

Particle Physics: Neutrinos – part I

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Week 8: March 25, 2017
Columbia University Science Honors Program



Course Policies

Attendance

Up to four absences

Send email notifications of all absences to
shpattendance@columbia.edu.

Please, no cell phones

Please, ask questions!

Lecture materials

<https://twiki.nevis.columbia.edu/twiki/bin/view/Main/ScienceHonorsProgram>

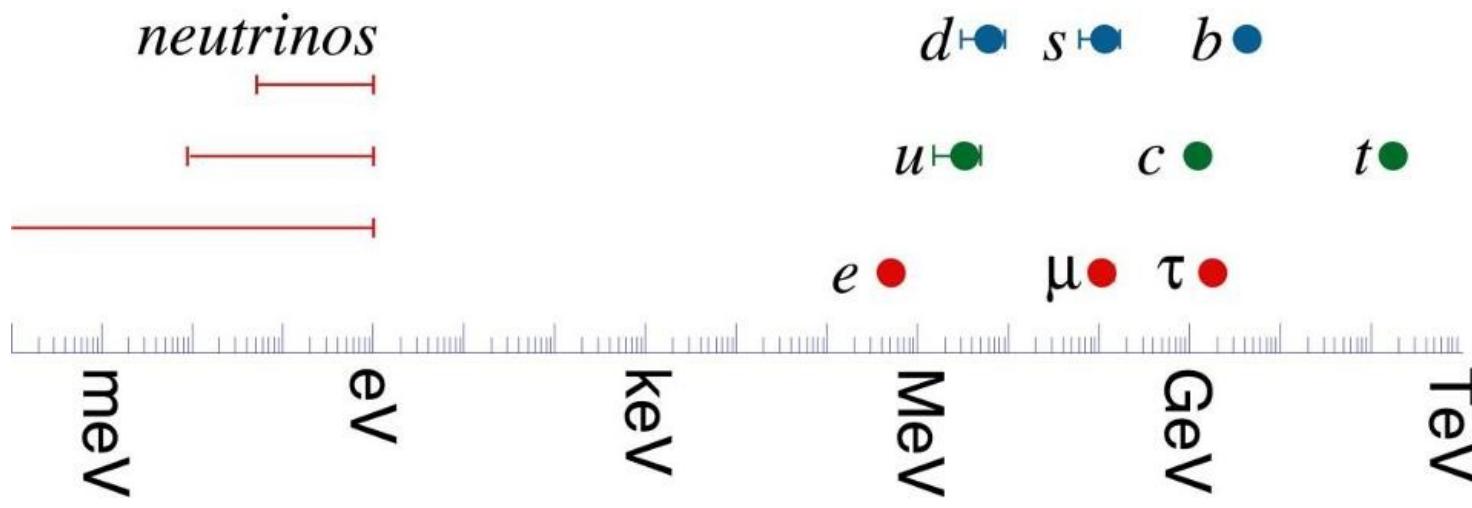
Schedule

1. ~~Introduction~~ (Inês)
2. ~~History of Particle Physics~~ (José)
3. ~~Special Relativity~~ (José)
4. ~~Quantum Mechanics~~ (Inês)
5. ~~Experimental Methods~~ (Cris)
6. ~~The Standard Model – Overview~~ (Cris)
7. ~~The Standard Model – Limitations~~ (Cris)
- 8. Neutrinos – part I (José)**
- 9. Neutrinos – part II (José)**
10. LHC and Experiments (Inês)
11. The Higgs Boson and Beyond (Inês)
12. Particle Cosmology (Cris)

Neutrinos in the Standard Model

Three Generations of Matter (Fermions) spin $\frac{1}{2}$								
	I	II	III					
mass →	2.4 MeV	1.27 GeV	171.2 GeV					
charge →	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$					
name →	u	c	t	top	Right			
Quarks	Left	Left	Left	charm	Right			
	up							
	Right							
	Left	Left	Left	top	Right			
	d	s	b	bottom	Right			
	Left	Left	Left	Right				
	down	strange	bottom					
	Right	Right	Right					
Leptons								
	0 eV	0 eV	0 eV					
	ν_e	ν_μ	ν_τ					
	Left	Left	Left	tau neutrino	Right			
	electron neutrino	muon neutrino	tau neutrino					
	Left	Left	Left	Right				
	electron	muon	tau					
	Right	Right	Right					

- Only left-handed neutrinos (and right-handed antineutrinos) in the Standard Model.
- Initially implemented as massless particles.
 - Neutrino oscillations** show neutrinos have mass!
- Why neutrino masses are so different from the other fermions?
 - Are neutrinos acquiring mass through the same mechanism (Higgs) or from something else?



Neutrino oscillations (2-neutrino example)

- Consequence of neutrino mixing (quantum superposition, as in Schrödinger's cat): the neutrinos that interact are not the same as the neutrinos that propagate.
- Two flavor approximation:

Flavor eigenstates

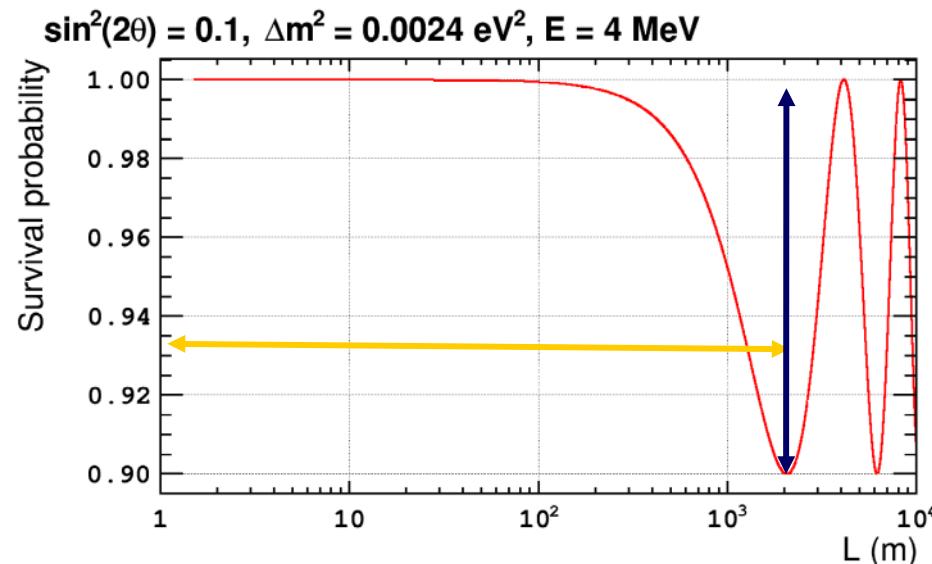
$$\begin{pmatrix} |\nu_l\rangle \\ |\nu_x\rangle \end{pmatrix} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} |\nu_1\rangle \\ |\nu_2\rangle \end{pmatrix}$$

Mass eigenstates

- Transition probability (derivation in blackboard):

$$P_{lx(l \neq x)}^{2\nu}(L, E) = \boxed{\sin^2(2\theta)} \sin^2 \left(\boxed{\frac{\Delta m^2 L}{4E}} \right)$$

Controlled by the experiment



- Survival probability:

$$P_{ll}^{2\nu}(L, E) = 1 - P_{lx(l \neq x)}^{2\nu}(L, E)$$

- Neutrino oscillation implies neutrinos are massive and non-degenerated.

3 neutrino mixing

- **Flavor eigenstates** (ν_e , ν_μ , ν_τ) \neq **mass eigenstates** (ν_1 , ν_2 , ν_3).
- Related by **Pontecorvo-Maki-Nakagawa-Sakata mixing matrix**:
3 neutrinos \rightarrow 3 angles (θ_{12} , θ_{23} , θ_{13}) + 1 CP-violating phase (δ).

PMNS matrix: U

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} 1 & & \\ & c_{23} & s_{23} \\ & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & s_{13} e^{-i\delta} & \\ -s_{13} e^{i\delta} & 1 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & \\ -s_{12} & c_{12} & \\ & & 1 \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix} \rightarrow \begin{pmatrix} m_1 \\ m_2 \\ m_3 \end{pmatrix}$$

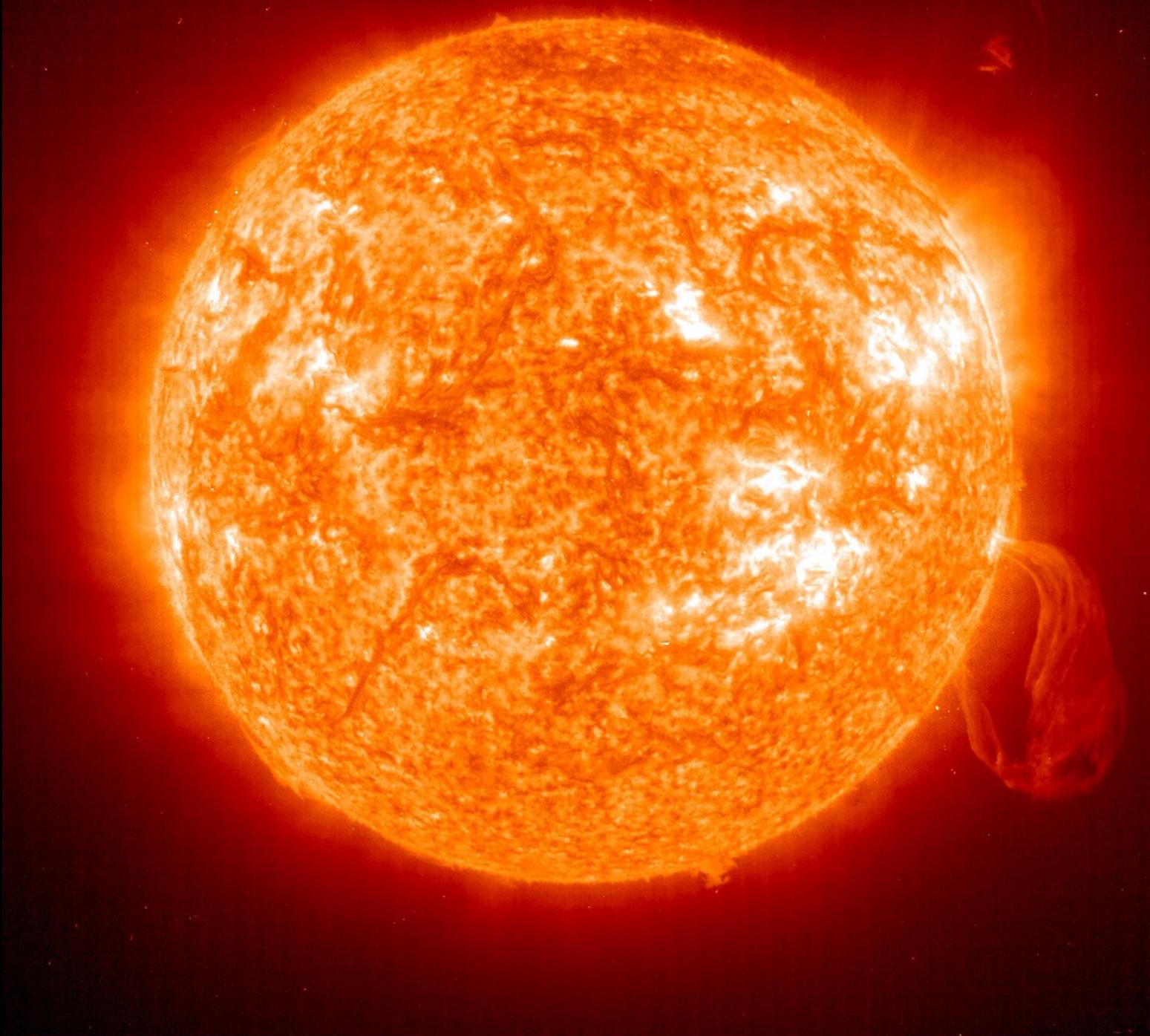
$c_{ij} = \cos \theta_{ij}$, $s_{ij} = \sin \theta_{ij}$

Atmospheric & Long-baseline accelerator experiments Reactor & Long-baseline accelerator experiments Solar & KamLAND experiments

- CP violation only possible if all three angles are not zero.

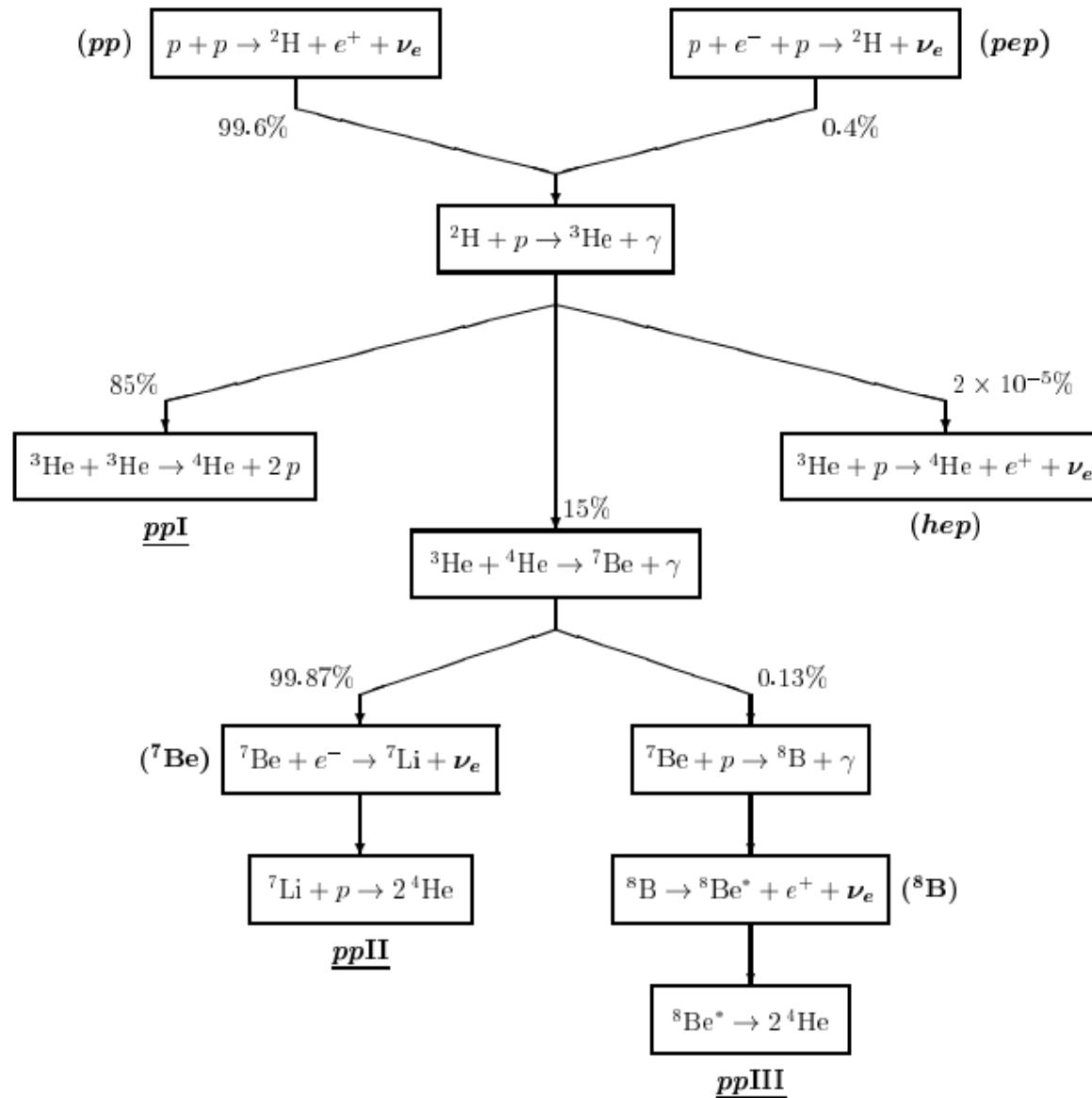
Measurement of θ_{12} and Δm^2_{21}

Solar experiments



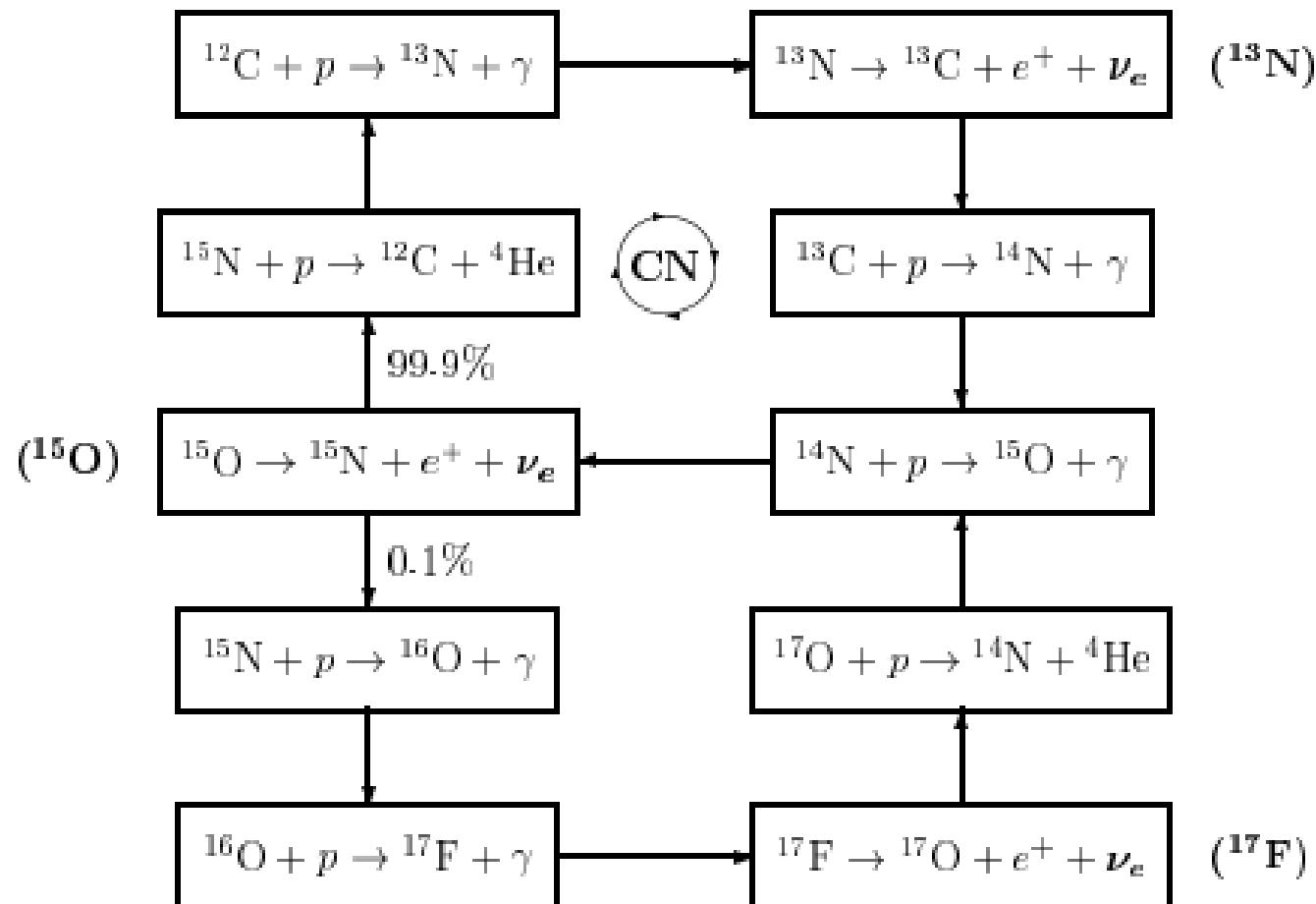
Solar neutrinos: pp chain

- 98.4% of Sun's fusion energy.

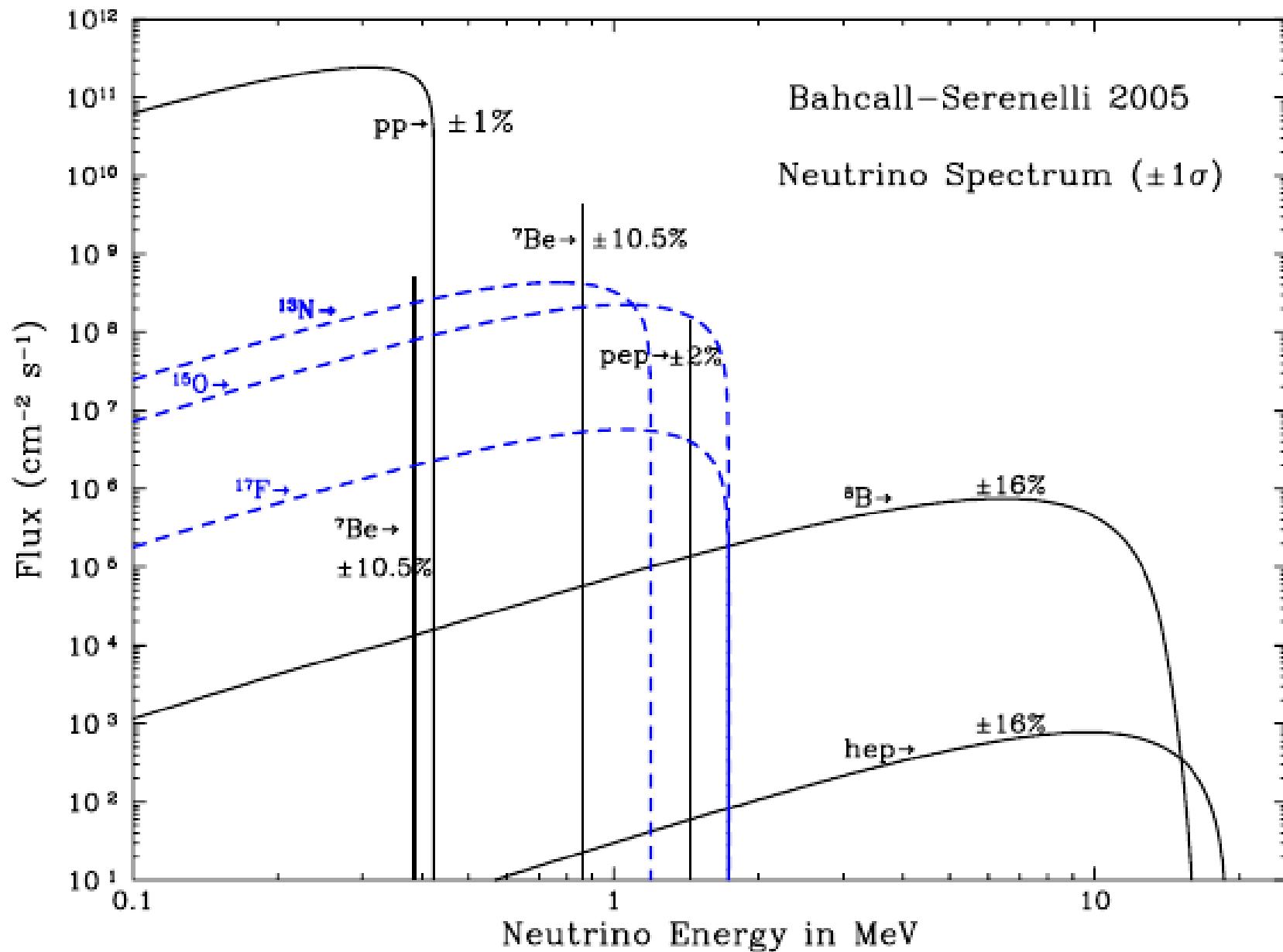


Solar neutrinos: CNO cycle

- 1.6% of Sun's fusion energy.



Solar neutrinos: energy spectrum



Homestake experiment



Homestake experiment

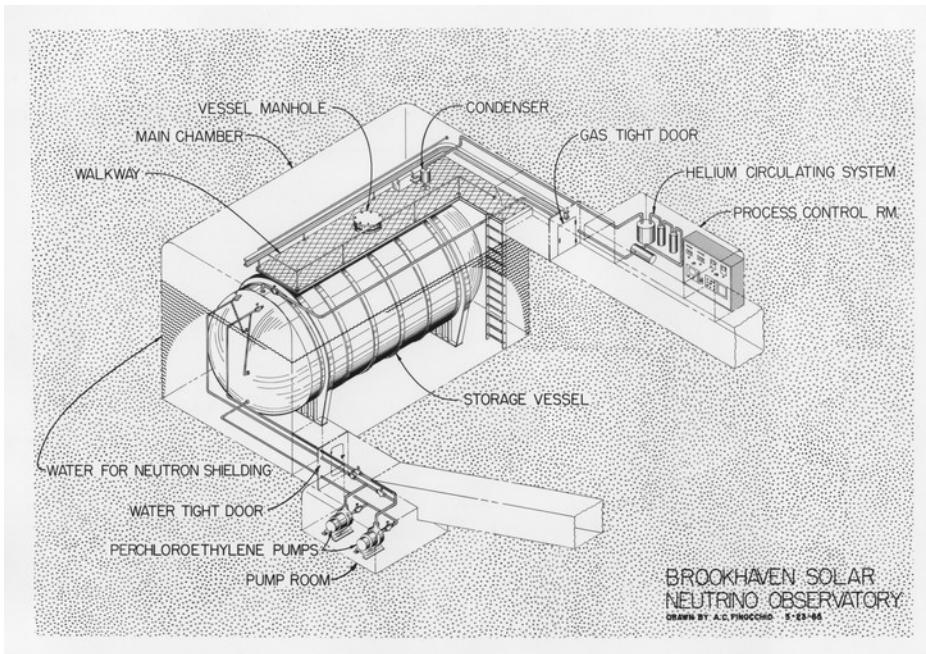
- Detection of solar neutrinos using the reaction:



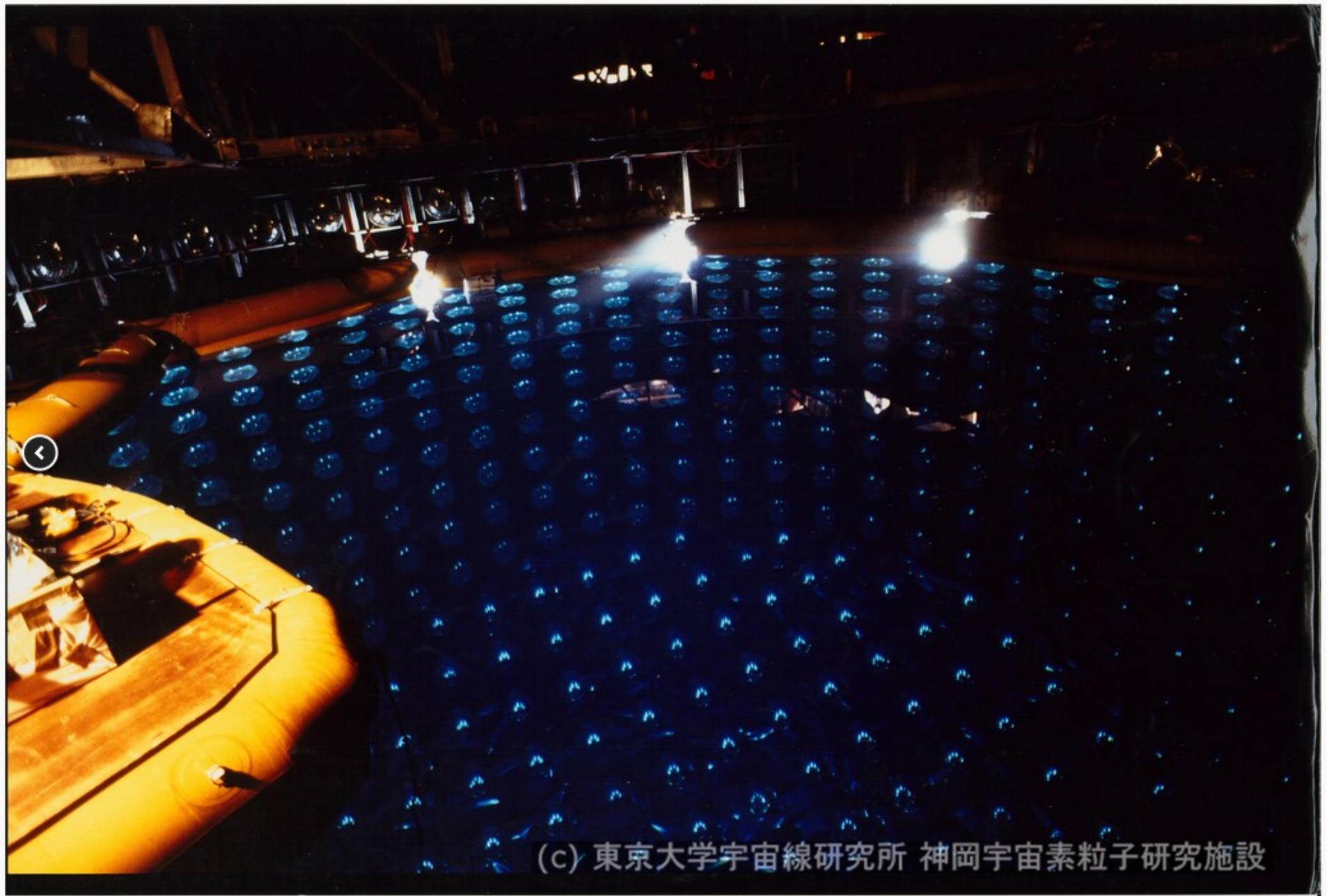
- Ratio of observed to predicted:

$$\frac{R_{\text{Cl}}}{R_{\text{SSM}}} = 0.301 \pm 0.027$$

- Missing neutrinos!



Kamiokande



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Kamiokande

- Detection of solar neutrinos using the reaction:



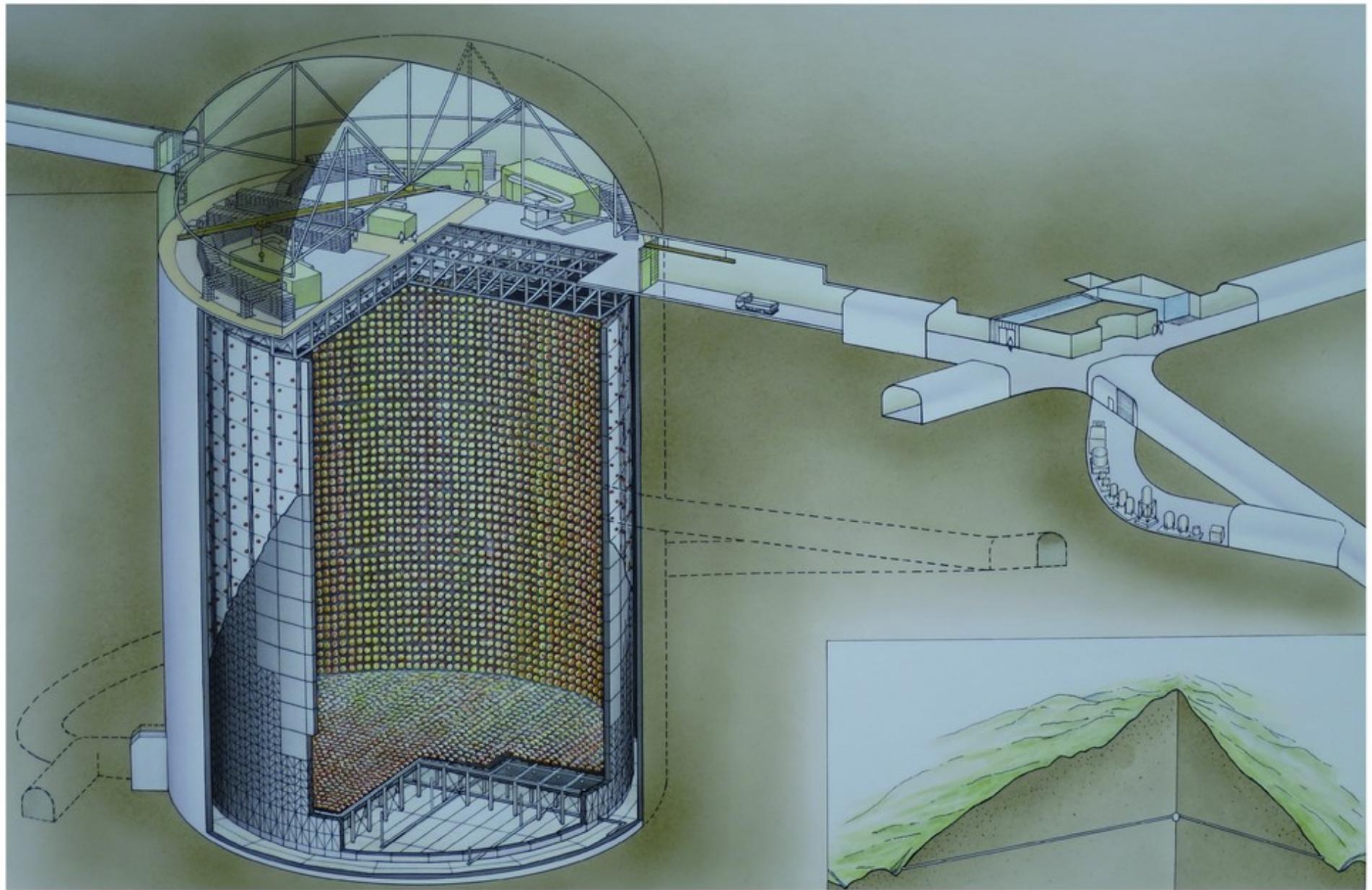
- Ratio of observed to predicted:

$$\frac{\Phi_{\text{Kamiokande}}}{\Phi_{\text{SSM}}} = 0.484 \pm 0.066.$$

- Missing neutrinos again!



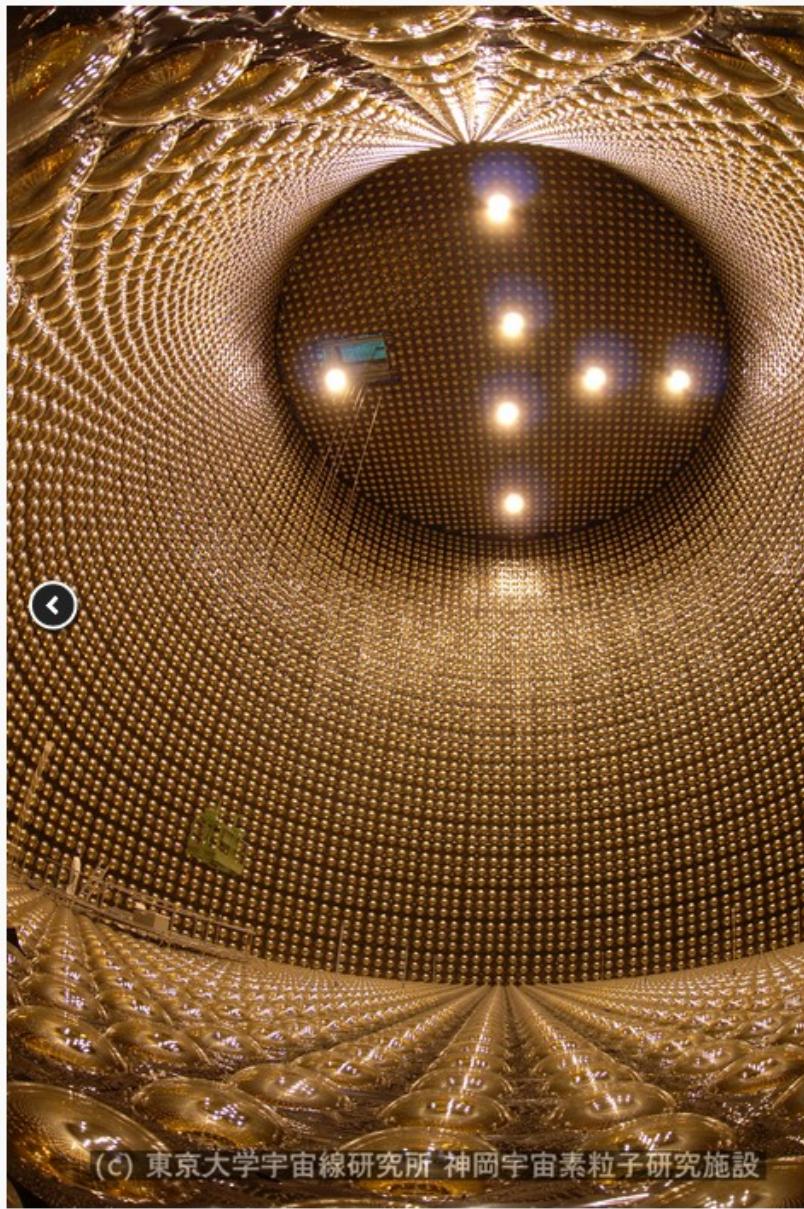
Super-Kamiokande



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NIKKEN SEKKEI

Super-Kamiokande



- Detection of solar neutrinos using the reaction:



- Ratio of observed to predicted:

$$\frac{\Phi_{\text{SK-I}}}{\Phi_{\text{SSM}}} = 0.406 \pm 0.014$$

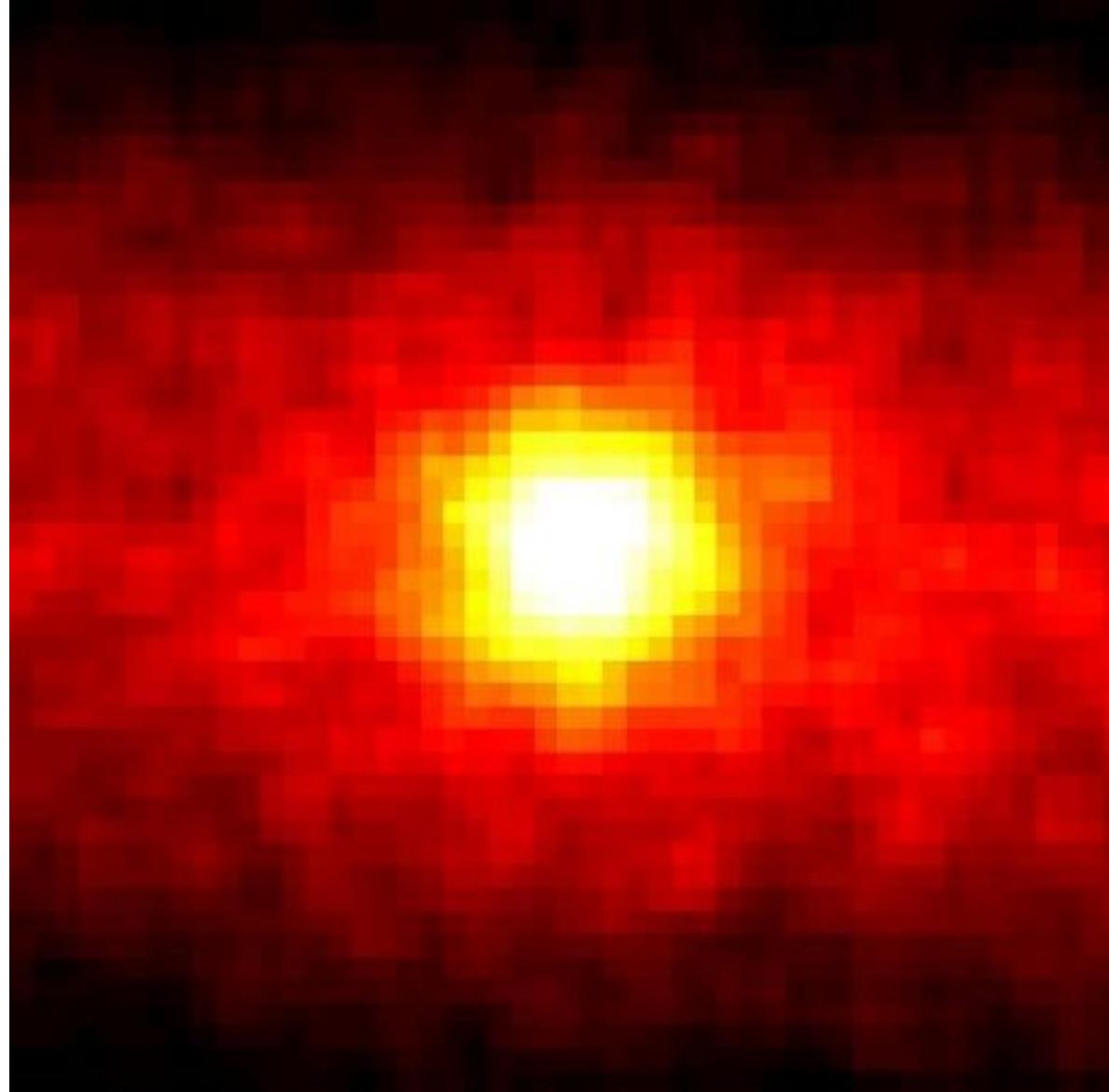
- Improved result over Kamiokande, neutrinos still missing!

Super-Kamiokande

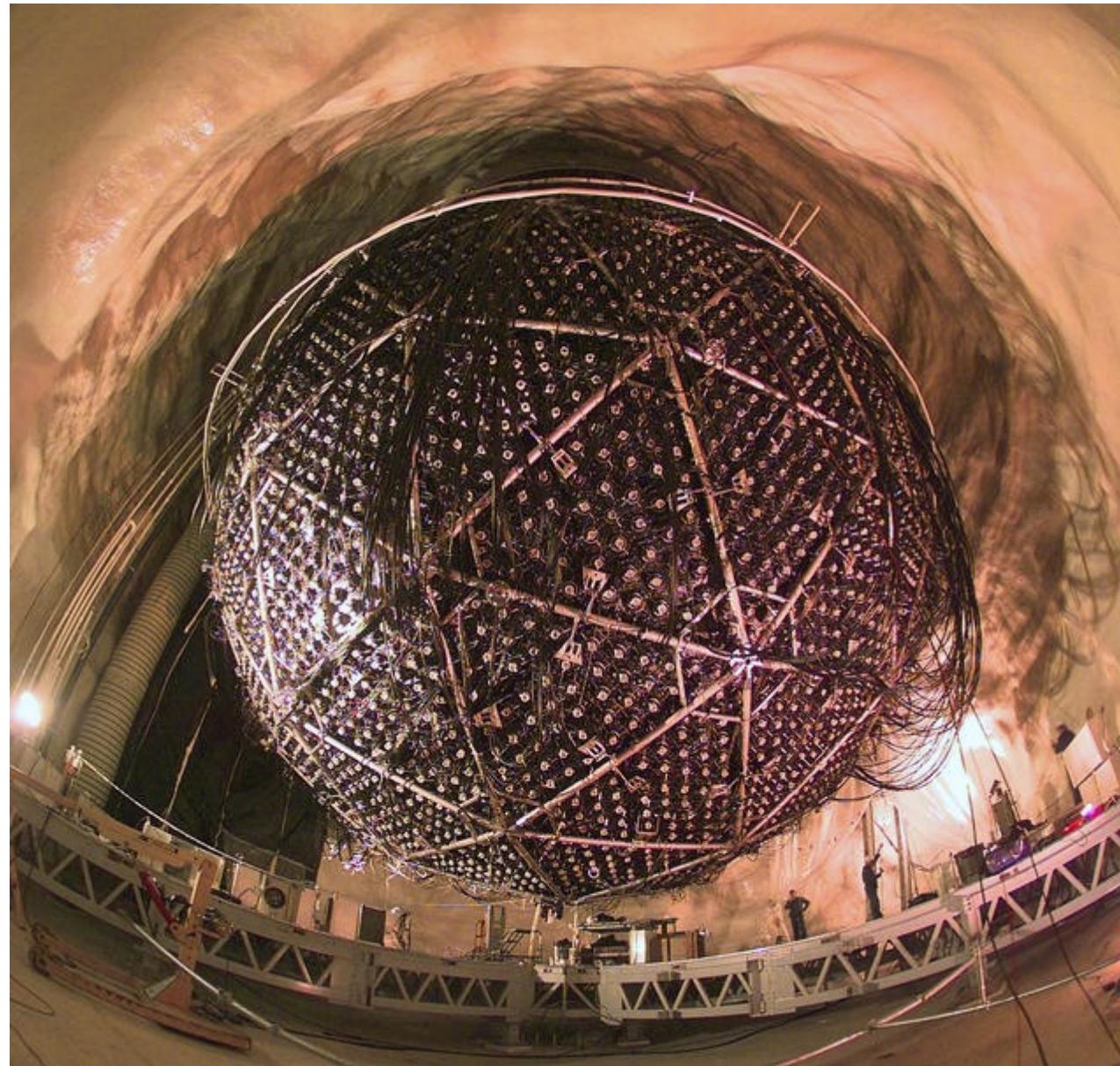


Super-Kamiokande

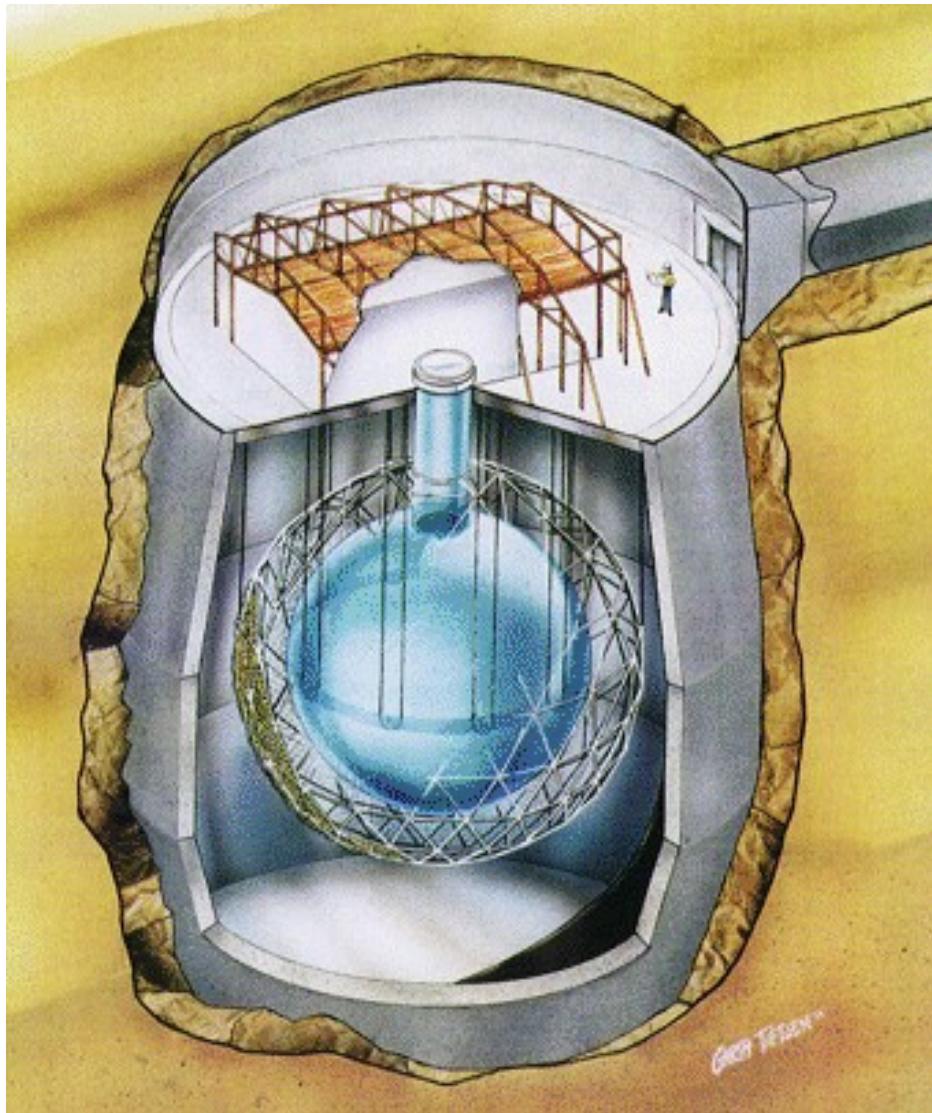
- NEUTRINOGRAPHY of the Sun. 500 days exposure!



SNO



SNO



- Detection of solar neutrinos using the reaction:

$$\nu_l + e^- \rightarrow \nu_l + e^- \quad (\text{ES})$$

$$\nu_e + D \rightarrow e^- + p + p \quad (\text{CC})$$

$$\nu_l + D \rightarrow \nu_l + p + n \quad (\text{NC})$$

- Ratio of observed to predicted:

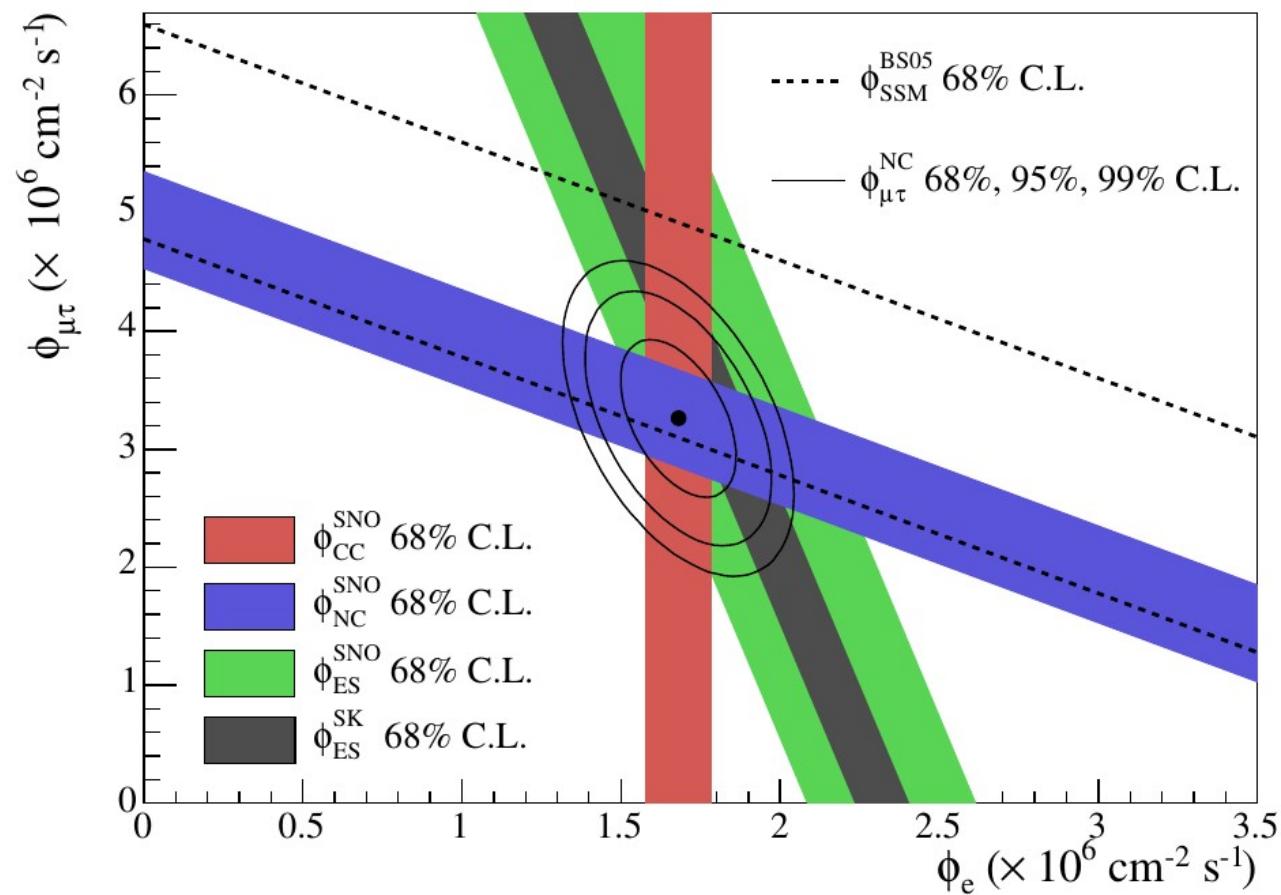
$$\frac{\Phi_{\text{SNO}}^{\text{ES}}}{\Phi_{\text{SSM}}} = 0.406 \pm 0.046$$

$$\frac{\Phi_{\text{SNO}}^{\text{CC}}}{\Phi_{\text{SSM}}} = 0.290 \pm 0.017$$

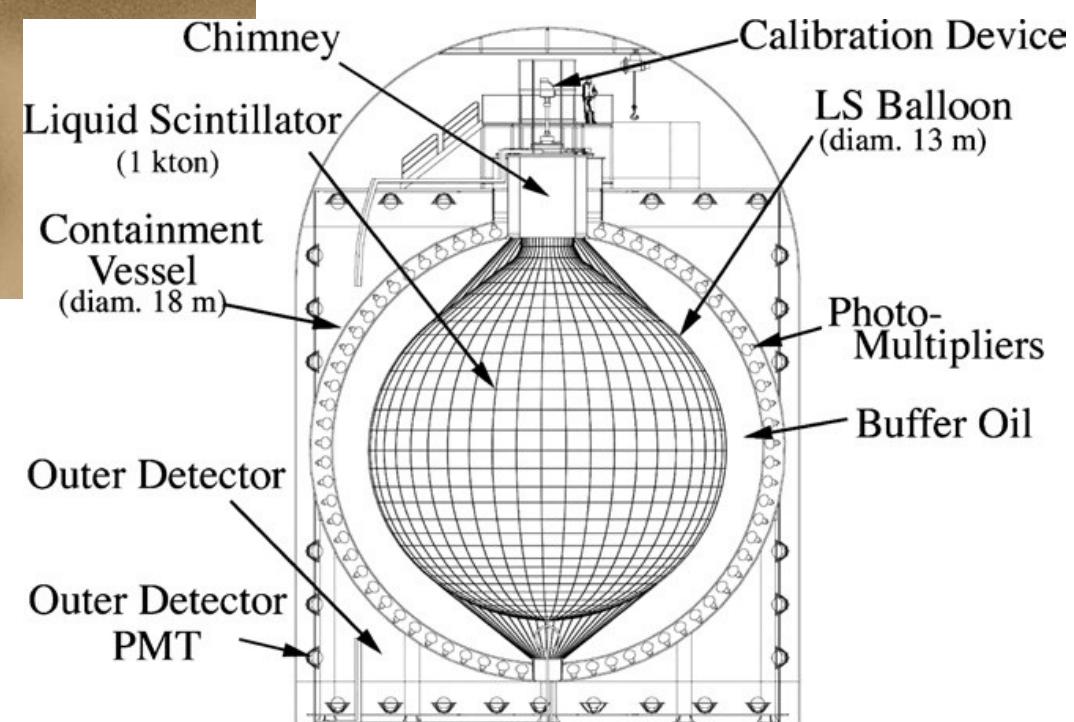
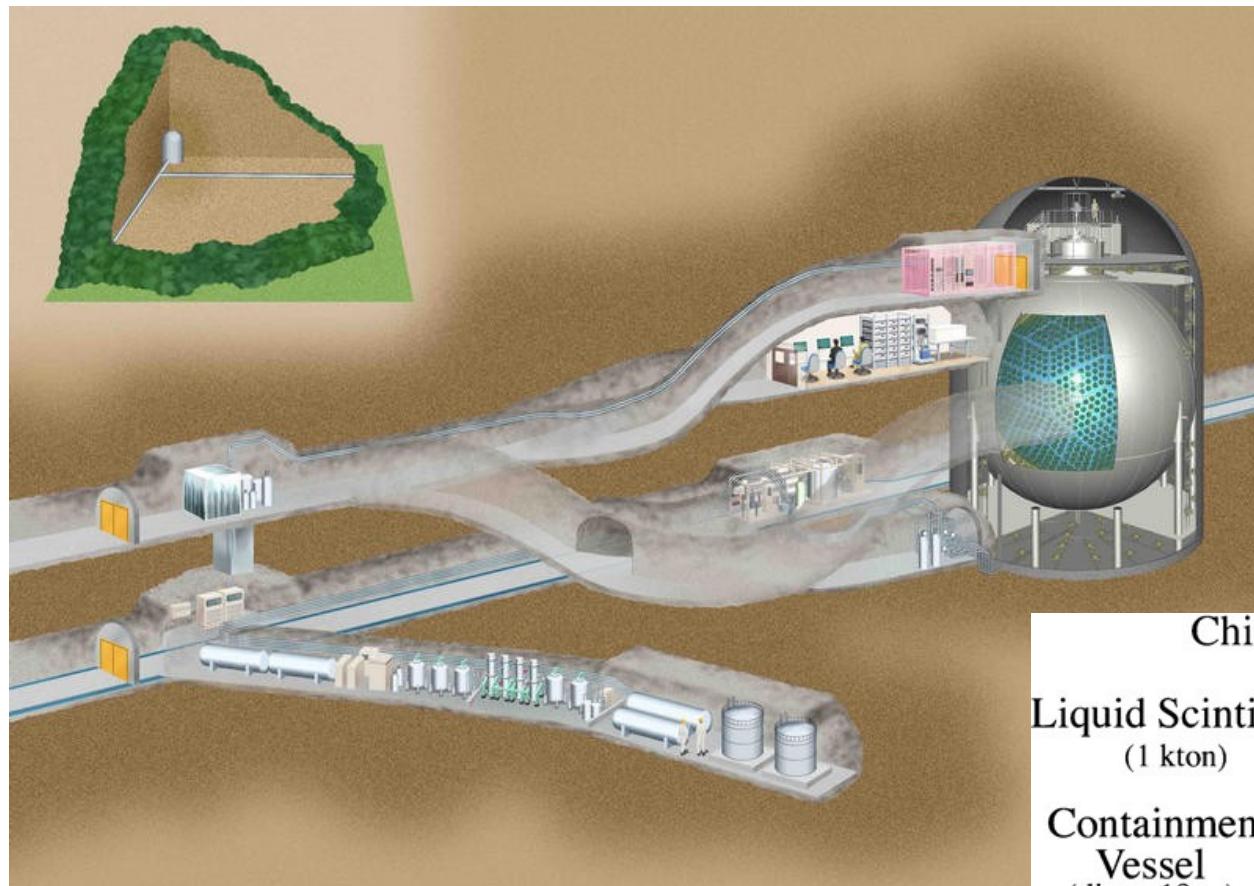
$$\frac{\Phi_{\text{SNO}}^{\text{NC}}}{\Phi_{\text{SSM}}} = 0.853 \pm 0.075$$

SNO

$$\begin{aligned}
 \Phi_{\text{SNO}}^{\nu_e} + r^{\text{ES}} \Phi_{\text{SNO}}^{\nu_{\mu, \tau}} &= \Phi_{\text{SNO}}^{\text{ES}} & r^{\text{ES}} \equiv \sigma_{\nu_{\mu, \tau}}^{\text{ES}} / \sigma_{\nu_e}^{\text{ES}} \approx 0.1553 \\
 \Phi_{\text{SNO}}^{\nu_e} &= \Phi_{\text{SNO}}^{\text{CC}} \\
 \Phi_{\text{SNO}}^{\nu_e} + \Phi_{\text{SNO}}^{\nu_{\mu, \tau}} &= \Phi_{\text{SNO}}^{\text{NC}}
 \end{aligned}$$

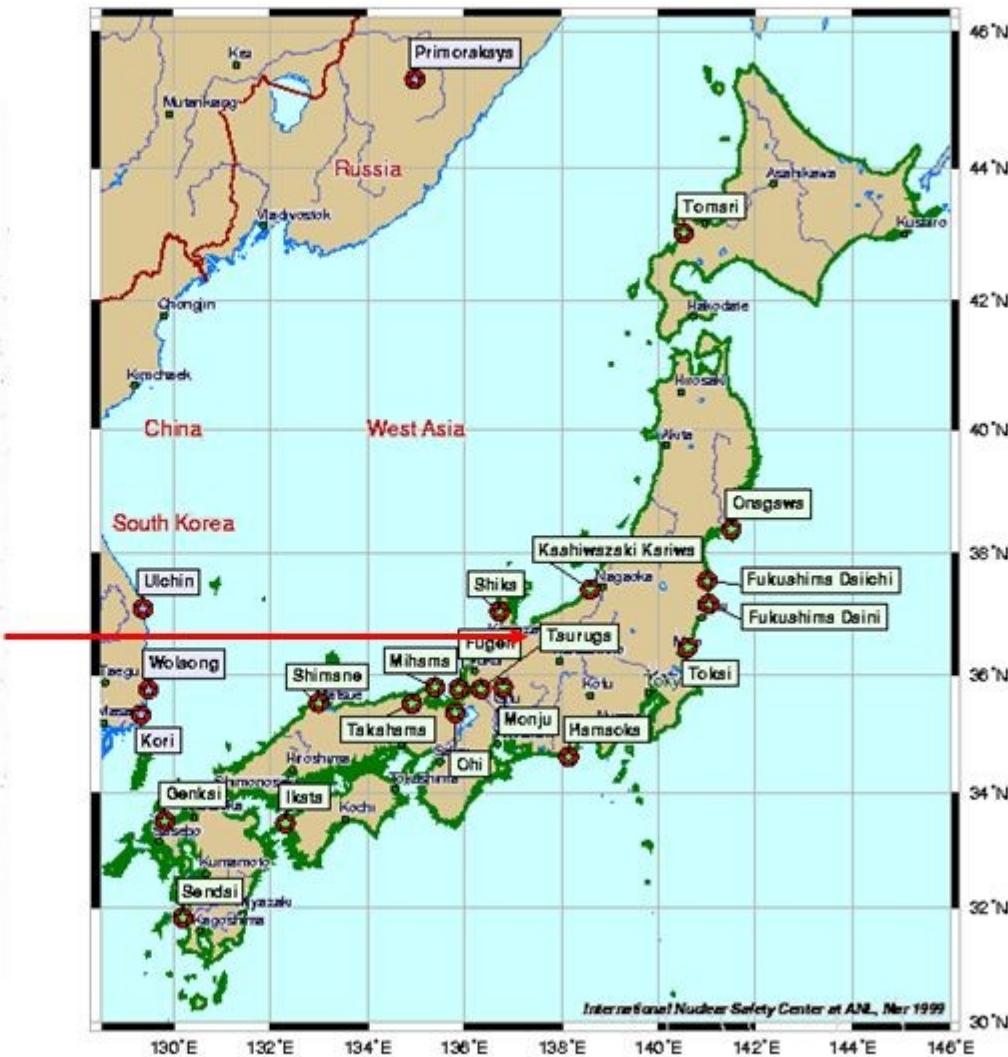
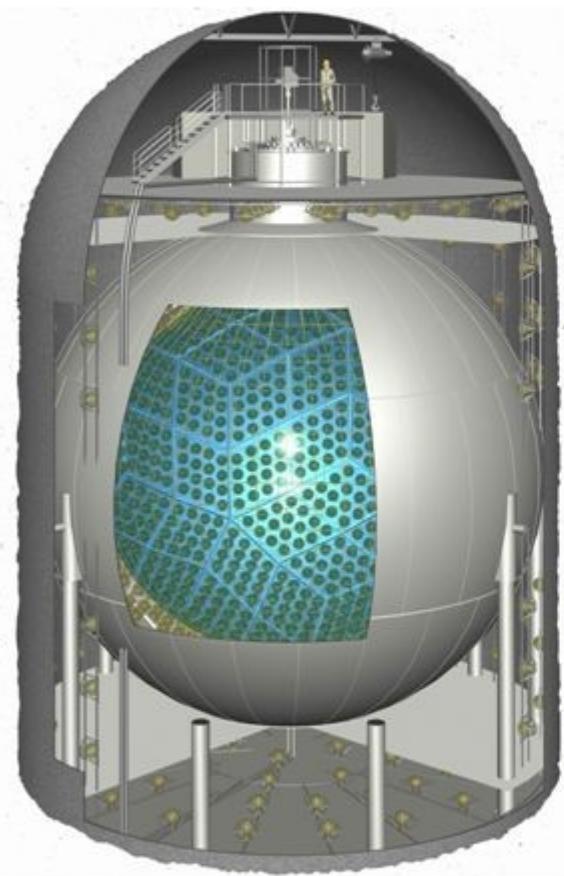


KamLAND



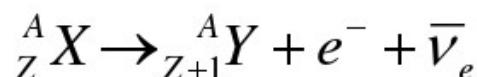


KamLAND

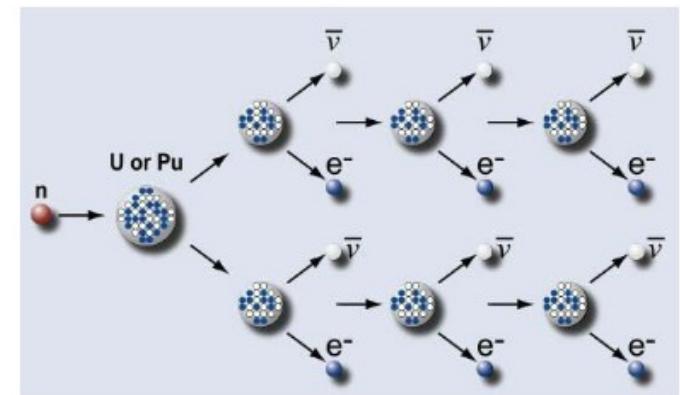


$\bar{\nu}_e$ production at nuclear reactors

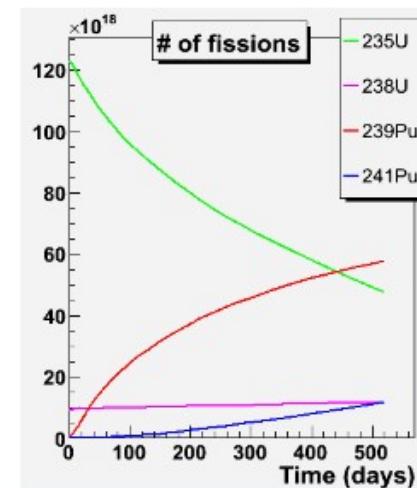
- Fission of nuclear fuel (^{235}U , ^{238}U , ^{239}Pu , ^{241}Pu) produces neutron rich fission products.
- β^- decay of fission products:



- Average per fission:
 - 200 MeV released.
 - 6 antineutrinos.

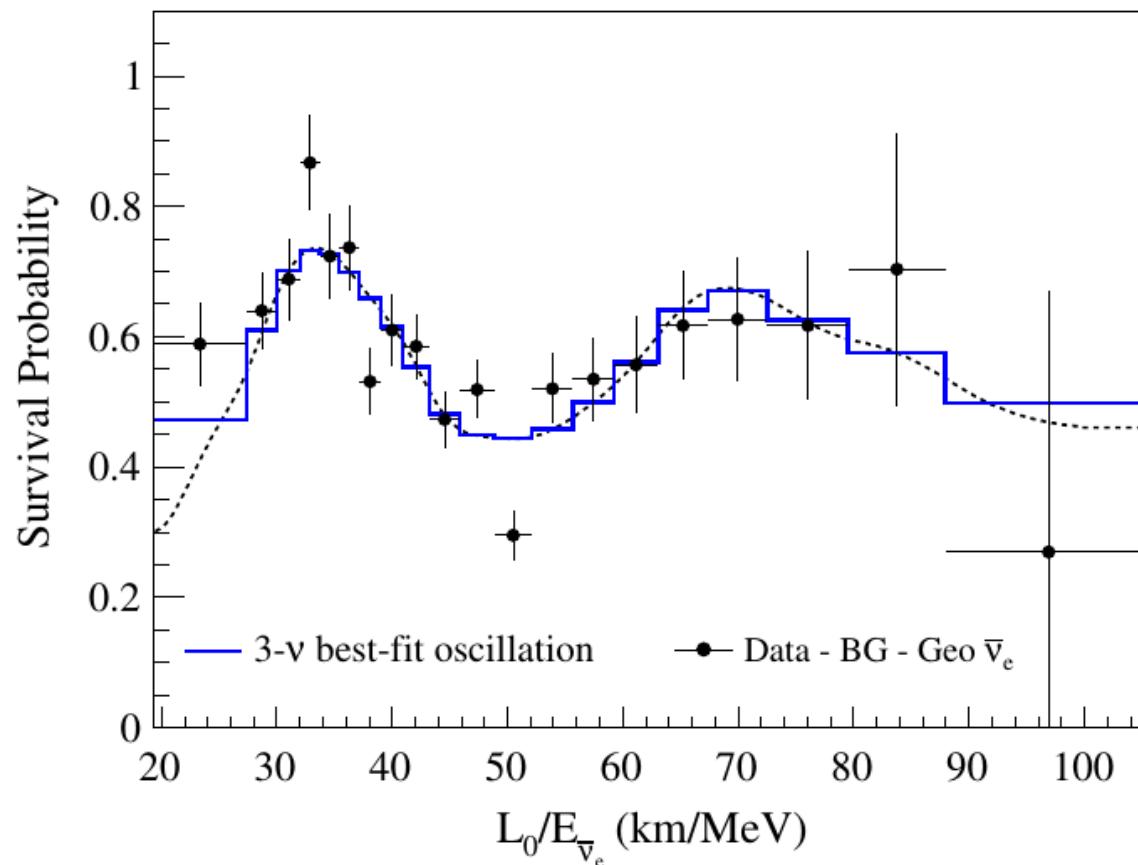
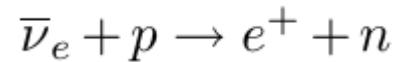


- Nuclear power plants: greatest man-made antineutrino source.
- Need to consider nuclear fuel evolution.

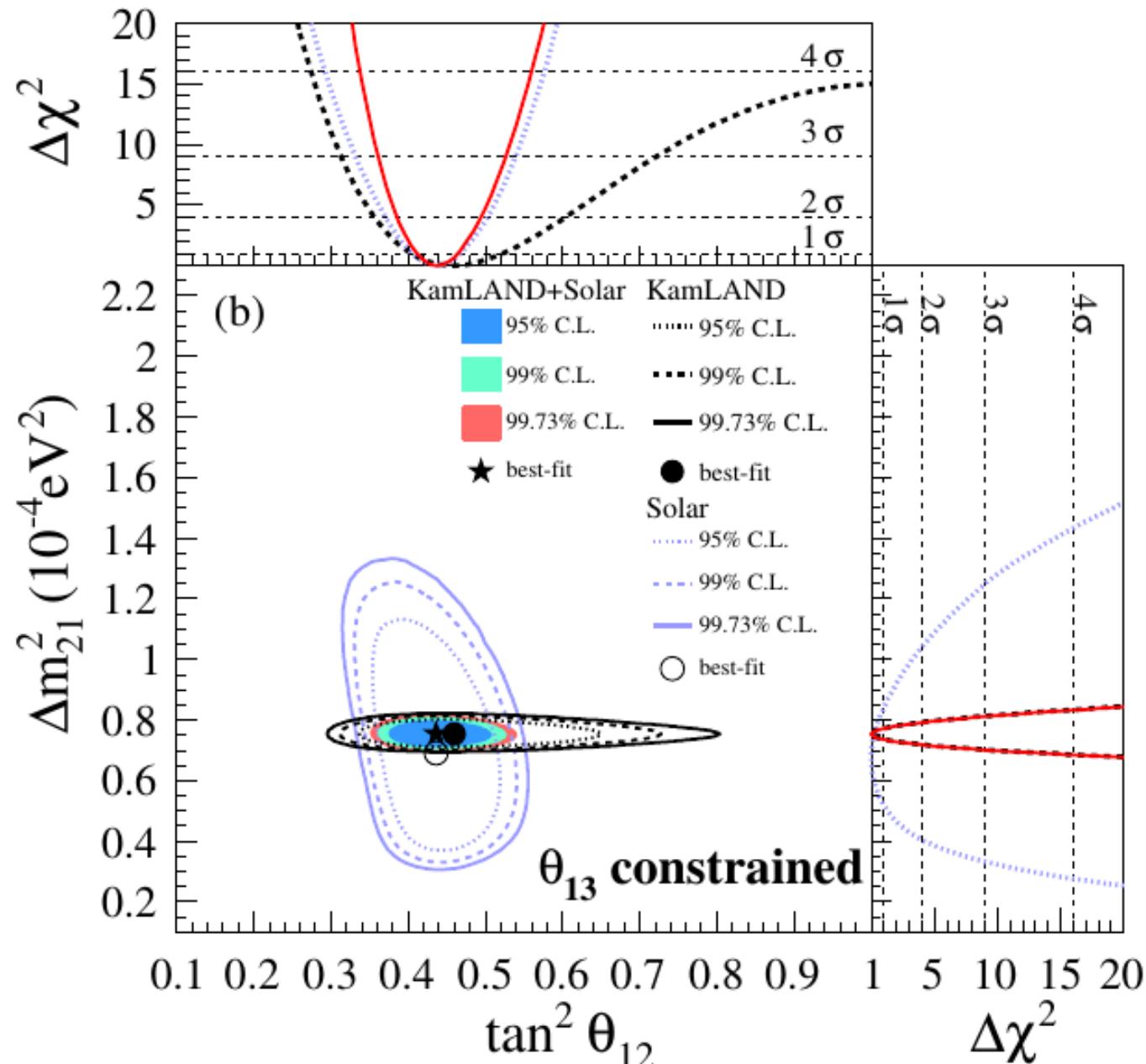


KamLAND

- Detection of reactor neutrinos using the inverse beta-decay reaction:

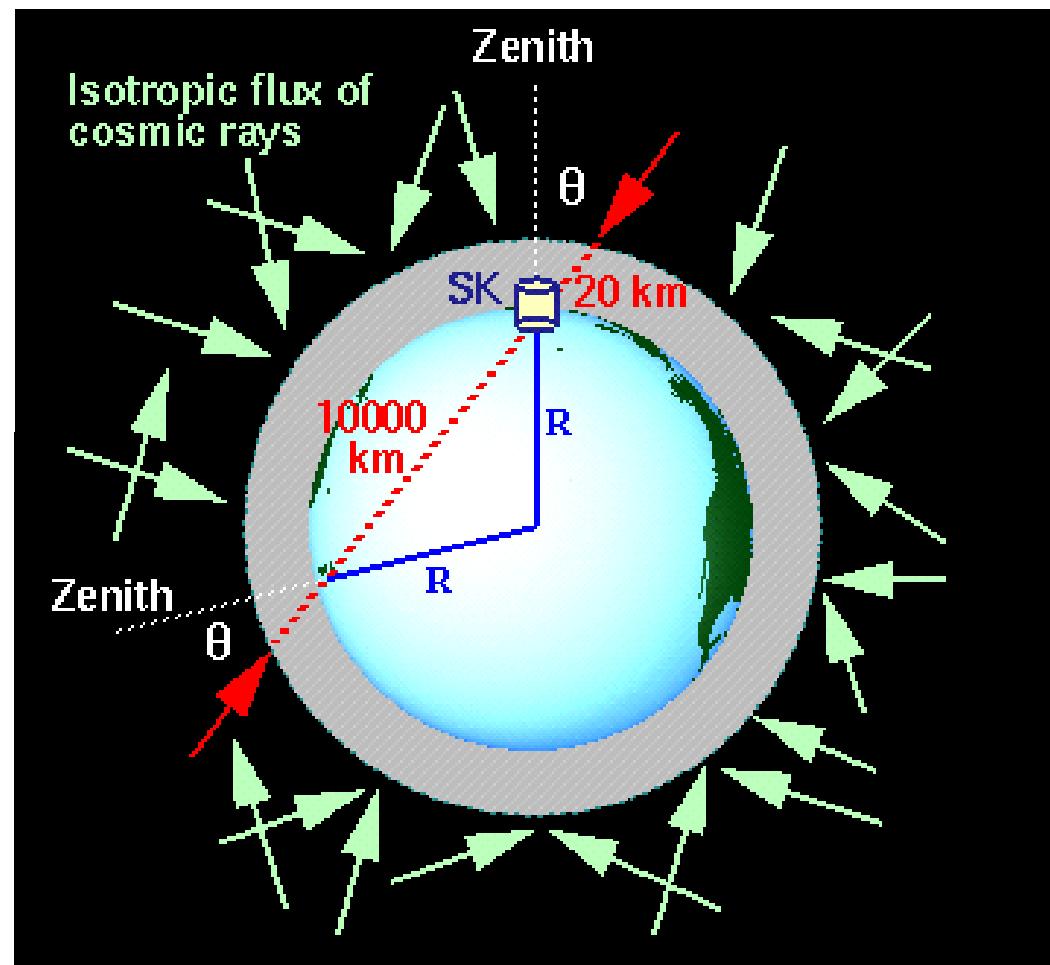
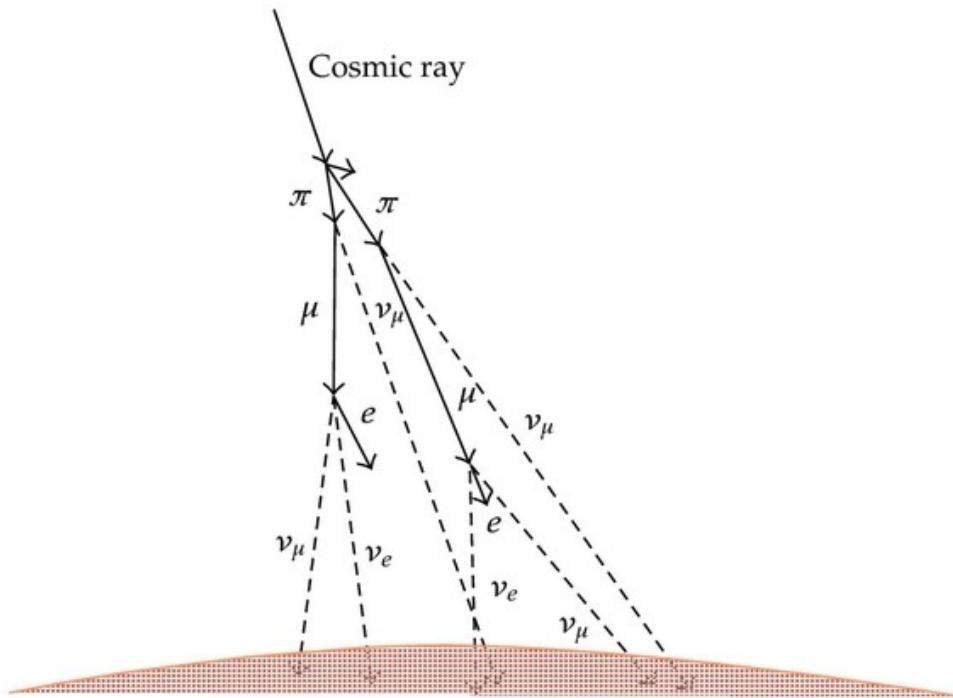


Solar + KamLAND results

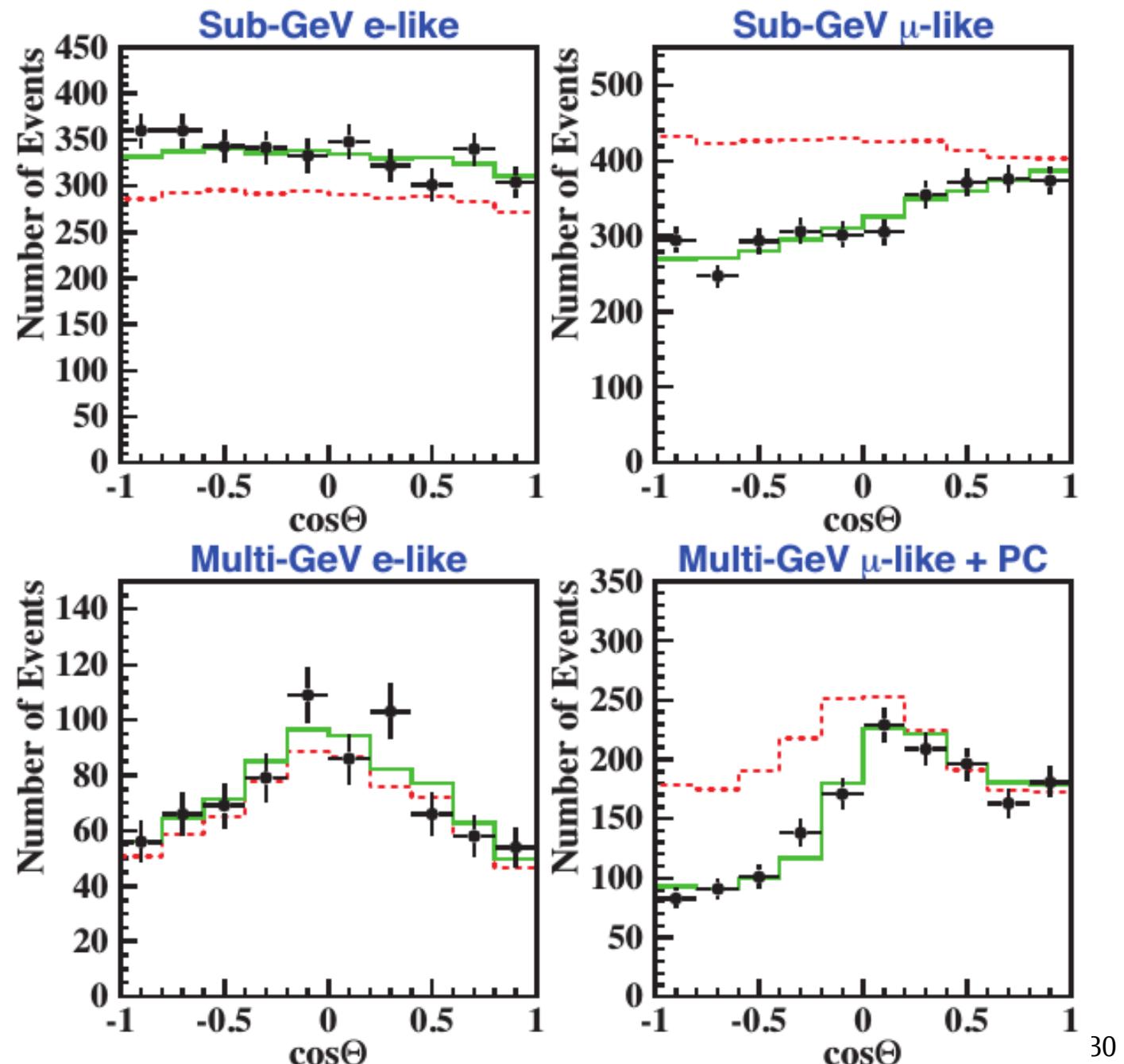
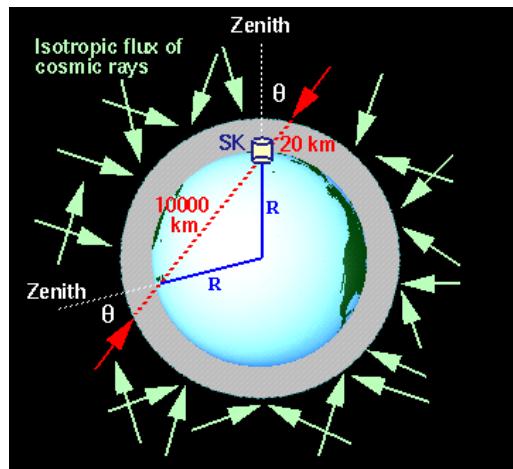


Measurement of θ_{23} and Δm^2_{atm}

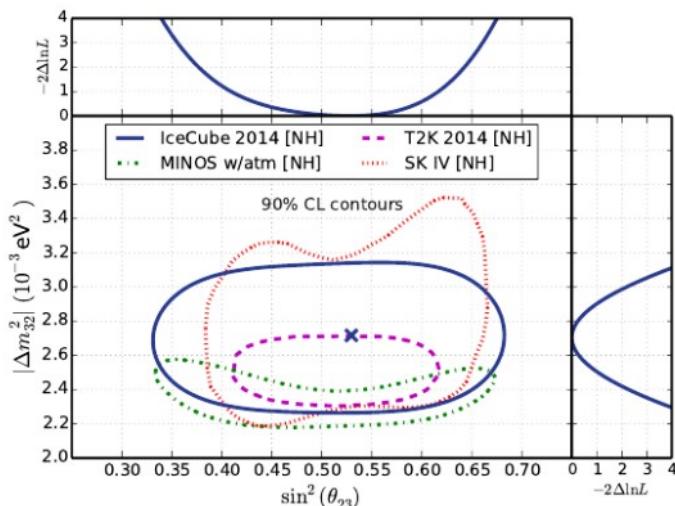
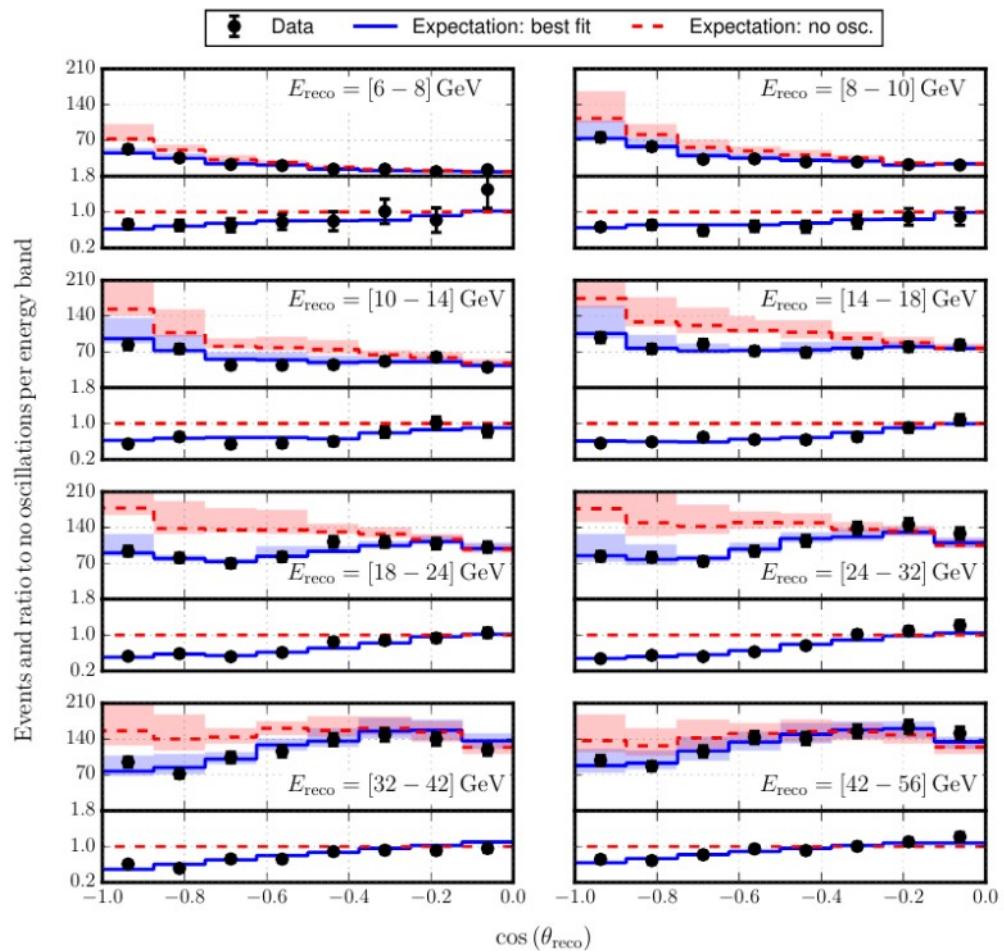
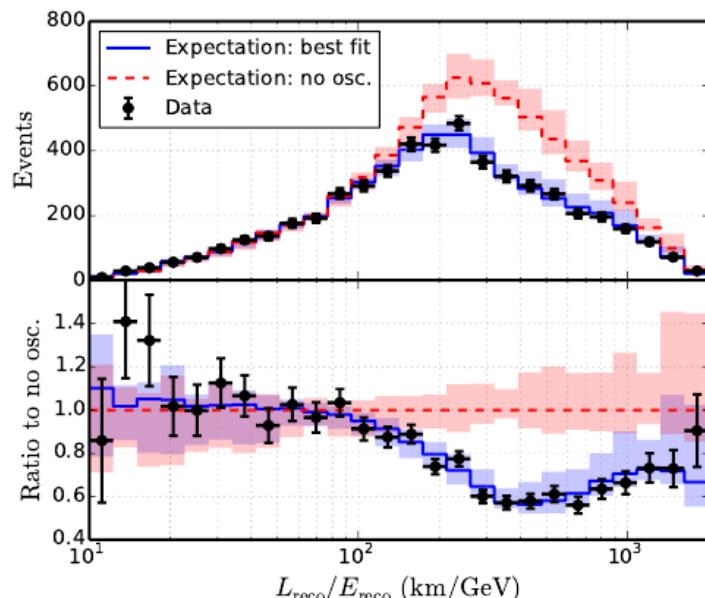
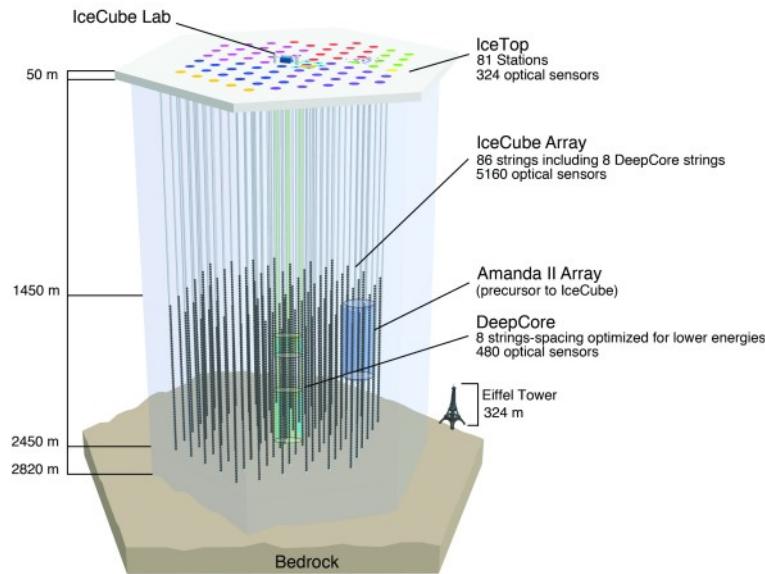
Atmospheric neutrinos



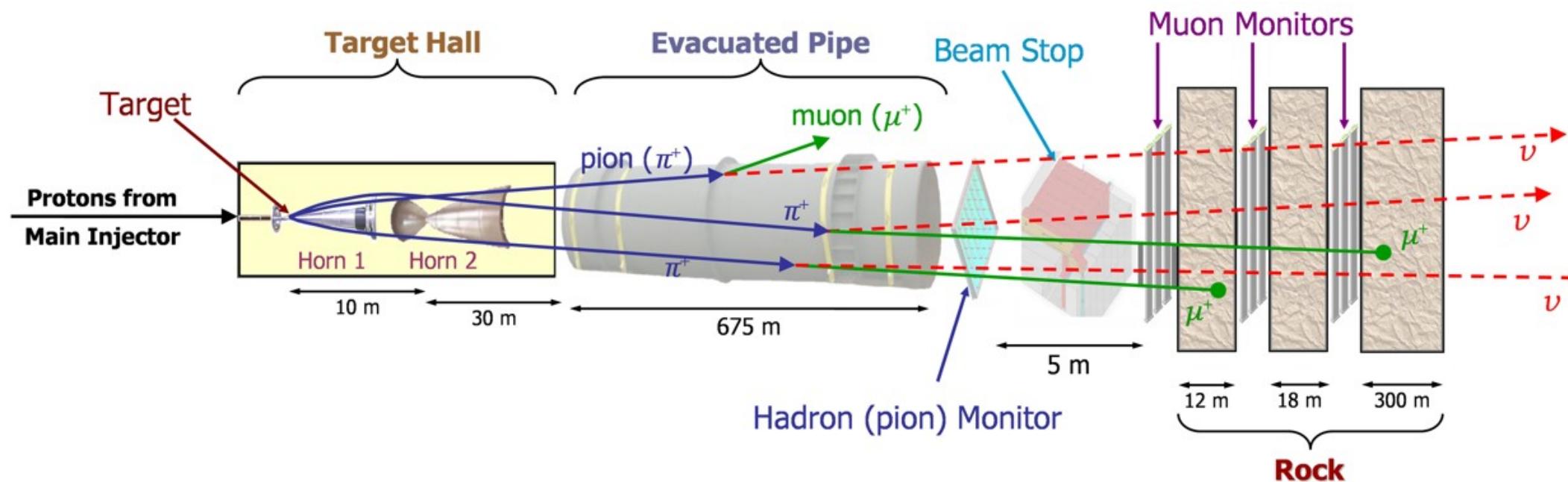
Super-Kamiokande results



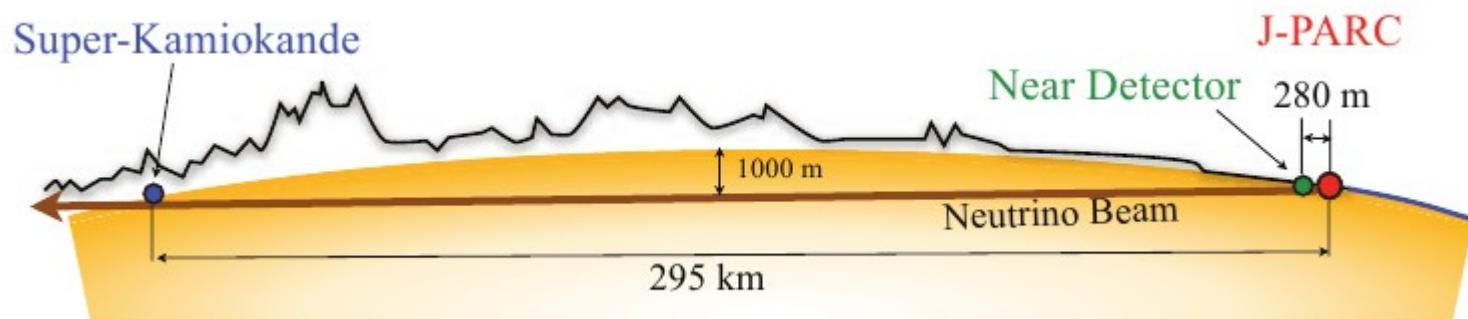
IceCube



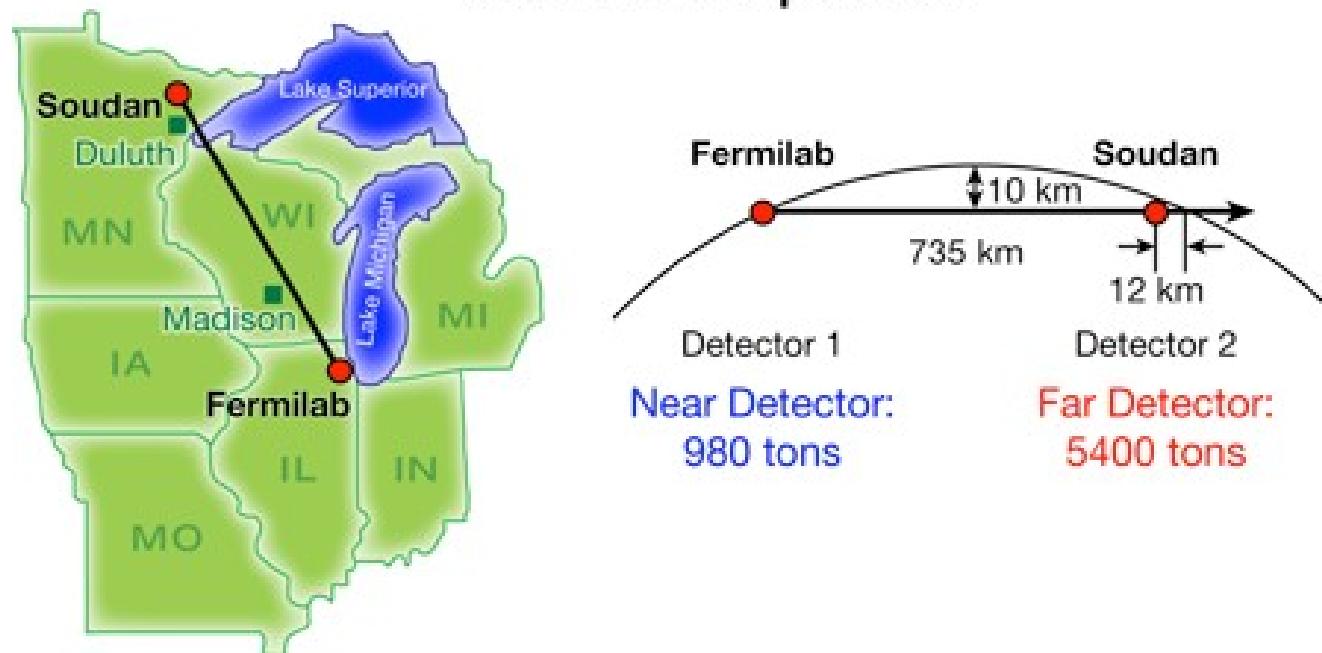
Accelerator neutrinos



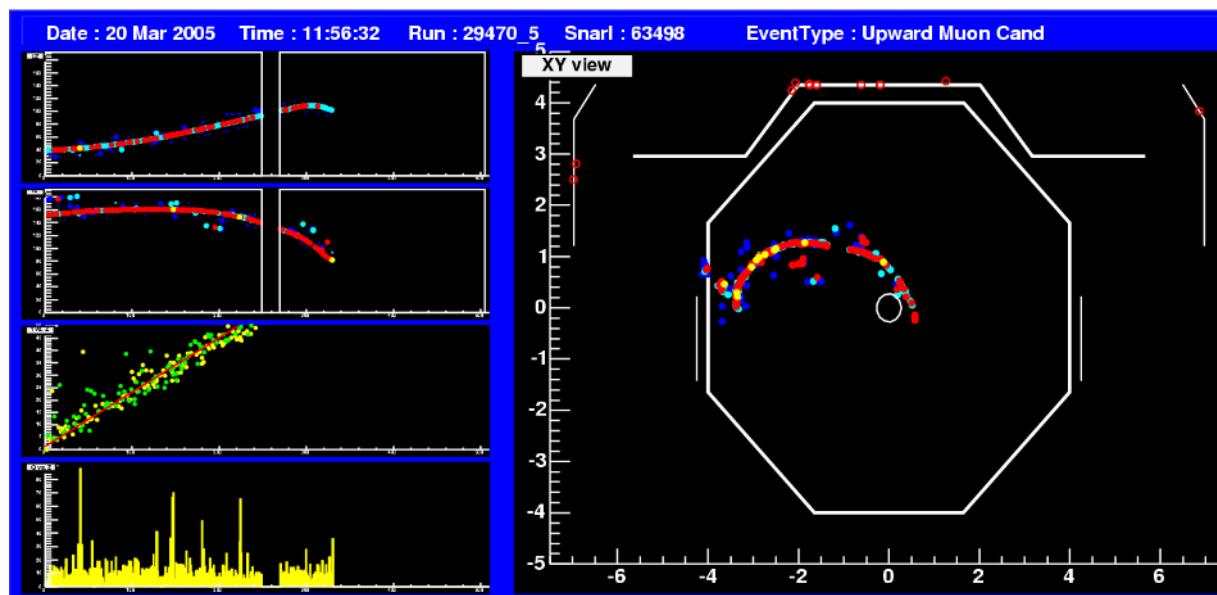
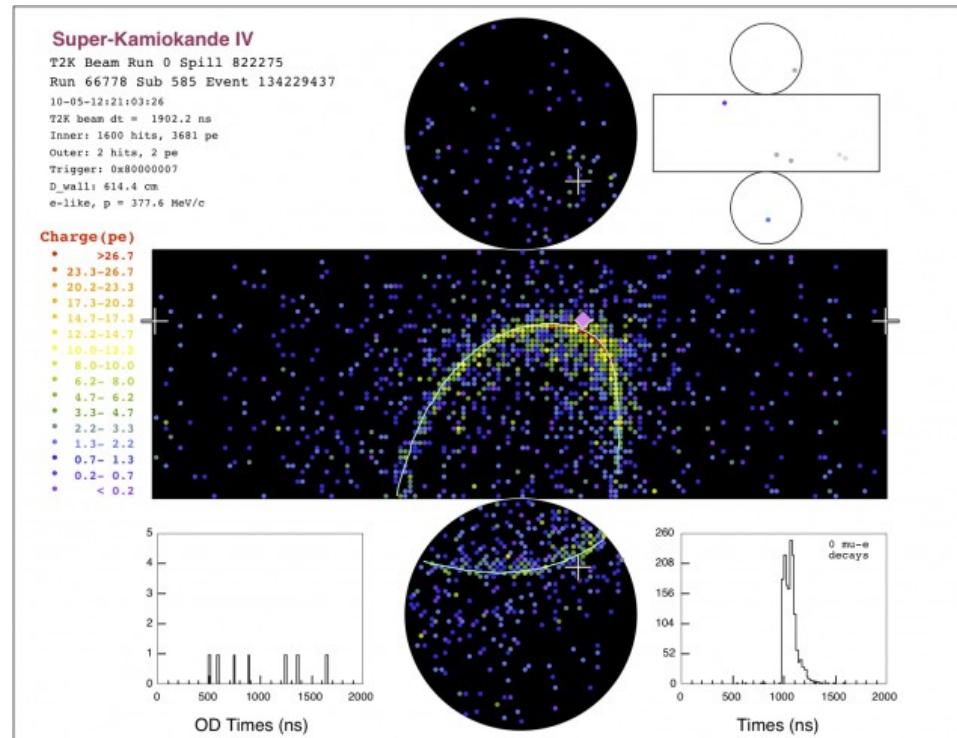
T2K & MINOS experiments



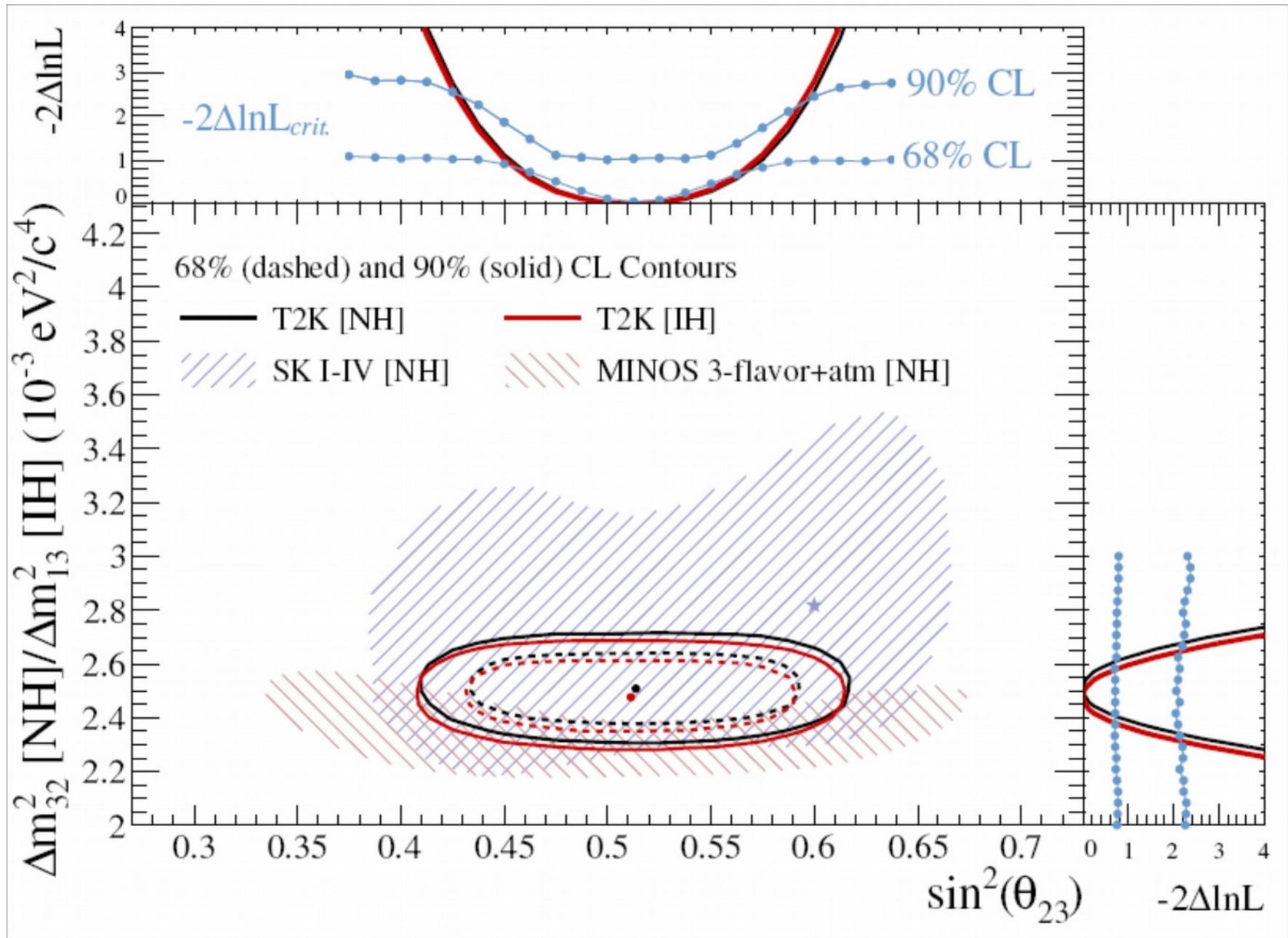
The MINOS Experiment



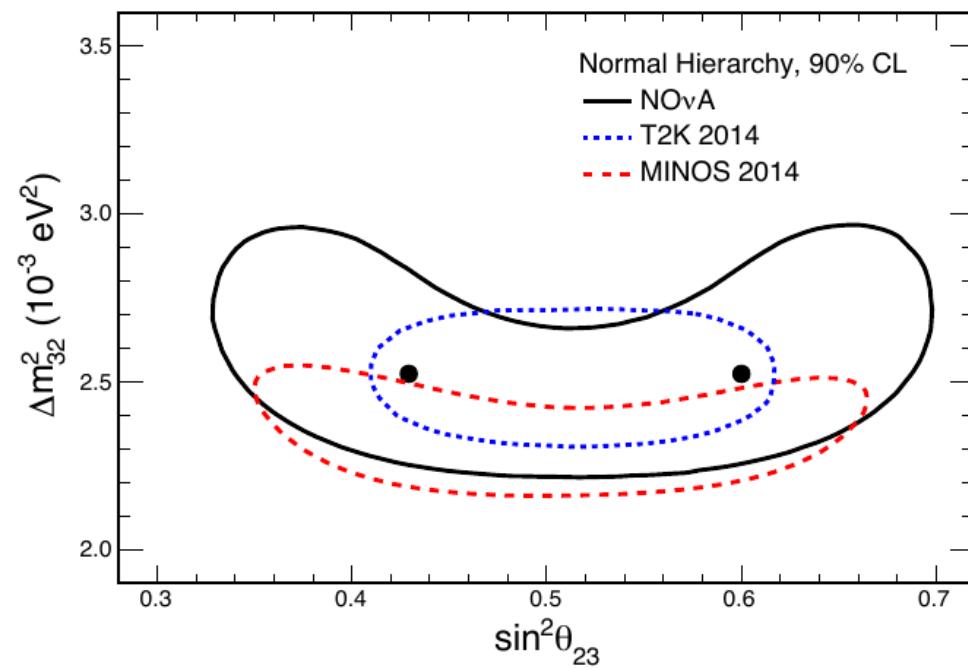
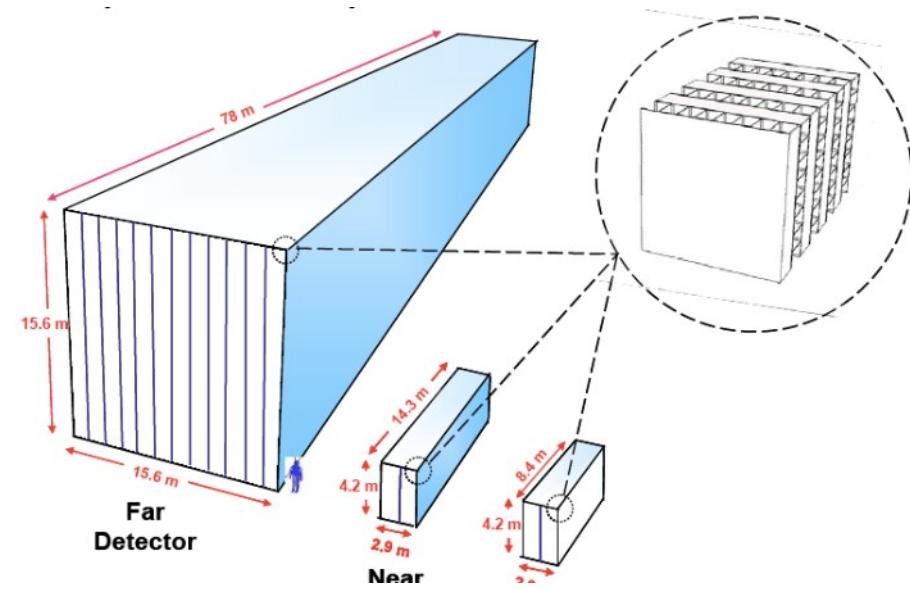
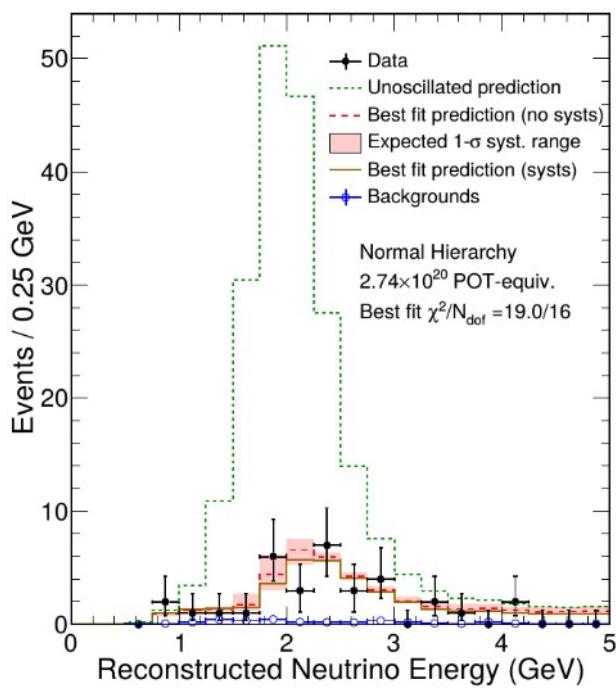
T2K & MINOS experiments



SK (atm) & T2K & MINOS

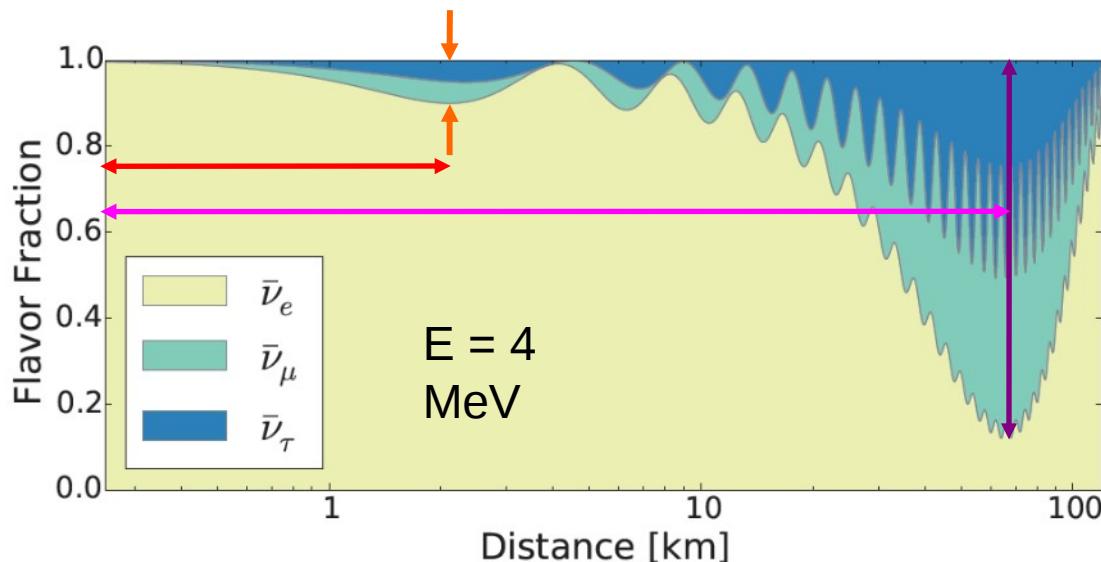


NOvA



Measurement of θ_{13}

Measurement of θ_{13} with reactors



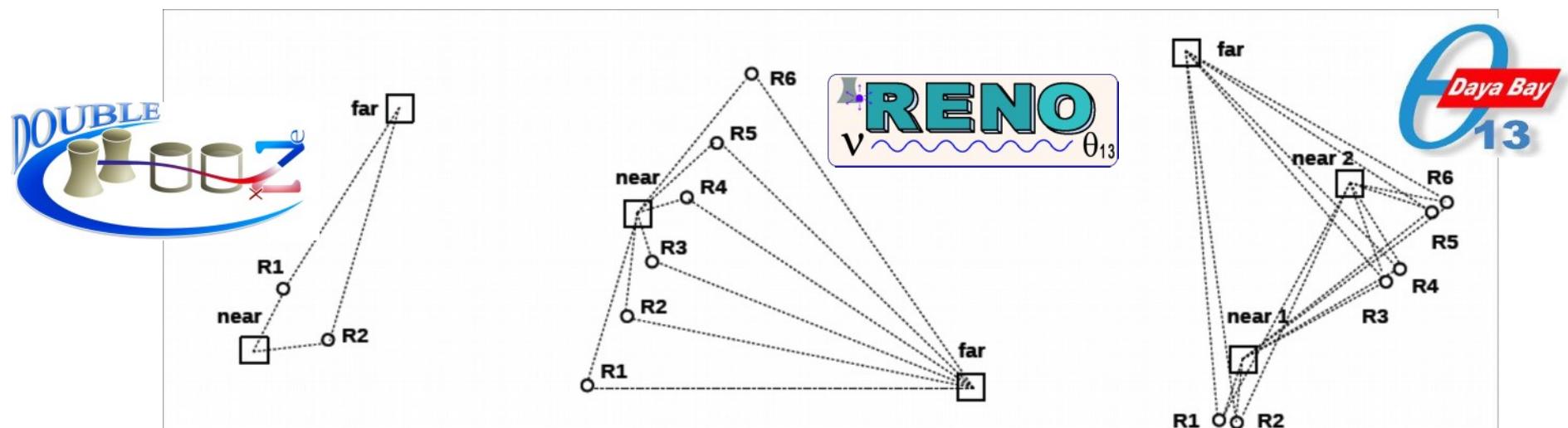
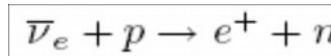
$$P_{ee}(L, E) = 1 - \cos^4(\theta_{13}) \sin^2(2\theta_{12}) \sin^2\left(\frac{\Delta m_{31}^2 L}{4E}\right) - \cos^2(\theta_{12}) \sin^2(2\theta_{13}) \sin^2\left(\frac{\Delta m_{31}^2 L}{4E}\right) - \sin^2(\theta_{12}) \sin^2(2\theta_{13}) \sin^2\left(\frac{\Delta m_{32}^2 L}{4E}\right)$$

- For baselines of ~ 1 km, the probability can be approximated by:

$$P_{ee}(L, E) \simeq 1 - \sin^2(2\theta_{13}) \sin^2\left(\frac{\Delta m_{31}^2 L}{4E}\right) \approx 1 - \sin^2(2\theta_{13}) \sin^2\left(1.27 \frac{\Delta m_{31}^2 [\text{eV}^2] L [\text{m}]}{E [\text{MeV}]}\right)$$

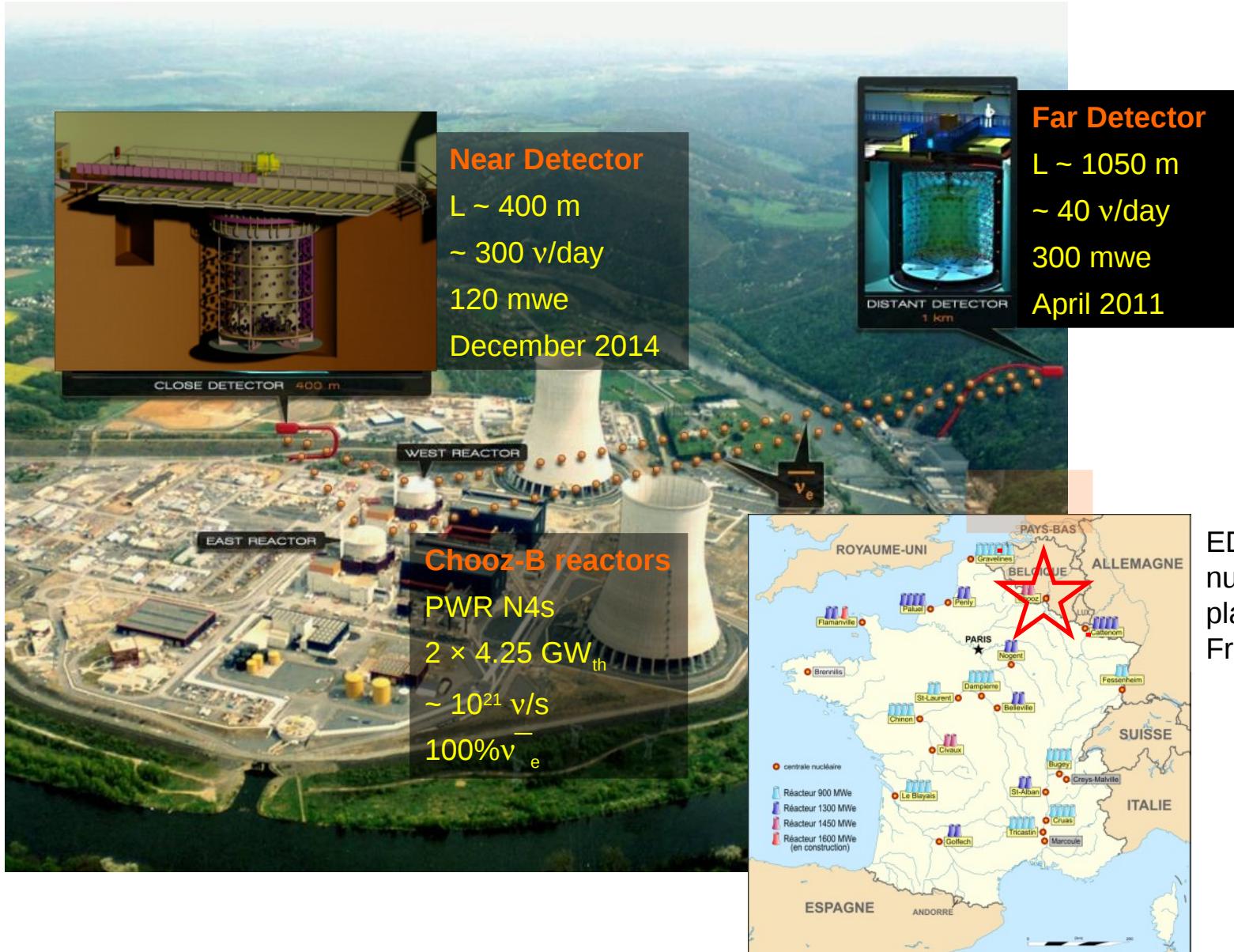
Measurement of θ_{13} with two-detector reactor experiments

- Antineutrinos detected by inverse β -decay:
on Gd-loaded liquid scintillator calorimeters.
- Reactor prediction and the antineutrino detection systematics can be reduced if **two identical detectors**, one near and one far from the reactors, are built.



Experiment	Reactor power (GW _{th})	Distance (m) Near / Far	Depth (mwe) Near / Far	Target mass (ton) \times detectors
Double Chooz	8.5	400 / 1050	120 / 300	8×2
Daya Bay	17.4	470, 576 / 1648	260 / 860	20×8
RENO	16.5	294 / 1383	120 / 450	16×2

Double Chooz: a two-detector experiment



Electron antineutrino detection

Inverse Beta Decay (IBD):

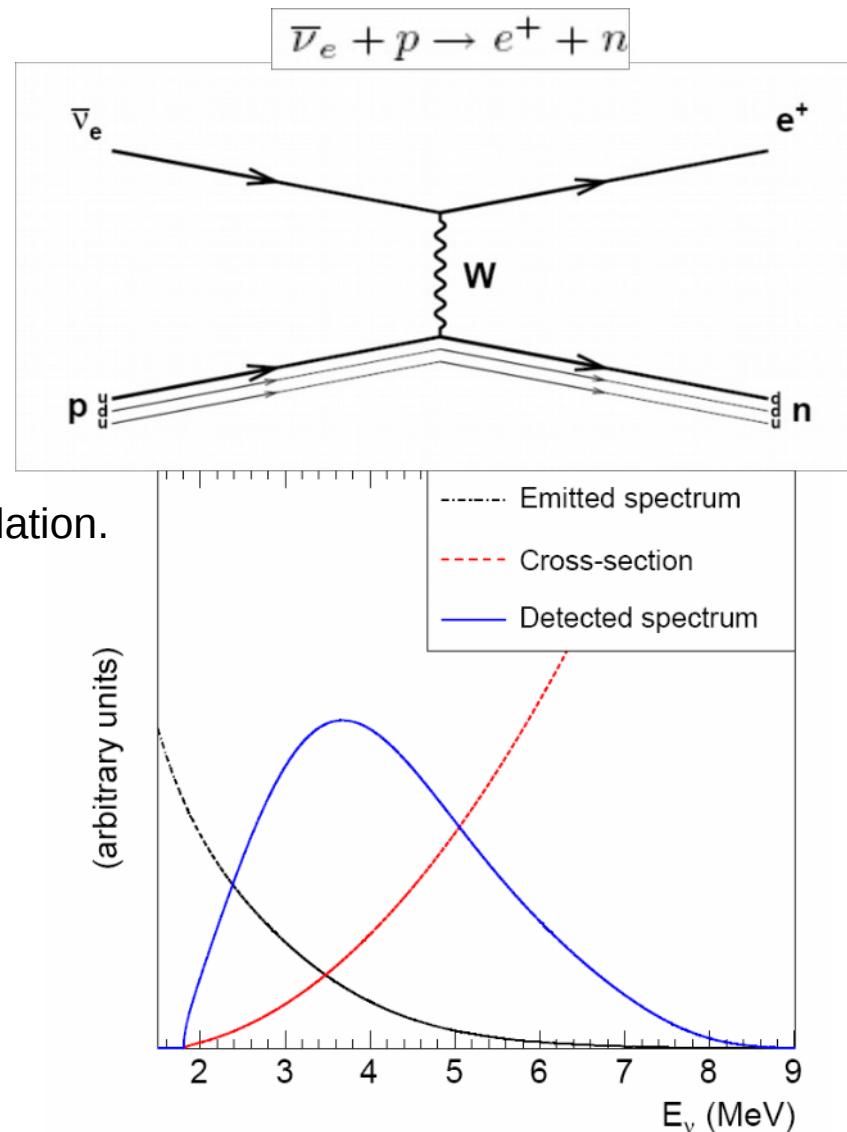
- Reaction threshold: $E_\nu \geq 1.806$ MeV.
- Disappearance experiment.
- Well known cross-section (0.2%).
- Coincidence of 2 signals: background suppression.

Prompt signal:

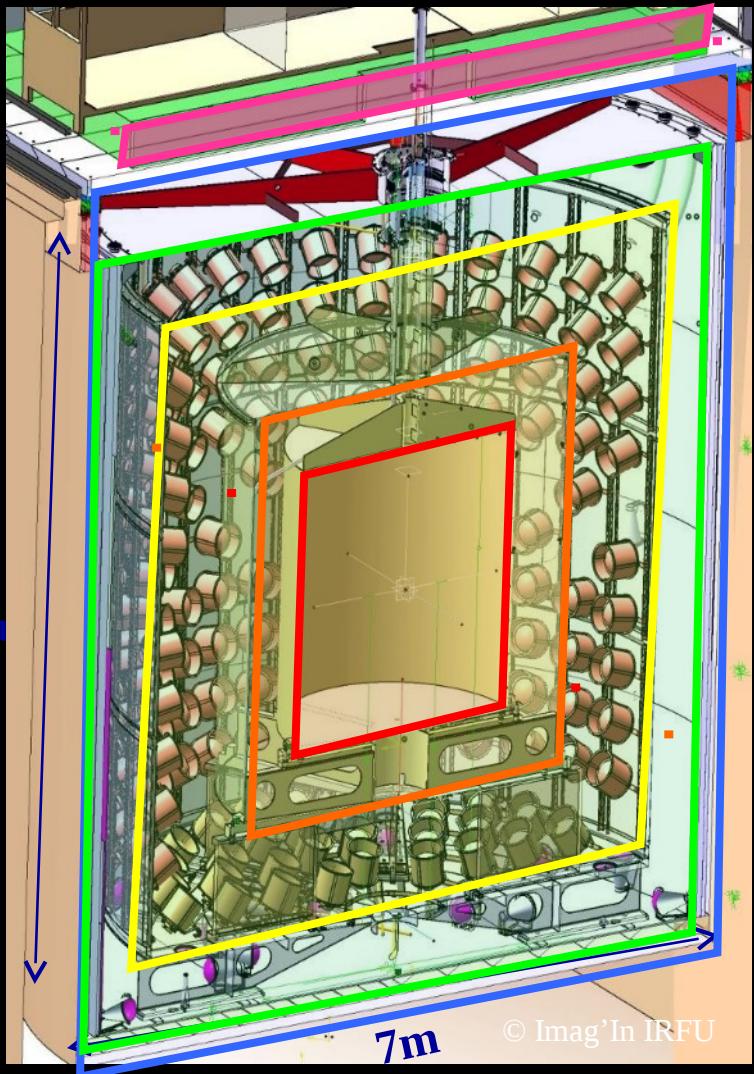
- Positron kinetic energy + γ 's from annihilation.
- $E_{\text{prompt}} \approx E_\nu - 0.782$ MeV
- $E_{\text{prompt}} \sim 1 - 9$ MeV

Delayed signal:

- γ 's from radiative neutron capture.
- **Gd**: $\Delta T \sim 30$ μ s, $E_{\text{delayed}} \sim 8$ MeV.
- **H**: $\Delta T \sim 200$ μ s, $E_{\text{delayed}} = 2.22$ MeV.



The Double Chooz Far Detector



Inner Detector:

- **Neutrino Target:** acrylic vessel (8 mm) with 10.3 m³ **Gd-loaded** (1 g/l) **liquid scintillator**.
- **Gamma-Catcher:** acrylic (12 mm) vessel with 22.5 m³ of **liquid scintillator**.
- **Buffer:** stainless steel (3 mm) vessel supporting **390 10"** **PMTs**, with 110 m³ of **non-scintillating mineral oil**.

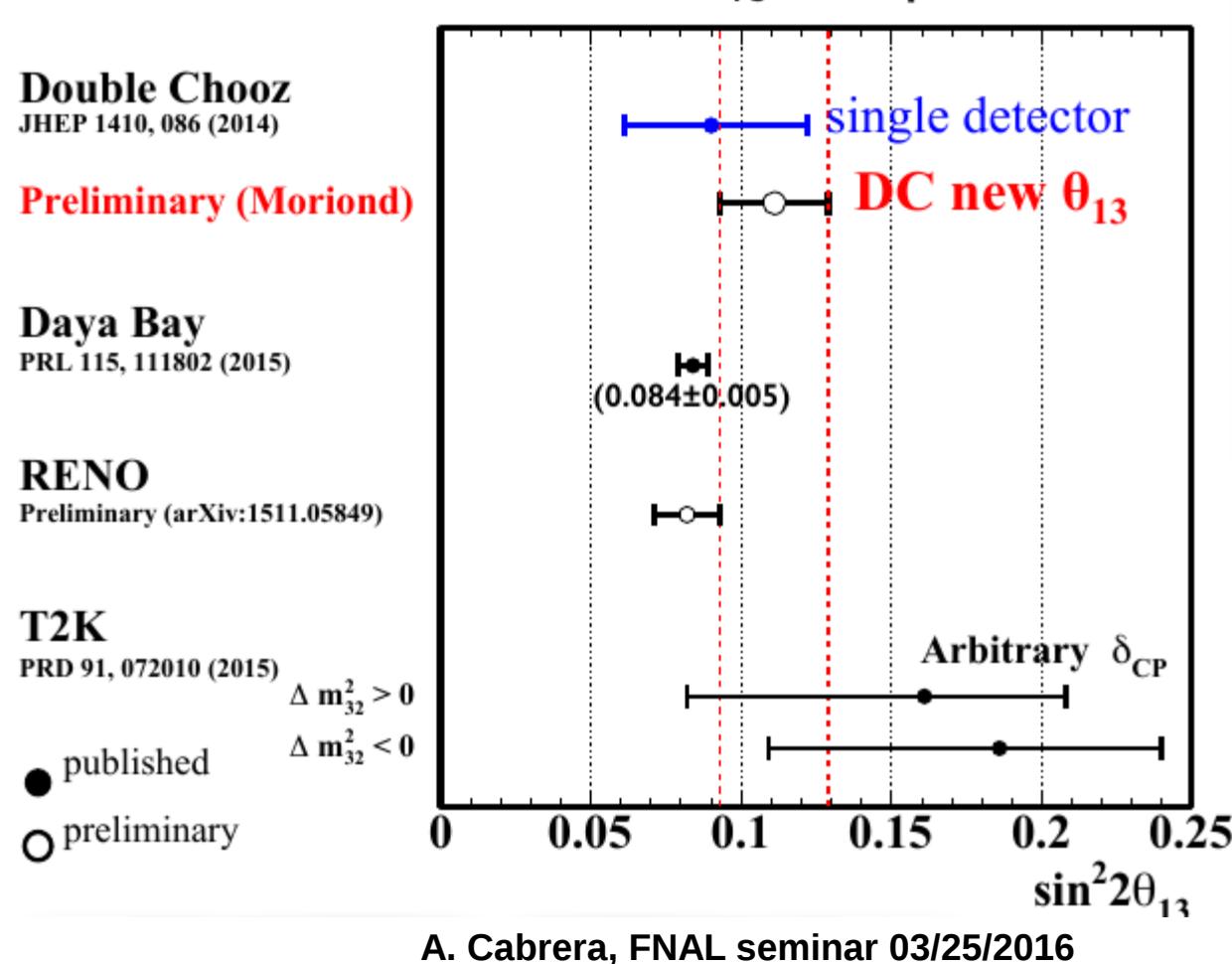
Outer Detector:

- **Inner Veto:** steel (10 mm) vessel supporting **78 8"** **PMTs**, with 90 m³ of **liquid scintillator**.
- **Shielding:** 15 cm **steel**.
- **Outer Veto:** **plastic scintillator** strips.



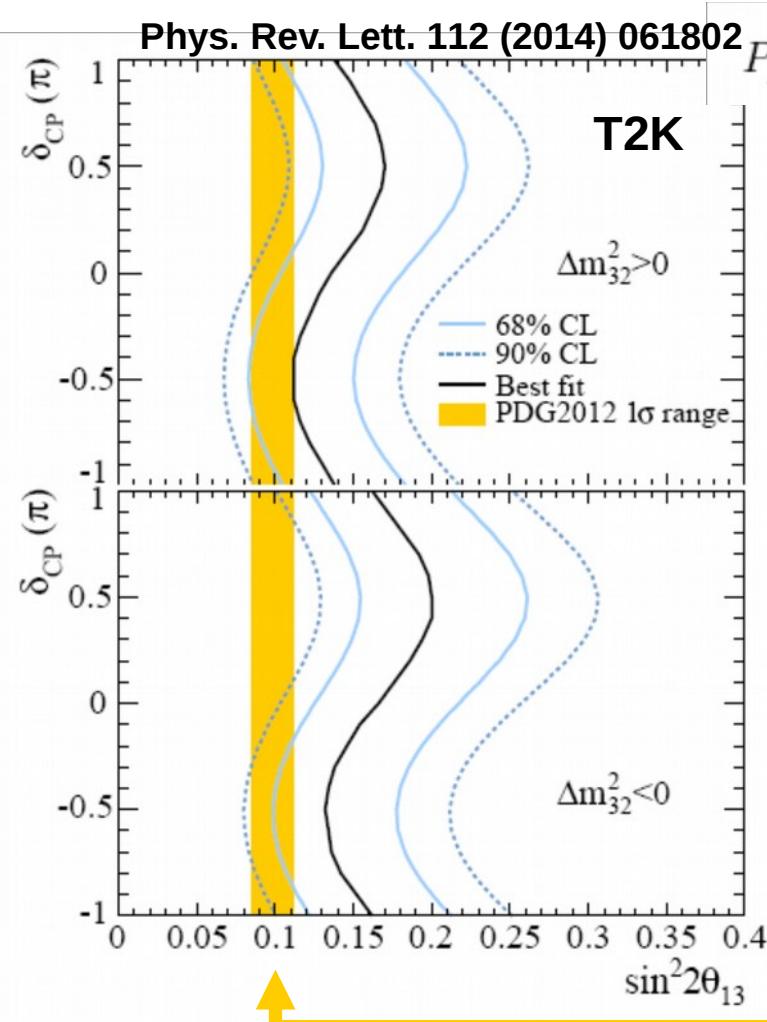
Latests measurements of θ_{13}

θ_{13} unknown until 2011. Huge progress in a few years.



First glimpse of δ

- $\nu_\mu \rightarrow \nu_e$ depends on the mass hierarchy and CP-violating phase.



$$\begin{aligned}
P_{\mu e}(L, E) = & \frac{1}{(A-1)^2} \sin^2(2\theta_{13}) \sin^2(\theta_{23}) \sin^2[(A-1)\Delta] \\
& \mp \frac{\alpha}{A(1-A)} \cos(\theta_{13}) \sin(2\theta_{12}) \sin(2\theta_{23}) \sin(2\theta_{13}) \times \\
& \times \underline{\sin(\delta)} \sin(\Delta) \sin(A\Delta) \sin[(1-A)\Delta] \\
& + \frac{\alpha}{A(1-A)} \cos(\theta_{13}) \sin(2\theta_{12}) \sin(2\theta_{23}) \sin(2\theta_{13}) \times \\
& \times \underline{\cos(\delta)} \cos(\Delta) \sin(A\Delta) \sin[(1-A)\Delta] \\
& + \frac{\alpha^2}{A^2} \cos^2(\theta_{23}) \sin^2(2\theta_{12}) \sin^2(A\Delta),
\end{aligned}$$

$$\alpha \equiv \Delta m_{21}^2 / \Delta m_{32}^2$$

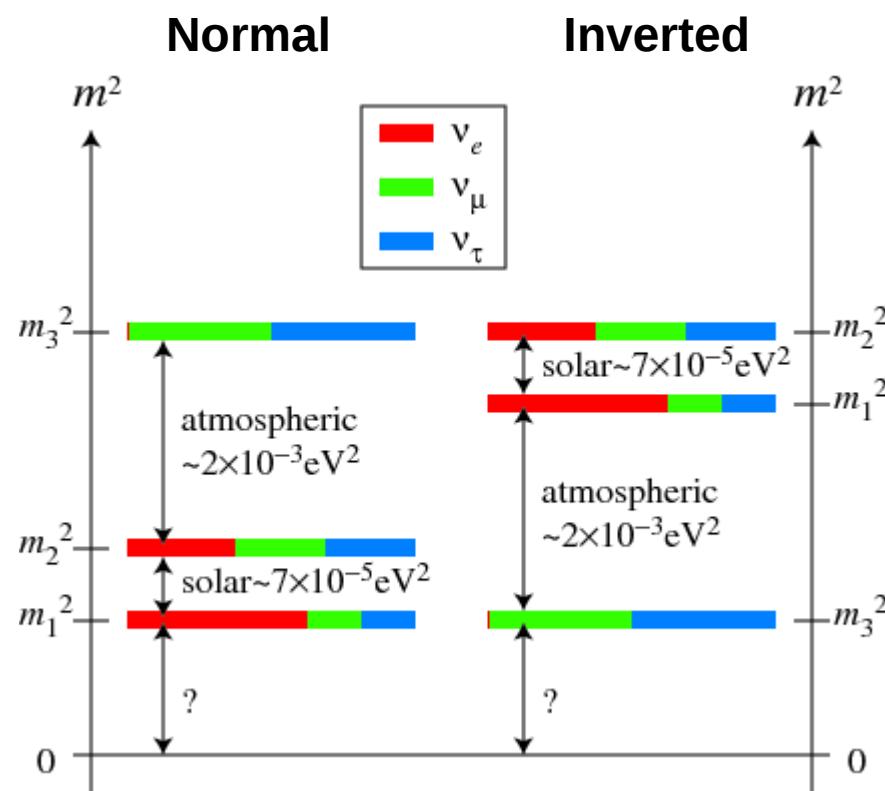
$$\Delta \equiv \frac{\Delta m_{32}^2 L}{4E}$$

$$A \equiv 2\sqrt{2}G_F N_e \frac{E}{\Delta m_{32}^2}$$

Critical input: Using the θ_{13} from the reactor experiments, the mass hierarchy and the CP-violating phase can be studied.

3 neutrinos: mass hierarchy

- 2 squared-mass differences
- But which is on top of which?
- The Solar + KamLAND experiments show that the mass eigenstate ν_2 is heavier than ν_1 .
- Which is the **lightest neutrino**? Two possibilities left:



Future: δ and mass hierarchy

- Both CP-violating phase and the mass hierarchy can be measured in a long-baseline accelerator experiment.
- Need a long baseline and a broad-energy beam to disentangle CP violation caused by matter effects (Earth is made only from matter) from the intrinsic CP violation.

