths will likely be suppressed by interference!

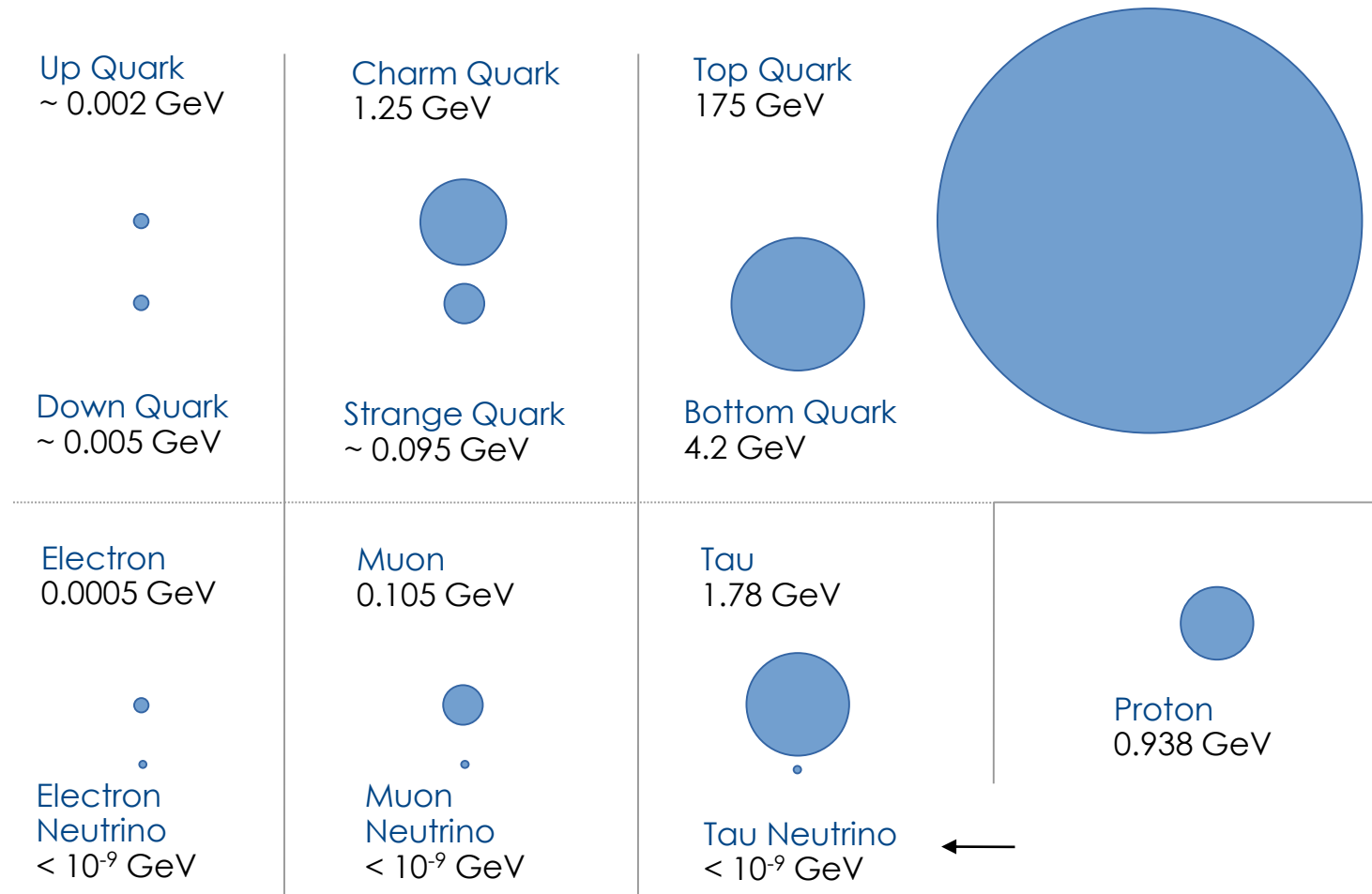
# COMMENTS ON THE AMPLITUDE



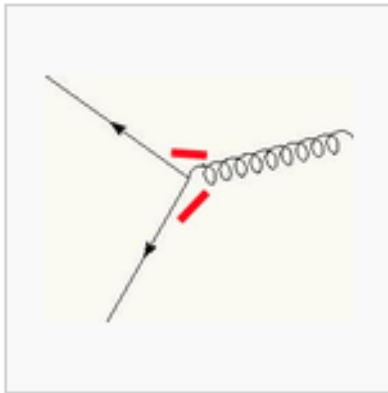
# COMMENTS ON THE AMPLITUDE



# MASSES OF SM FERMIONS



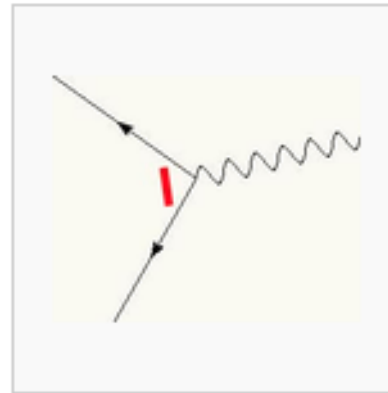
# GLUON DISCOVERY AT TASSO, PETRA



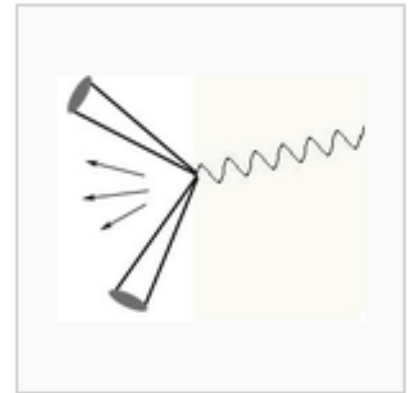
Two **quarks** (solid lines) and a **gluon** (curly line) fly apart, with the **strings** (red bars) primarily between the gluon and each quark.



As a result, three **jets** (cones) form, with extra **hadrons** (arrows) found where the strings formed.



For comparison, physicists looked at events with two quarks and a **photon** (wavy line). Here the string forms only between quarks.



Therefore extra hadrons are found only between the two jets, which is inconsistent with observations.