

Particle Physics: Neutrinos – part I

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Week 8: March 25, 2017
Columbia University Science Honors Program



Course Policies

Attendance

Up to four absences

Send email notifications of all absences to
shpattendance@columbia.edu.

Please, no cell phones

Please, ask questions!

Lecture materials

<https://twiki.nevis.columbia.edu/twiki/bin/view/Main/ScienceHonorsProgram>

Schedule

1. ~~Introduction (Inês)~~
2. ~~History of Particle Physics (José)~~
3. ~~Special Relativity (José)~~
4. ~~Quantum Mechanics (Inês)~~
5. ~~Experimental Methods (Cris)~~
6. ~~The Standard Model – Overview (Cris)~~
7. ~~The Standard Model – Limitations (Cris)~~
- 8. Neutrinos – part I (José)**
- 9. Neutrinos – part II (José)**
10. LHC and Experiments (Inês)
11. The Higgs Boson and Beyond (Inês)
12. Particle Cosmology (Cris)

Neutrinos in the Standard Model

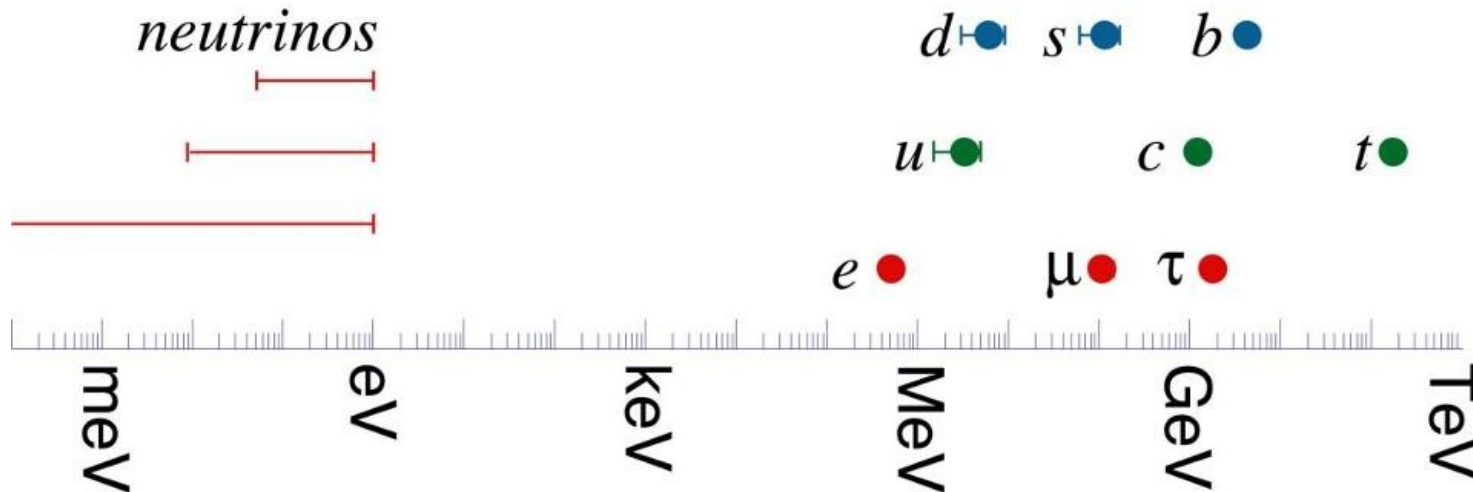
Three Generations
of Matter (Fermions) spin $\frac{1}{2}$

	I	II	III
mass →	2.4 MeV	1.27 GeV	171.2 GeV
charge →	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$
name →	Left u up Right	Left c charm Right	Left t top Right
Quarks	4.8 MeV	104 MeV	4.2 GeV
	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$
	Left d down Right	Left s strange Right	Left b bottom Right
	0 eV	0 eV	0 eV
	Left ν_e electron neutrino Right	Left ν_μ muon neutrino Right	Left ν_τ tau neutrino Right
Leptons	0.511 MeV	105.7 MeV	1.777 GeV
	-1	-1	-1
	Left e electron Right	Left μ muon Right	Left τ tau Right

0	0	g	gluon
0	0	γ	photon
91.2 GeV	0	Z	weak force
80.4 GeV	± 1	W$^\pm$	weak force

Bosons (Forces) spin 1

- Only left-handed neutrinos (and right-handed antineutrinos) in the Standard Model.
- Initially implemented as massless particles.
 - Neutrino oscillations** show neutrinos have mass!
- Why neutrino masses are so different from the other fermions?
 - Are neutrinos acquiring mass through the same mechanism (Higgs) or from something else?



Neutrino oscillations (2-neutrino example)

- Consequence of neutrino mixing (quantum superposition, as in Schrödinger's cat): the neutrinos that interact are not the same as the neutrinos that propagate.

- Two flavor approximation:

Flavor eigenstates

Mass eigenstates

$$\begin{pmatrix} |\nu_l\rangle \\ |\nu_x\rangle \end{pmatrix} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} |\nu_1\rangle \\ |\nu_2\rangle \end{pmatrix}$$

- Transition** probability (derivation in blackboard):

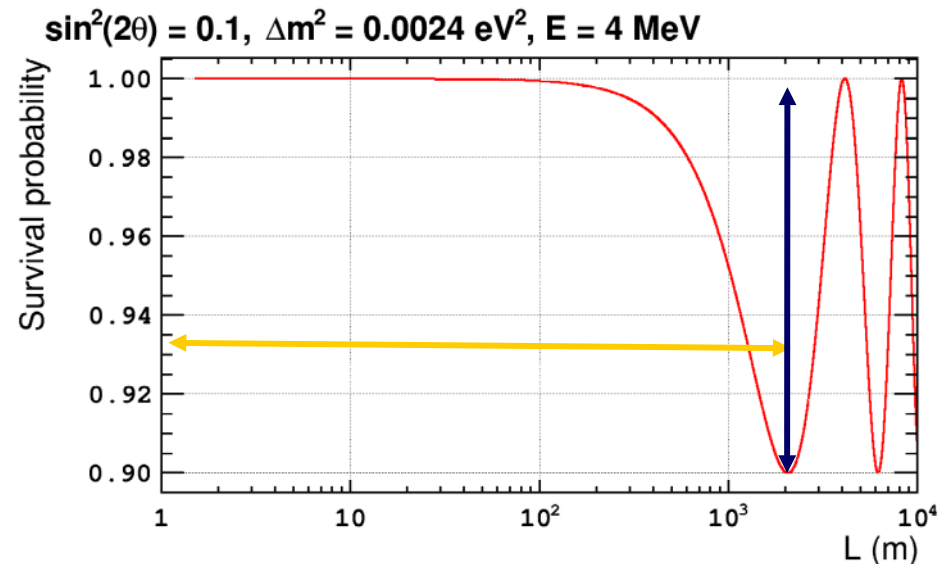
$$P_{lx(l \neq x)}^{2\nu}(L, E) = \boxed{\sin^2(2\theta)} \sin^2\left(\frac{\boxed{\Delta m^2 L}}{\boxed{4E}}\right)$$

Controlled by the experiment

- Survival** probability:

$$P_{ll}^{2\nu}(L, E) = 1 - P_{lx(l \neq x)}(L, E)$$

- Neutrino oscillation** implies **neutrinos are massive** and non-degenerated.



3 neutrino mixing

- **Flavor eigenstates** (ν_e, ν_μ, ν_τ) \neq **mass eigenstates** (ν_1, ν_2, ν_3).
- Related by **Pontecorvo-Maki-Nakagawa-Sakata mixing matrix**:
3 neutrinos \rightarrow 3 angles ($\theta_{12}, \theta_{23}, \theta_{13}$) + 1 CP-violating phase (δ).

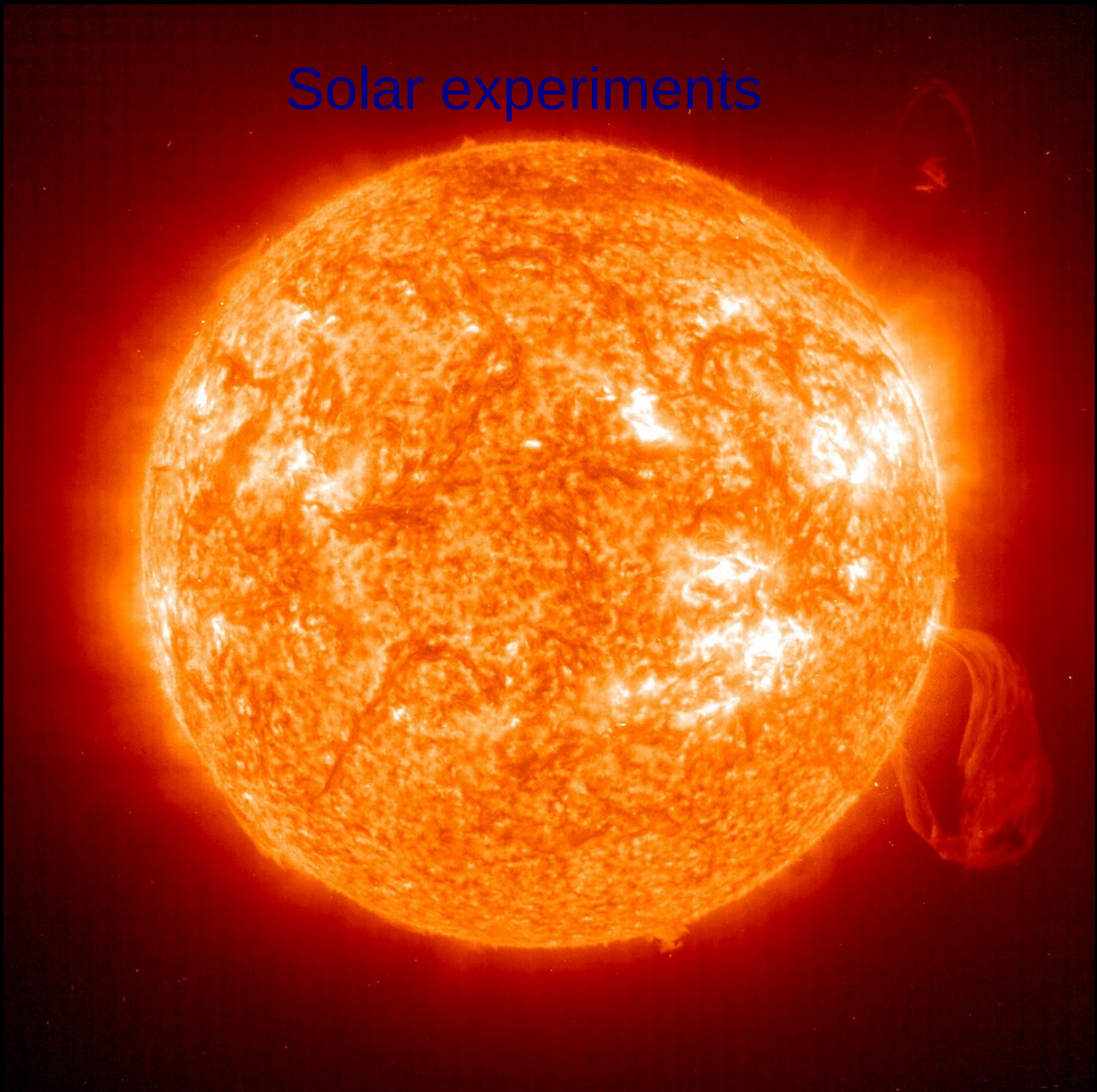
PMNS matrix: U $c_{ij} = \cos \theta_{ij}, s_{ij} = \sin \theta_{ij}$

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \underbrace{\begin{pmatrix} 1 & & \\ & c_{23} & s_{23} \\ & -s_{23} & c_{23} \end{pmatrix}}_{\text{Atmospheric \& Long-baseline accelerator experiments}} \underbrace{\begin{pmatrix} c_{13} & & s_{13} e^{-i\delta} \\ & 1 & \\ -s_{13} e^{i\delta} & & c_{13} \end{pmatrix}}_{\text{Reactor \& Long-baseline accelerator experiments}} \underbrace{\begin{pmatrix} c_{12} & s_{12} \\ -s_{12} & c_{12} \\ & & 1 \end{pmatrix}}_{\text{Solar \& KamLAND experiments}} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix} \rightarrow \begin{matrix} m_1 \\ m_2 \\ m_3 \end{matrix}$$

- CP violation only possible if all three angles are not zero.

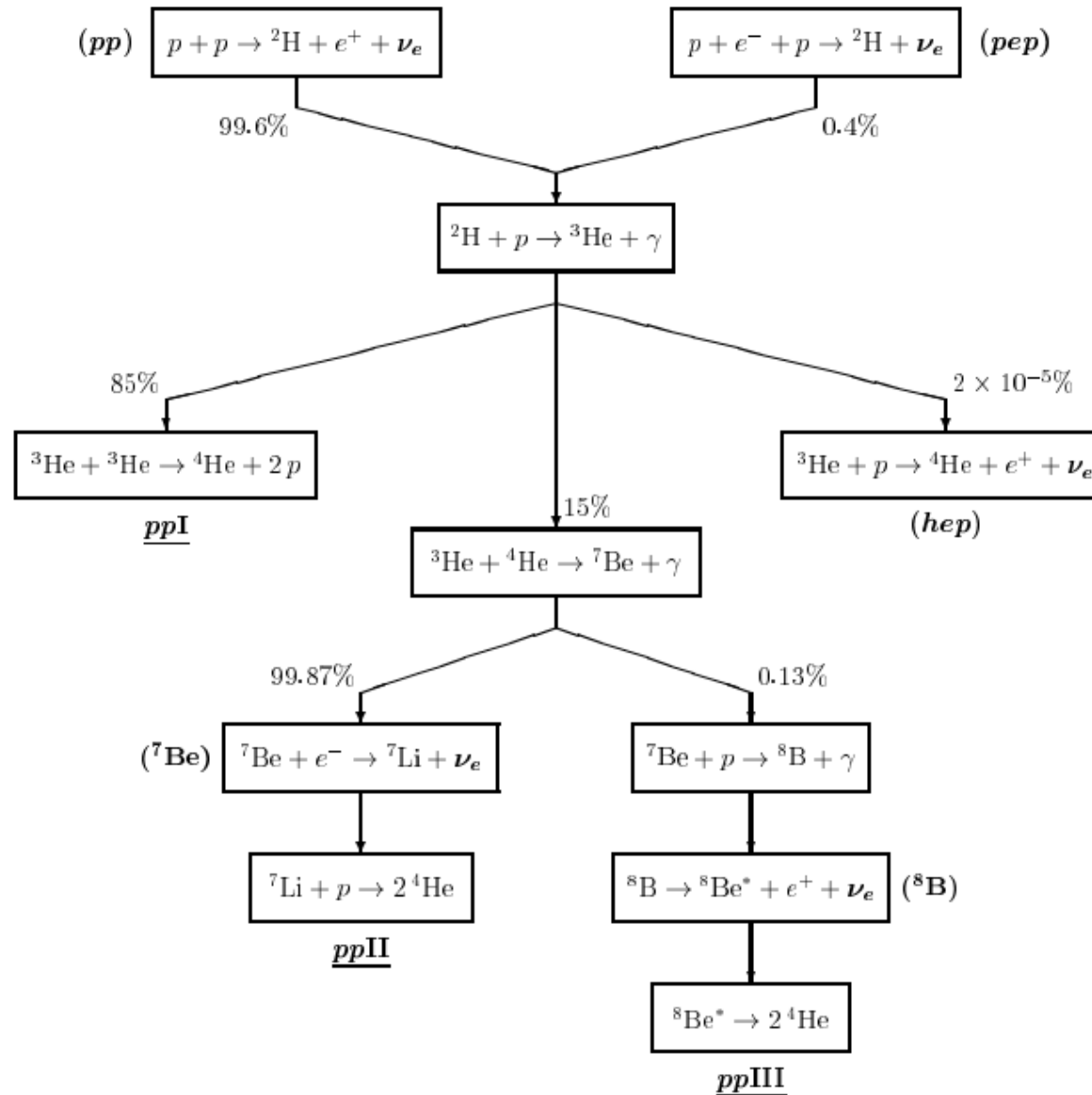
Measurement of θ_{12} and Δm^2_{21}

Solar experiments



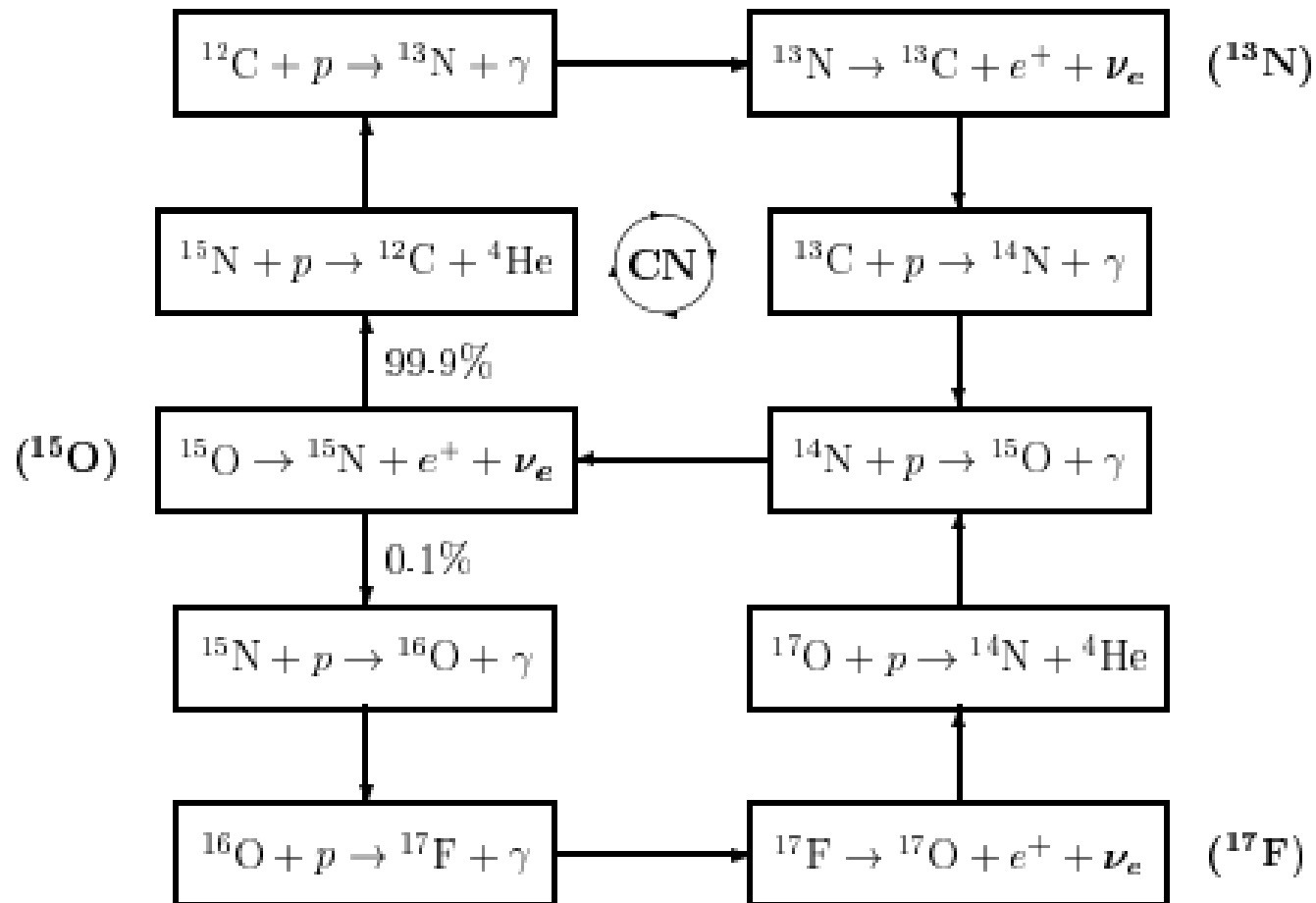
Solar neutrinos: pp chain

- 98.4% of Sun's fusion energy.

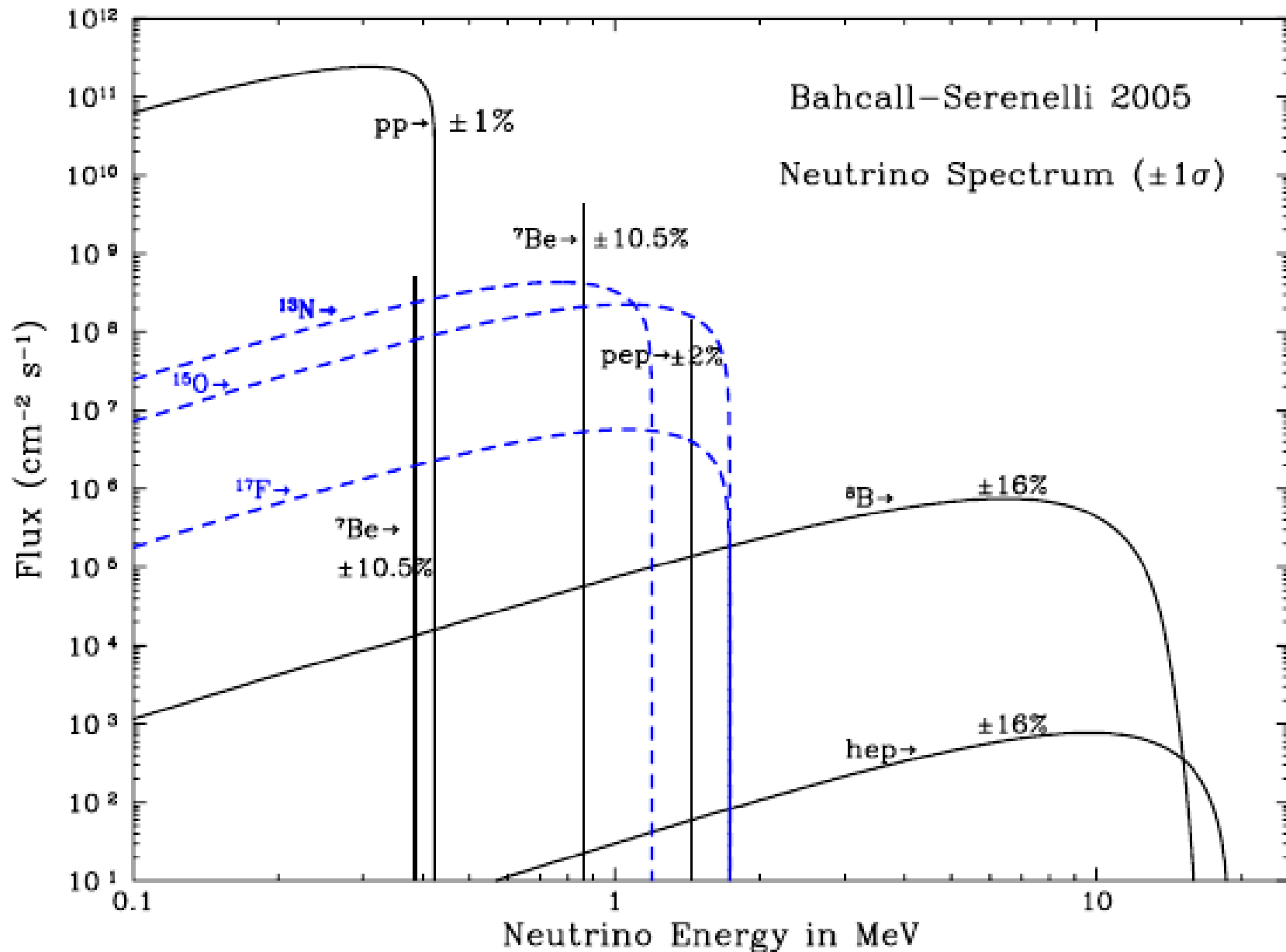


Solar neutrinos: CNO cycle

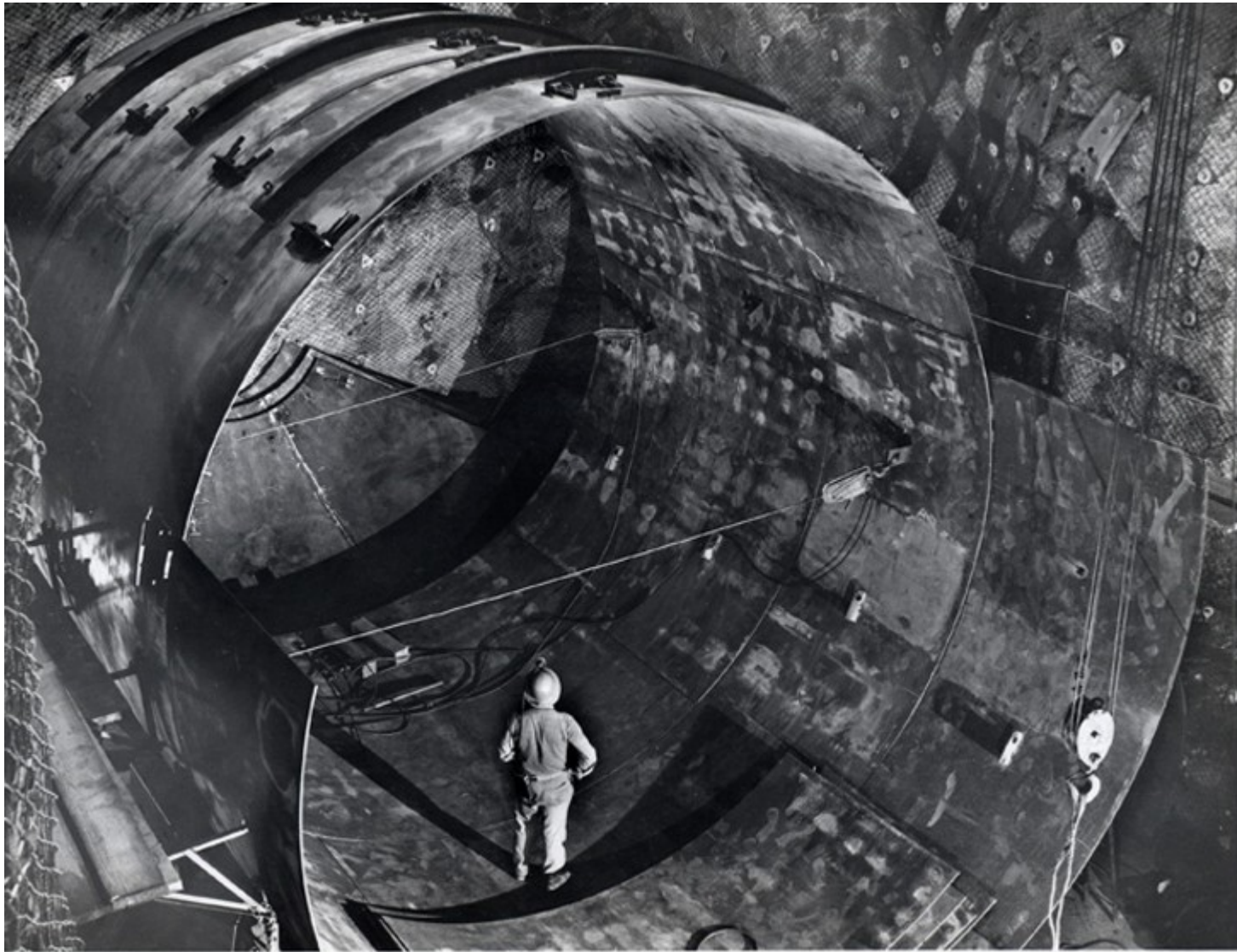
- 1.6% of Sun's fusion energy.



Solar neutrinos: energy spectrum



Homestake experiment



Homestake experiment

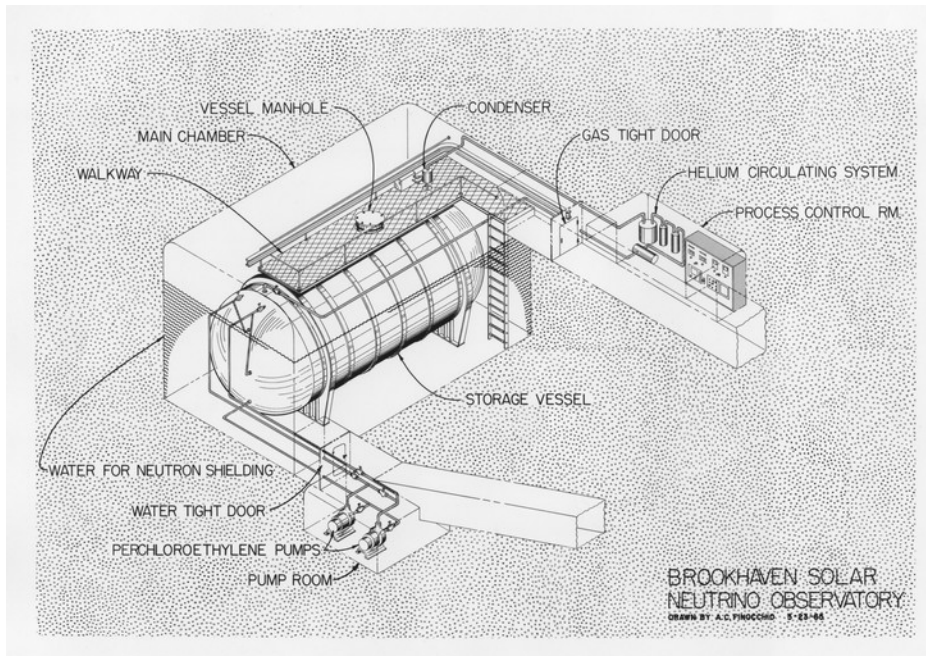
- Detection of solar neutrinos using the reaction:



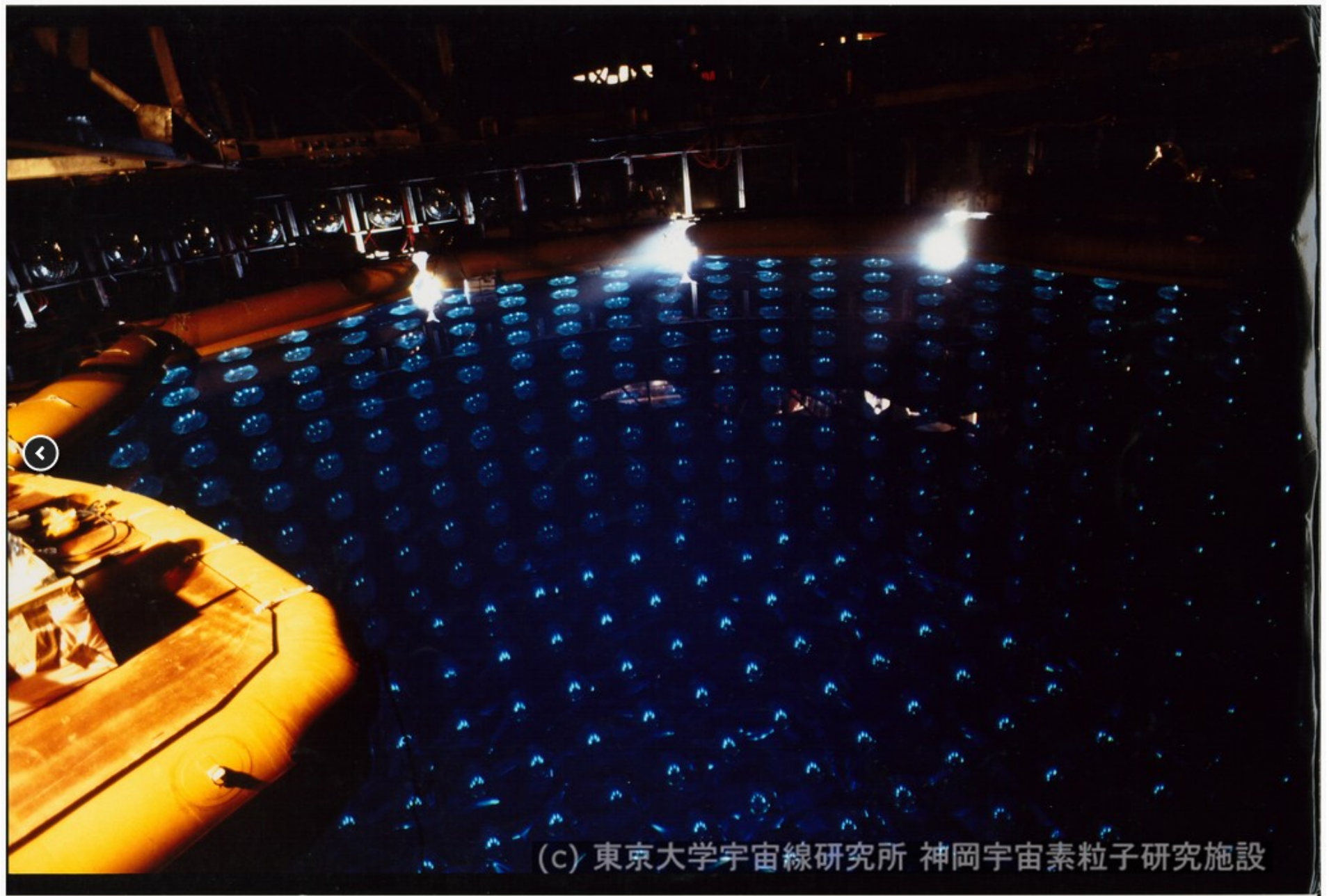
- Ratio of observed to predicted:

$$\frac{R_{\text{Cl}}}{R_{\text{SSM}}} = 0.301 \pm 0.027$$

- Missing neutrinos!



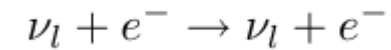
Kamiokande



(c) 東京大学宇宙線研究所 神岡宇宙素粒子研究施設

Kamiokande

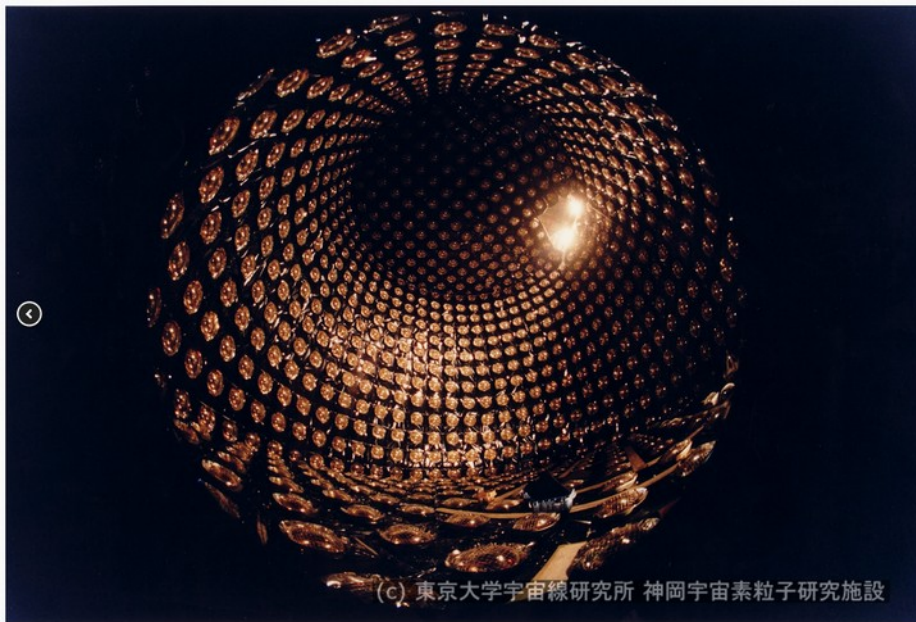
- Detection of solar neutrinos using the reaction:



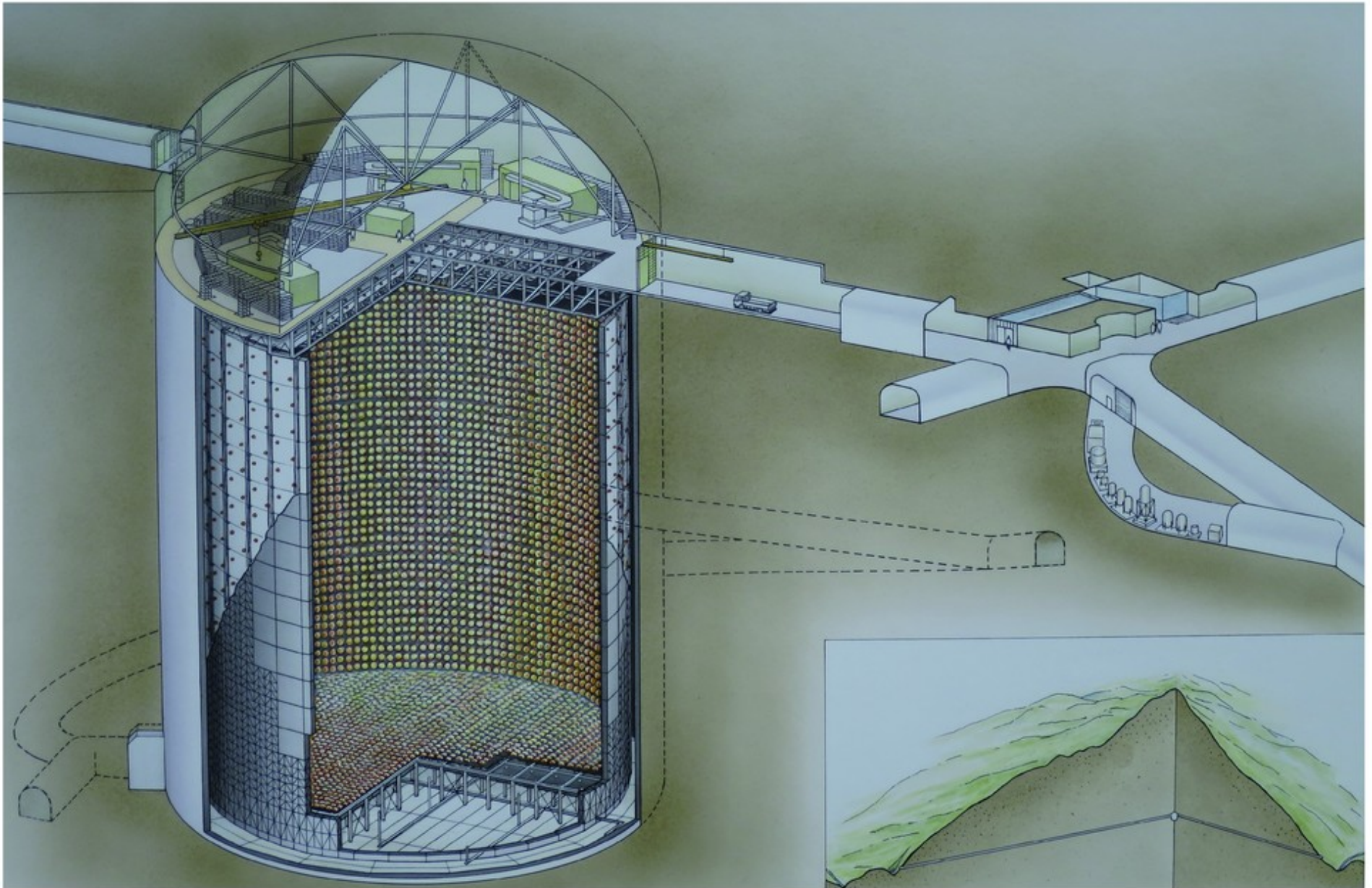
- Ratio of observed to predicted:

$$\frac{\Phi_{\text{Kamiokande}}}{\Phi_{\text{SSM}}} = 0.484 \pm 0.066.$$

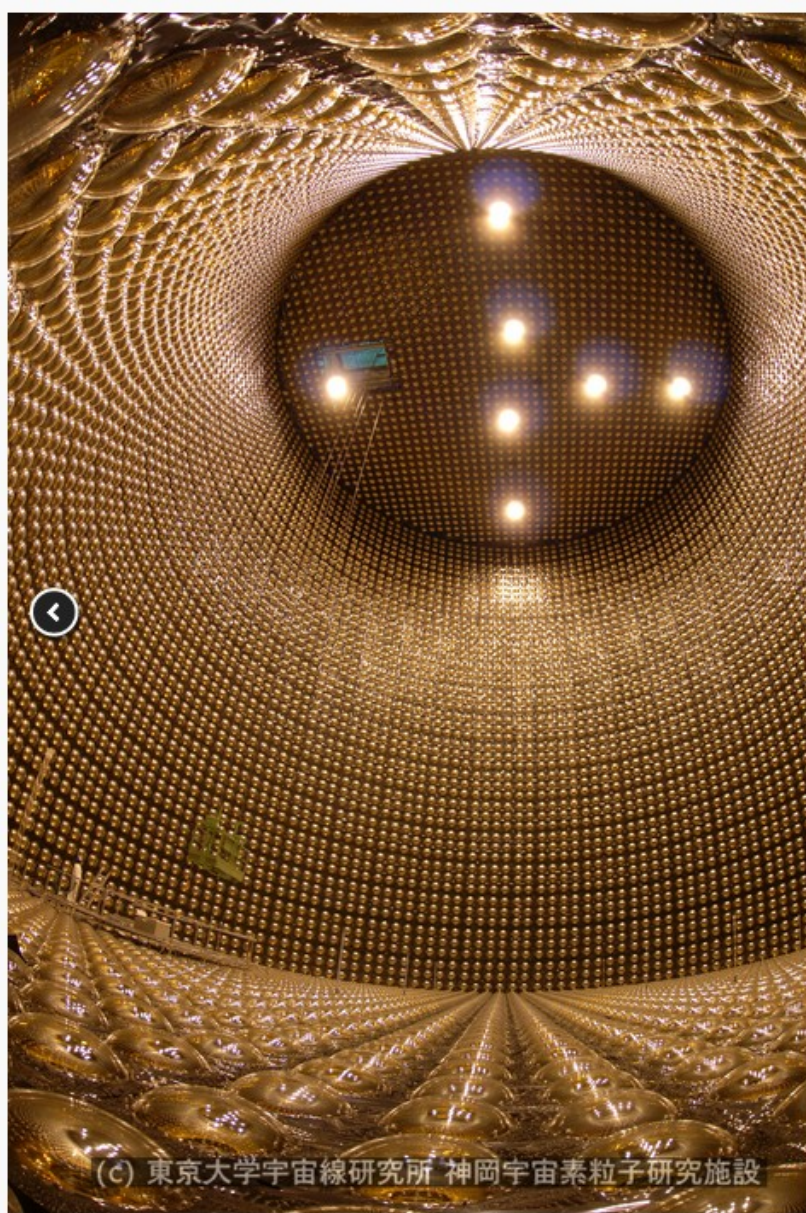
- Missing neutrinos again!



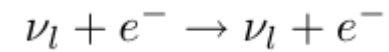
Super-Kamiokande



Super-Kamiokande



- Detection of solar neutrinos using the reaction:



- Ratio of observed to predicted:

$$\frac{\Phi_{\text{SK-I}}}{\Phi_{\text{SSM}}} = 0.406 \pm 0.014$$

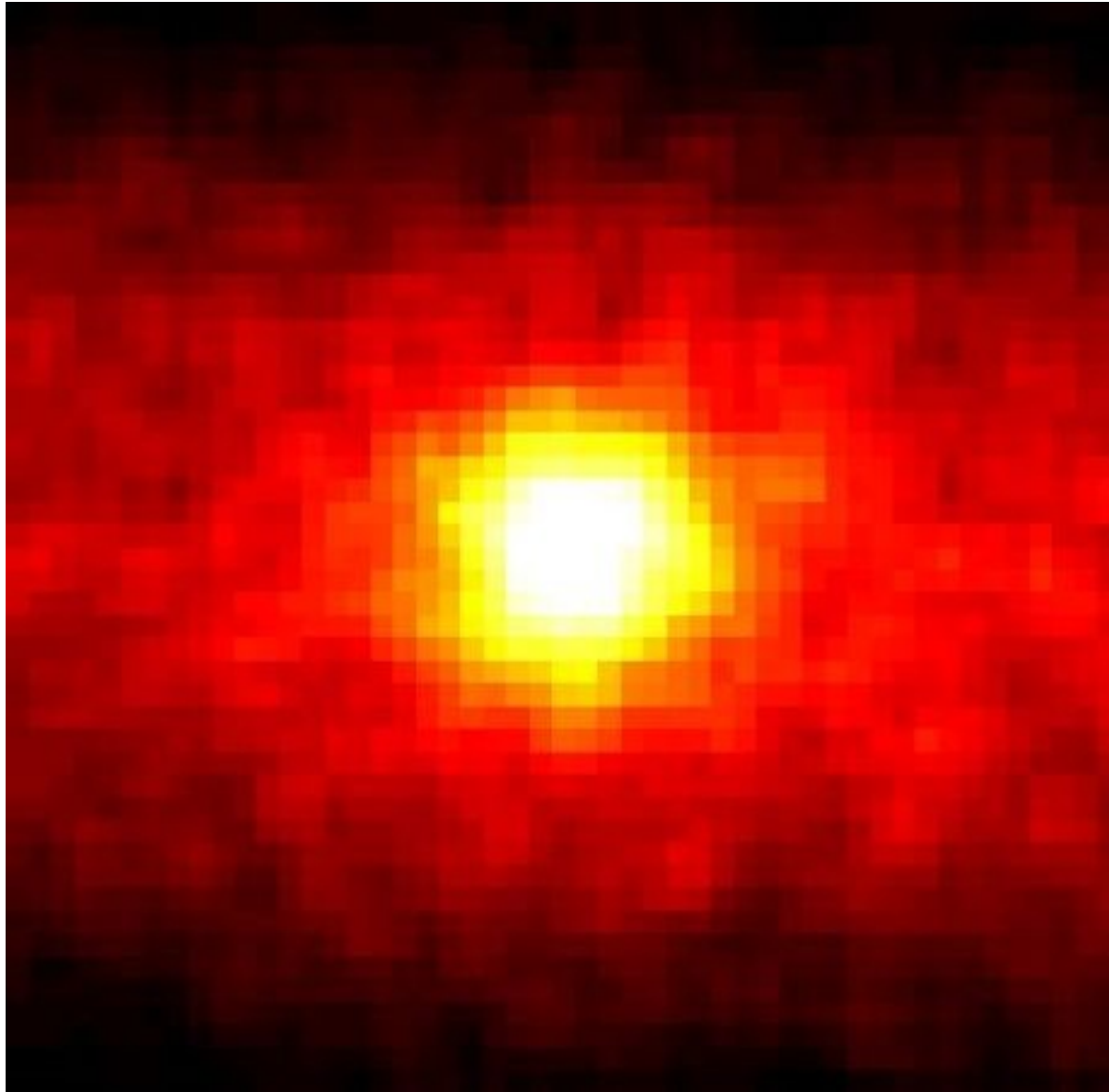
- Improved result over Kamiokande, neutrinos still missing!

Super-Kamiokande

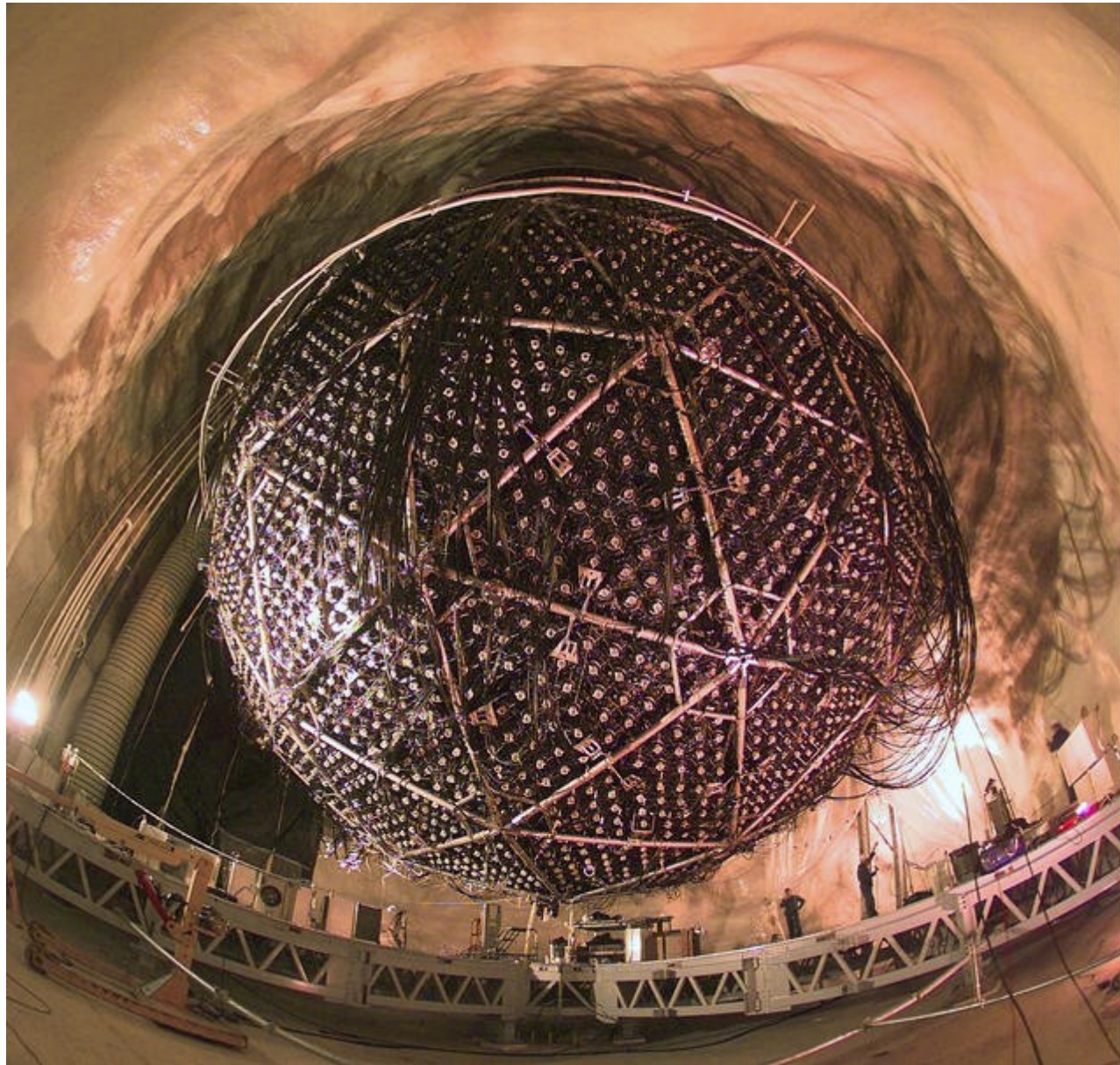


Super-Kamiokande

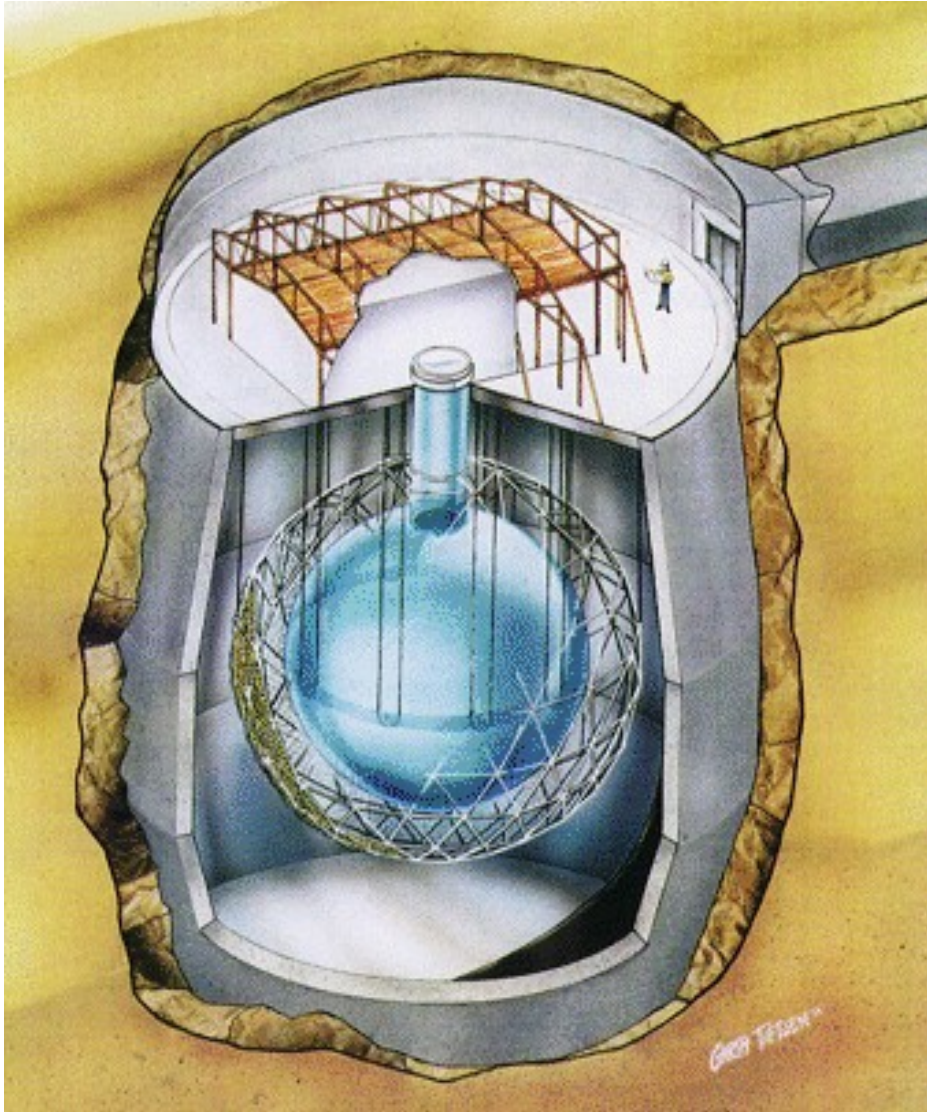
- NEUTRINOGRAPHY of the Sun. 500 days exposure!



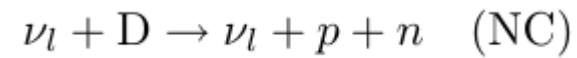
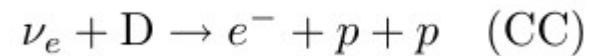
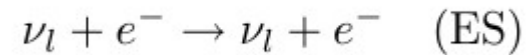
SNO



SNO



- Detection of solar neutrinos using the reaction:



- Ratio of observed to predicted:

$$\frac{\Phi_{\text{SNO}}^{\text{ES}}}{\Phi_{\text{SSM}}} = 0.406 \pm 0.046$$

$$\frac{\Phi_{\text{SNO}}^{\text{CC}}}{\Phi_{\text{SSM}}} = 0.290 \pm 0.017$$

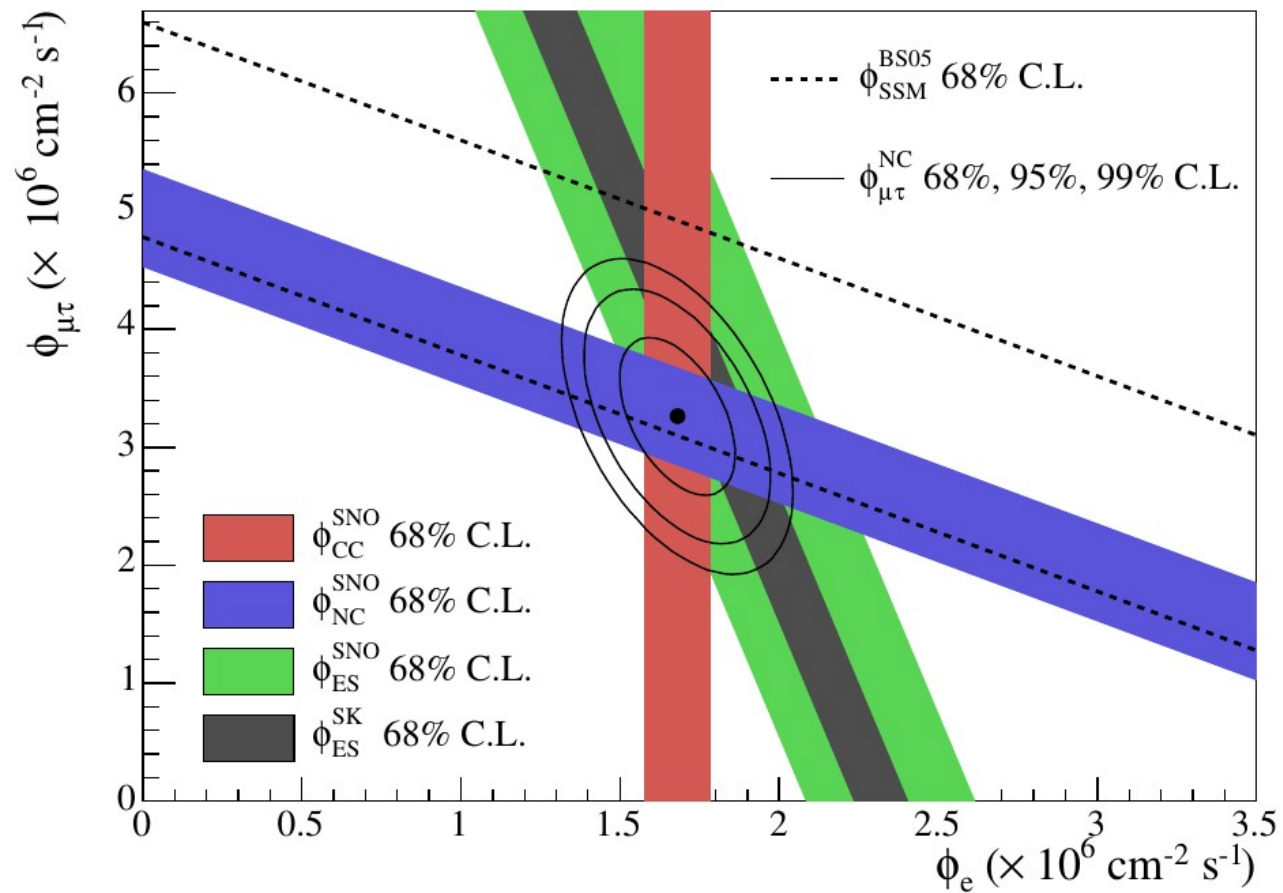
$$\frac{\Phi_{\text{SNO}}^{\text{NC}}}{\Phi_{\text{SSM}}} = 0.853 \pm 0.075$$

SNO

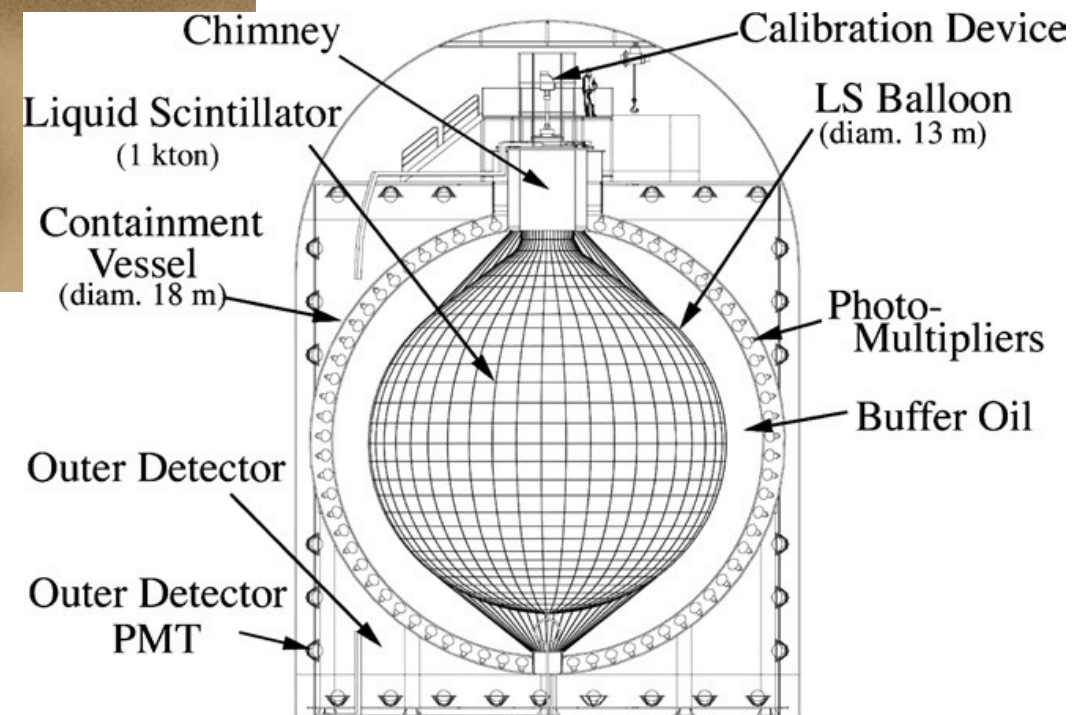
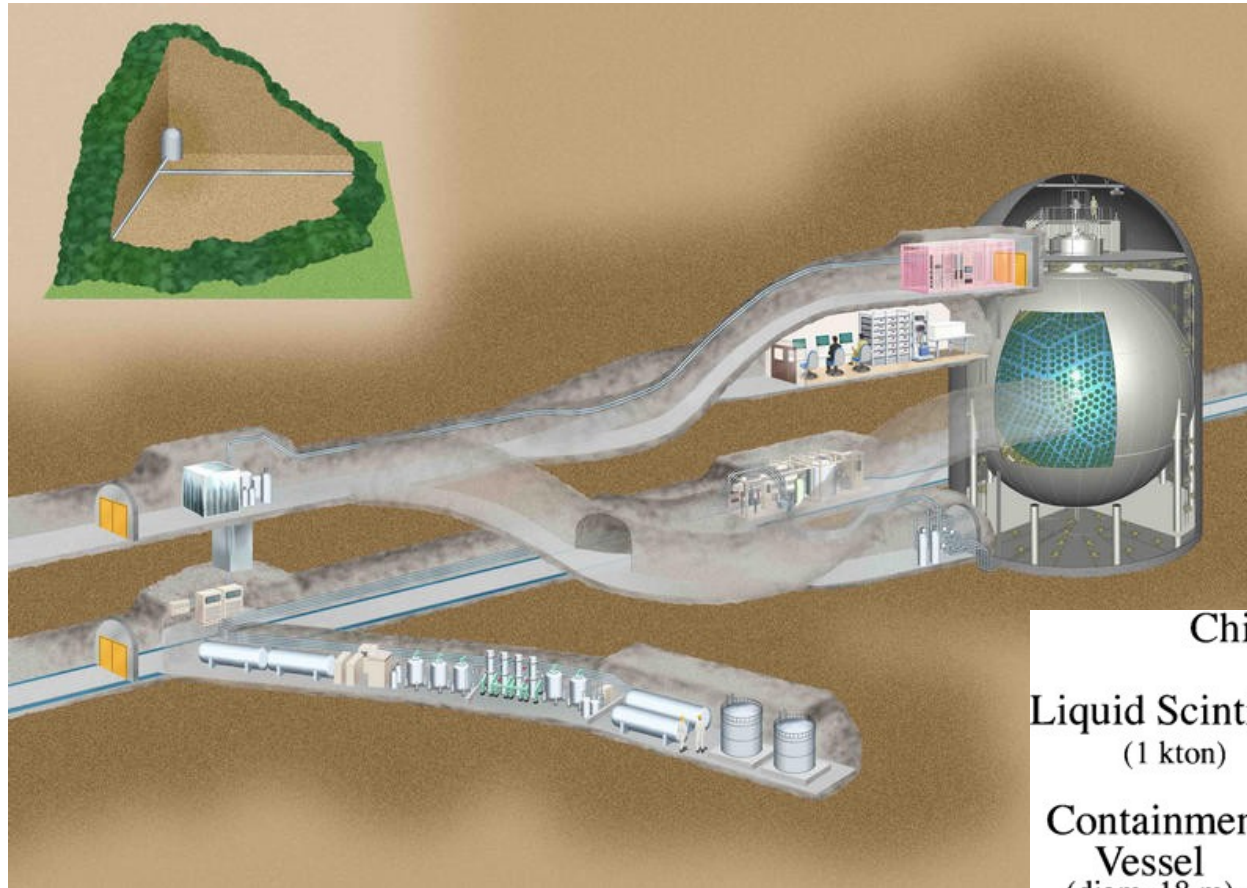
$$\Phi_{\text{SNO}}^{\nu_e} + r^{\text{ES}} \Phi_{\text{SNO}}^{\nu_{\mu,\tau}} = \Phi_{\text{SNO}}^{\text{ES}} \quad \underline{r^{\text{ES}}} \equiv \sigma_{\nu_{\mu,\tau}}^{\text{ES}} / \sigma_{\nu_e}^{\text{ES}} \approx 0.1553.$$

$$\Phi_{\text{SNO}}^{\nu_e} = \Phi_{\text{SNO}}^{\text{CC}}$$

$$\Phi_{\text{SNO}}^{\nu_e} + \Phi_{\text{SNO}}^{\nu_{\mu,\tau}} = \Phi_{\text{SNO}}^{\text{NC}}$$

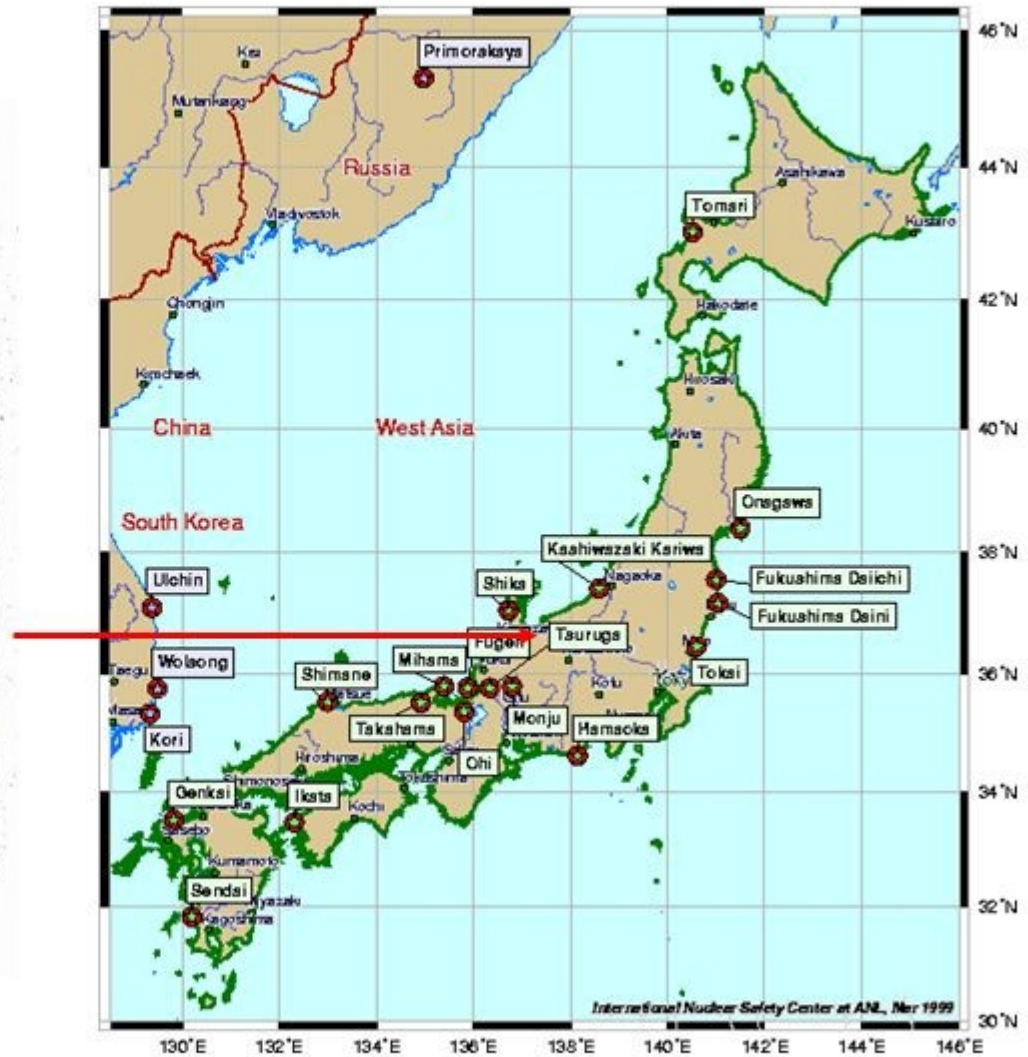
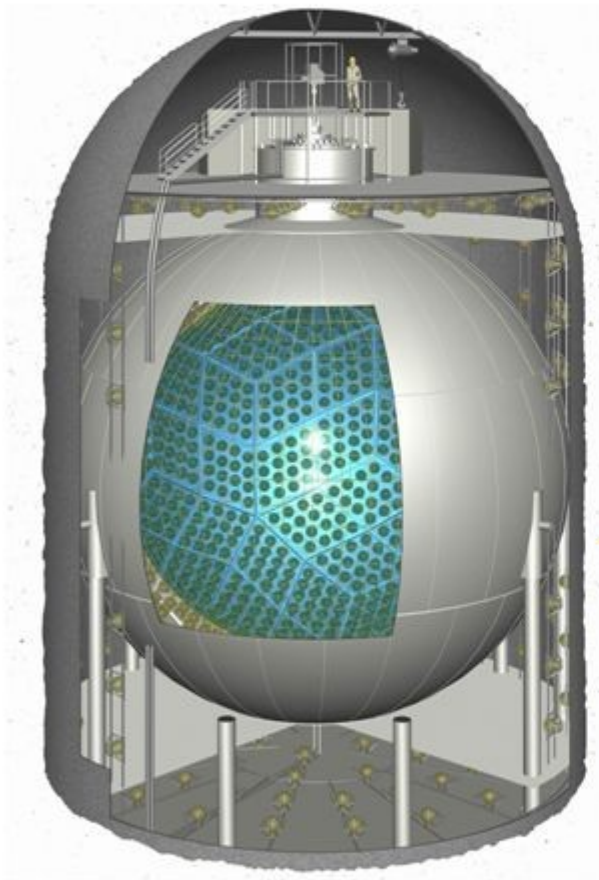


KamLAND





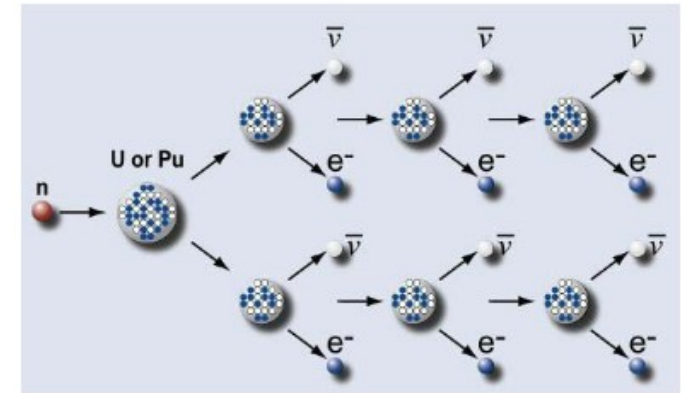
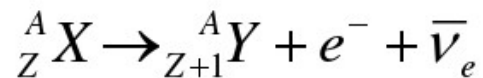
KamLAND



$\bar{\nu}_e$ production at nuclear reactors

- Fission of nuclear fuel (^{235}U , ^{238}U , ^{239}Pu , ^{241}Pu) produces neutron rich fission products.

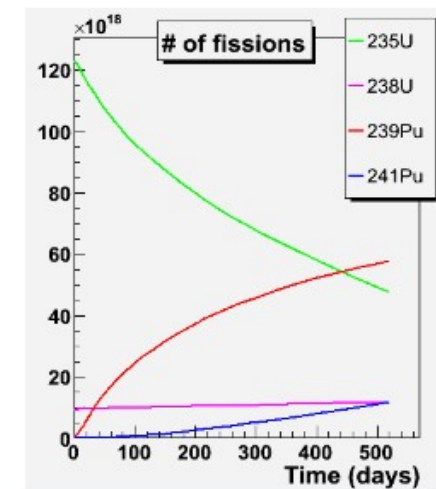
- β^- decay of fission products:



- Average per fission:

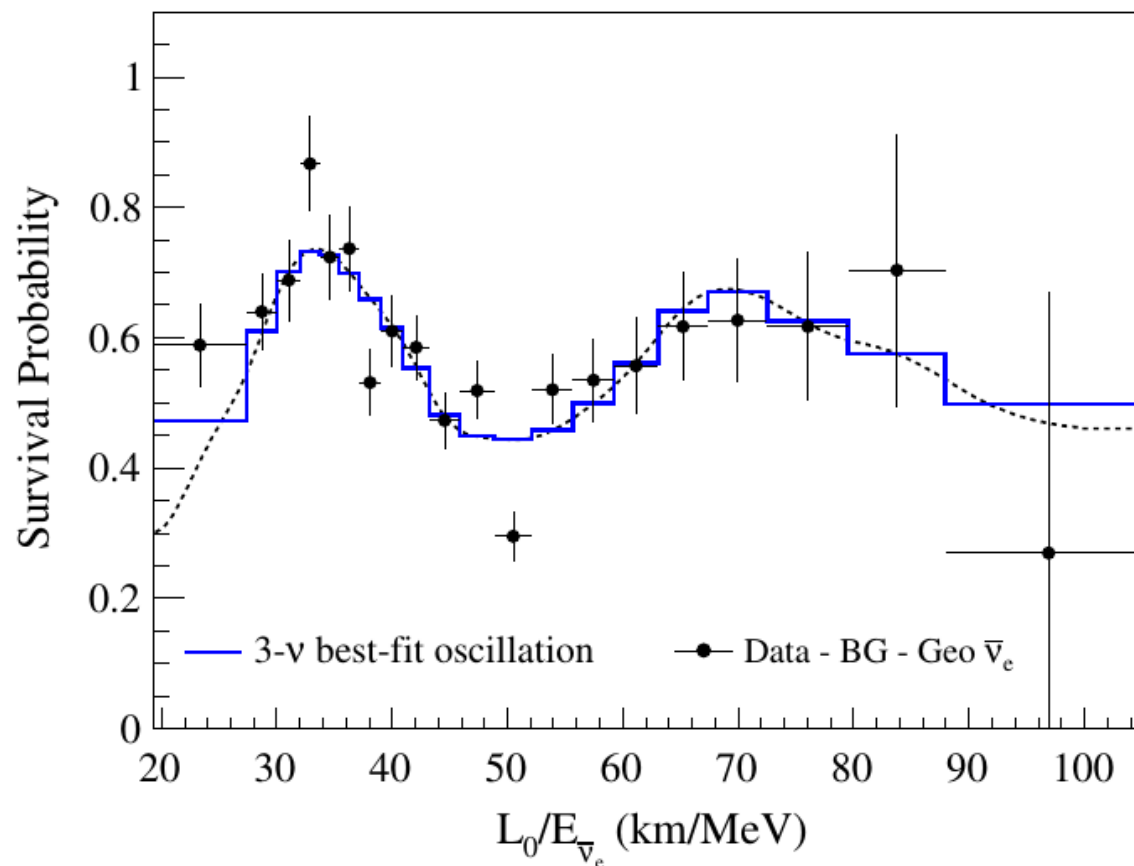
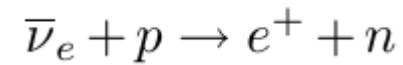
- 200 MeV released.
- 6 antineutrinos.

- Nuclear power plants: greatest man-made antineutrino source.
- Need to consider nuclear fuel evolution.

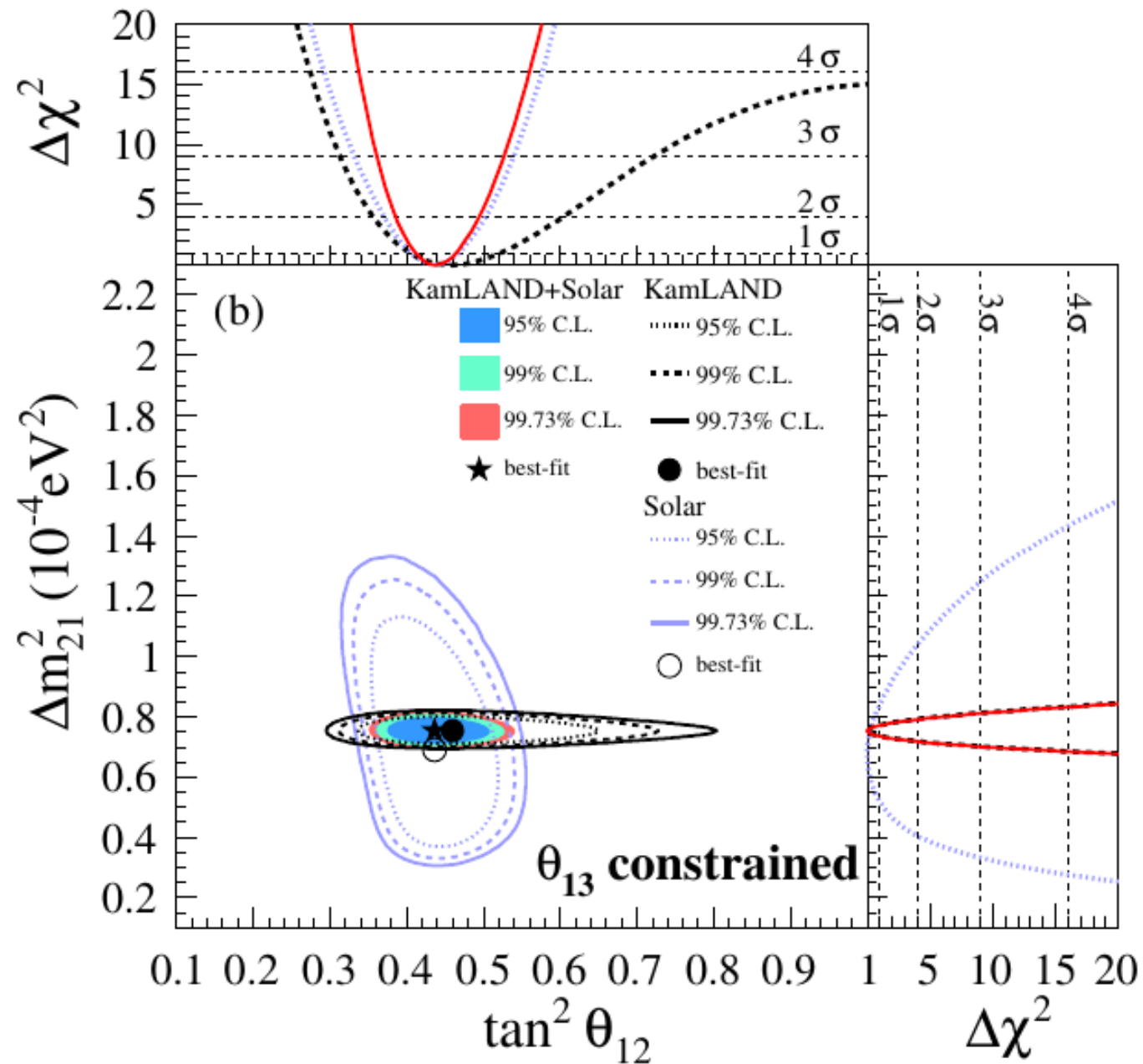


KamLAND

- Detection of reactor neutrinos using the inverse beta-decay reaction:

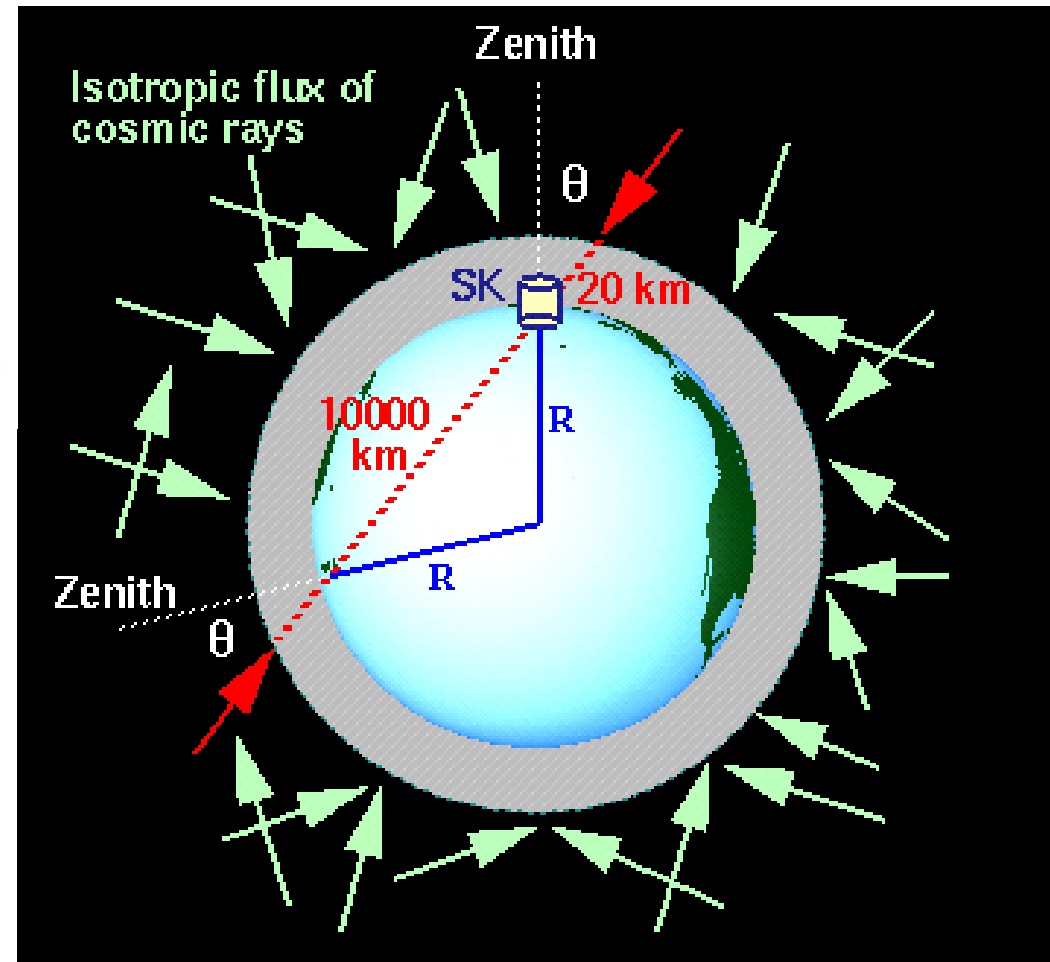
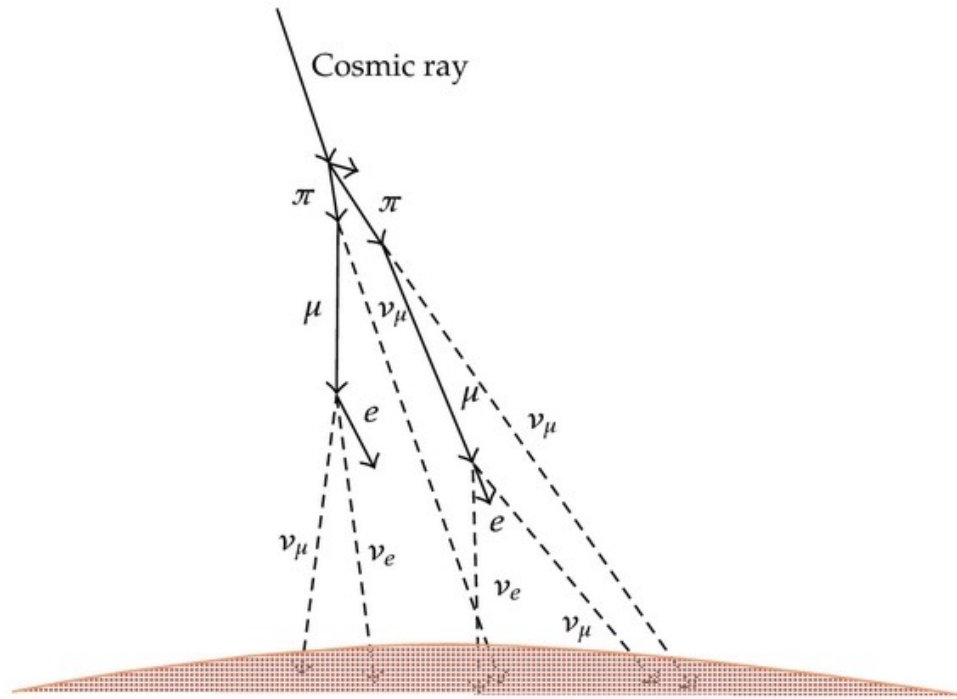


Solar + KamLAND results

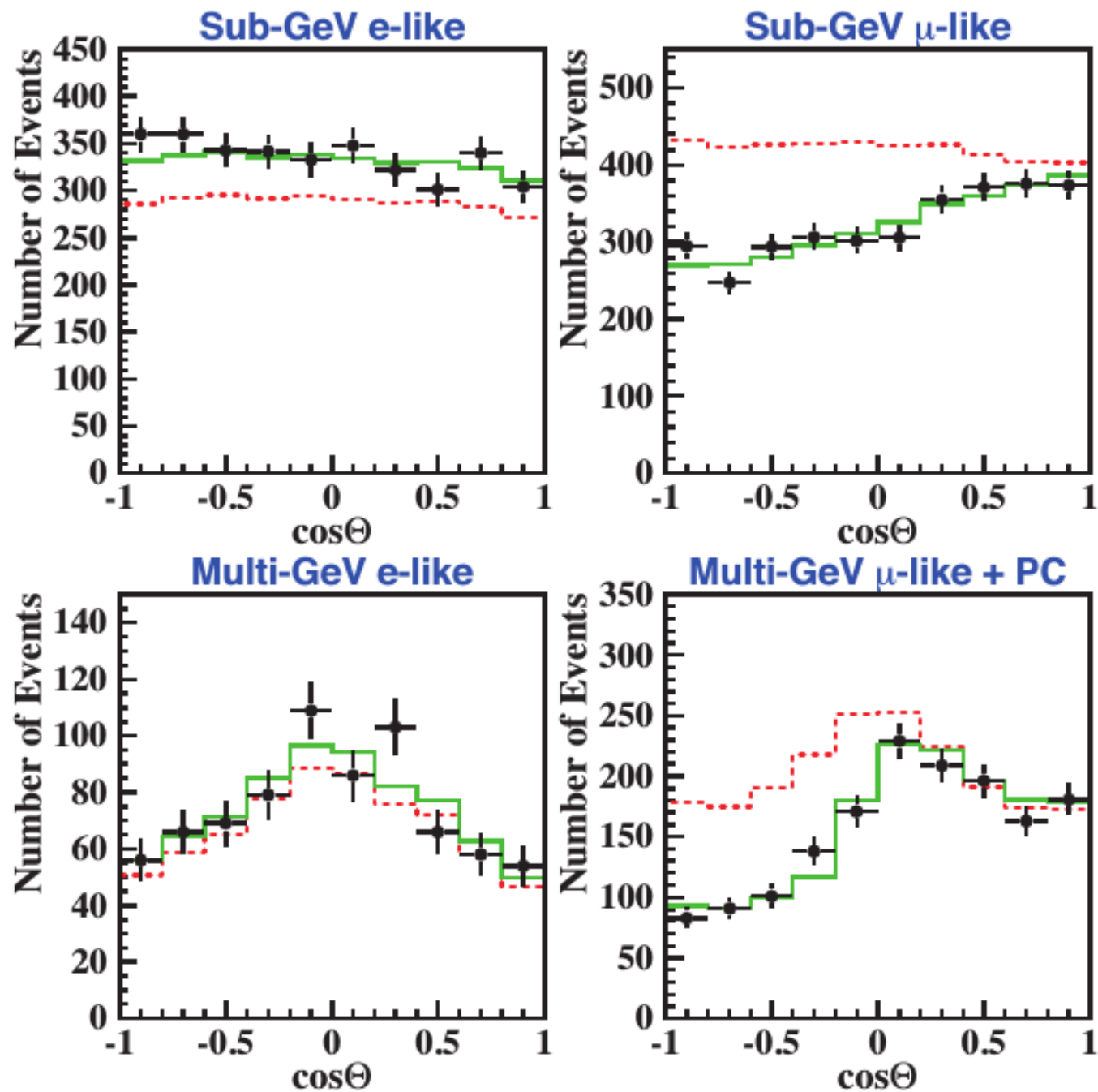
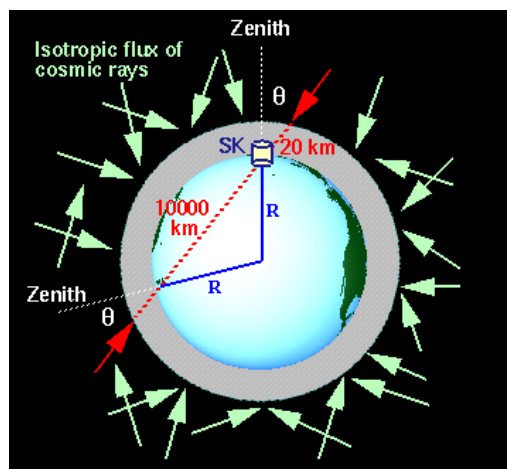


Measurement of θ_{23} and Δm^2_{atm}

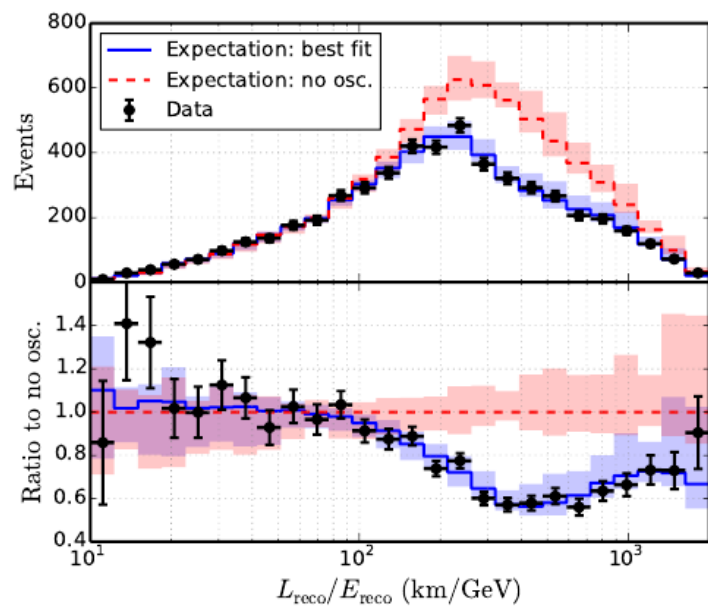
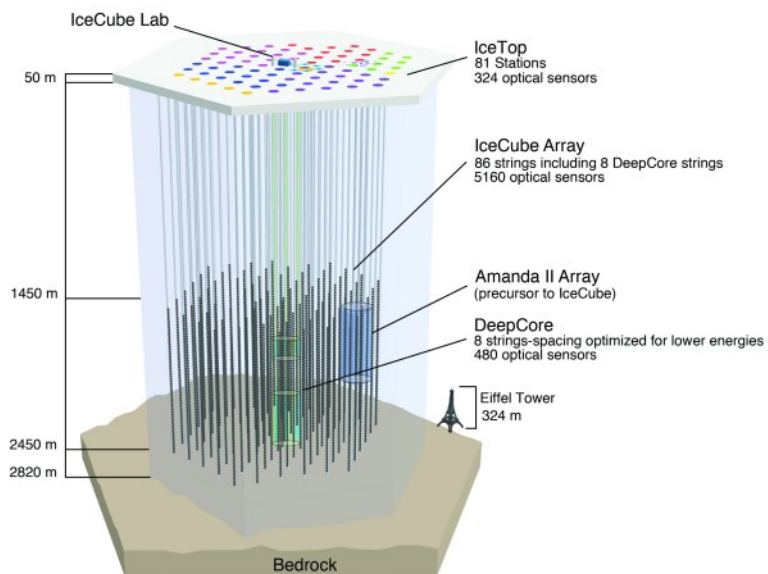
Atmospheric neutrinos



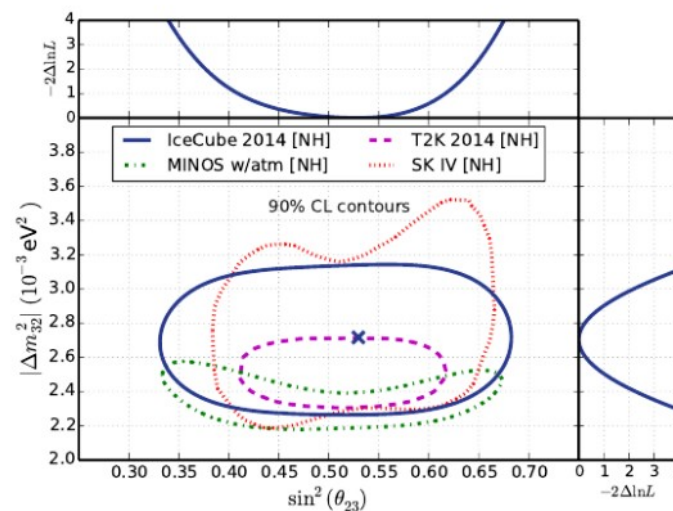
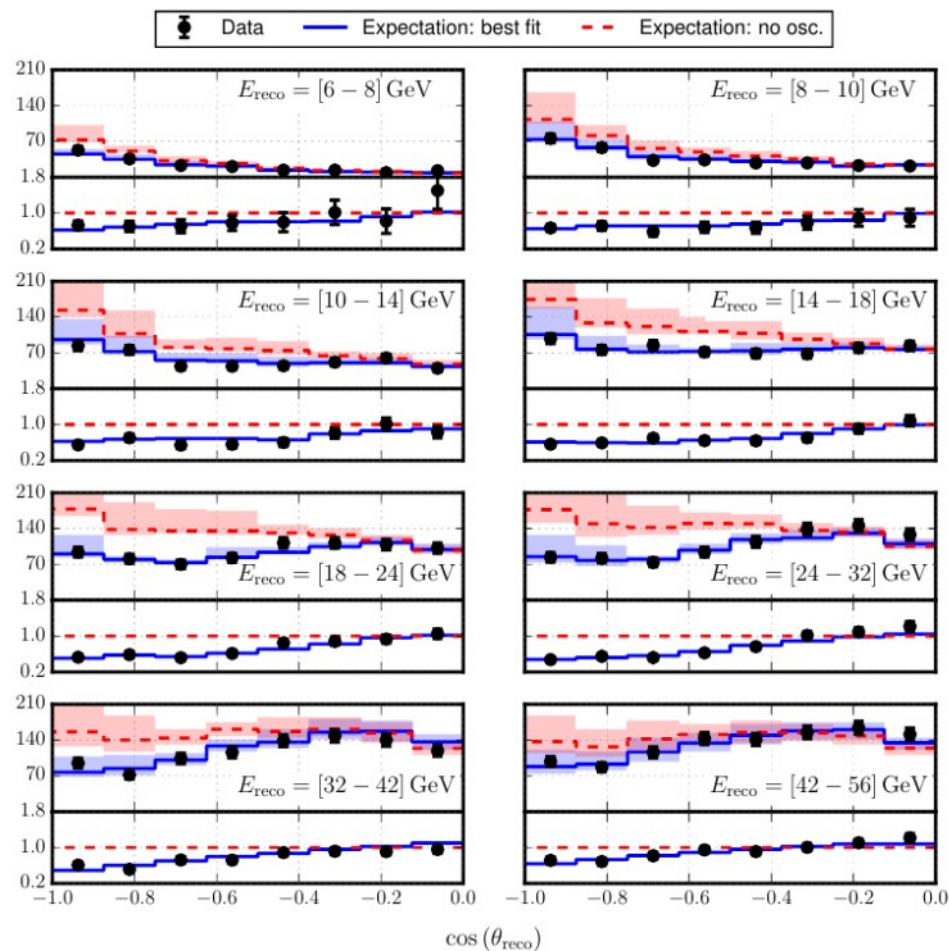
Super-Kamiokande results



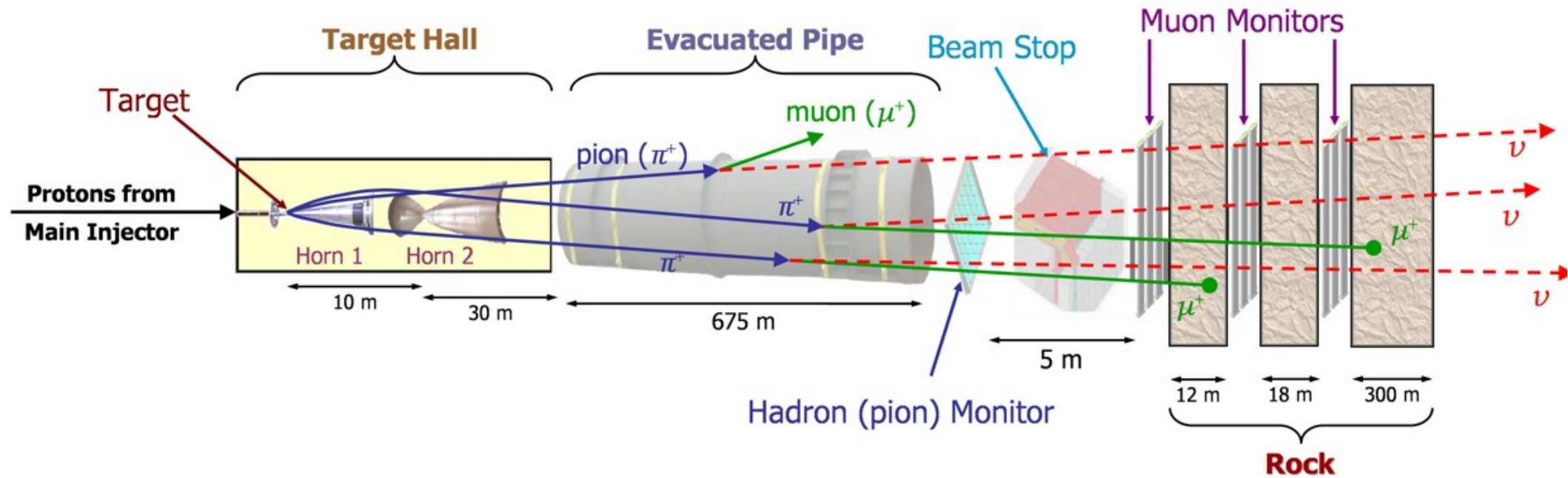
IceCube



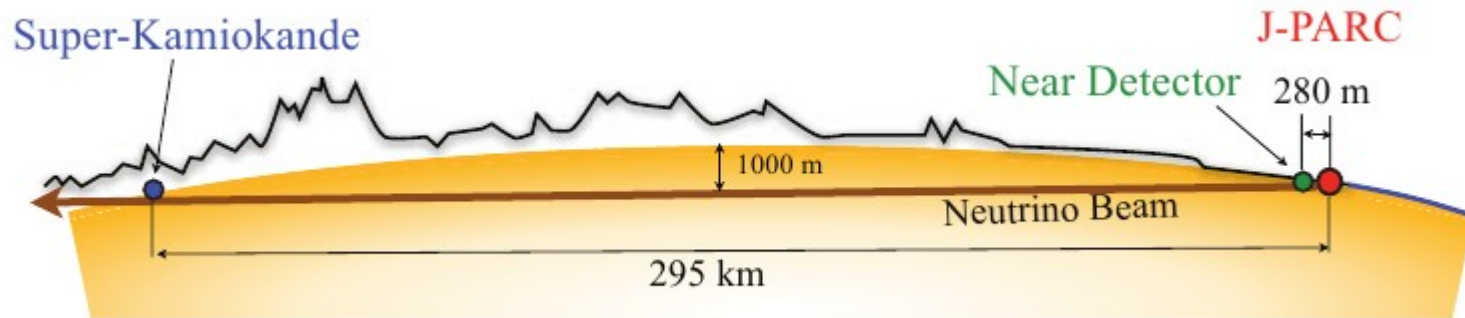
Events and ratio to no oscillations per energy band



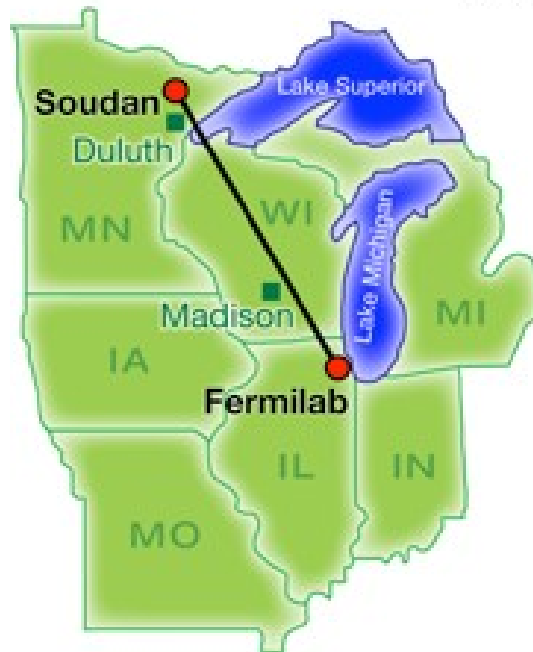
Accelerator neutrinos



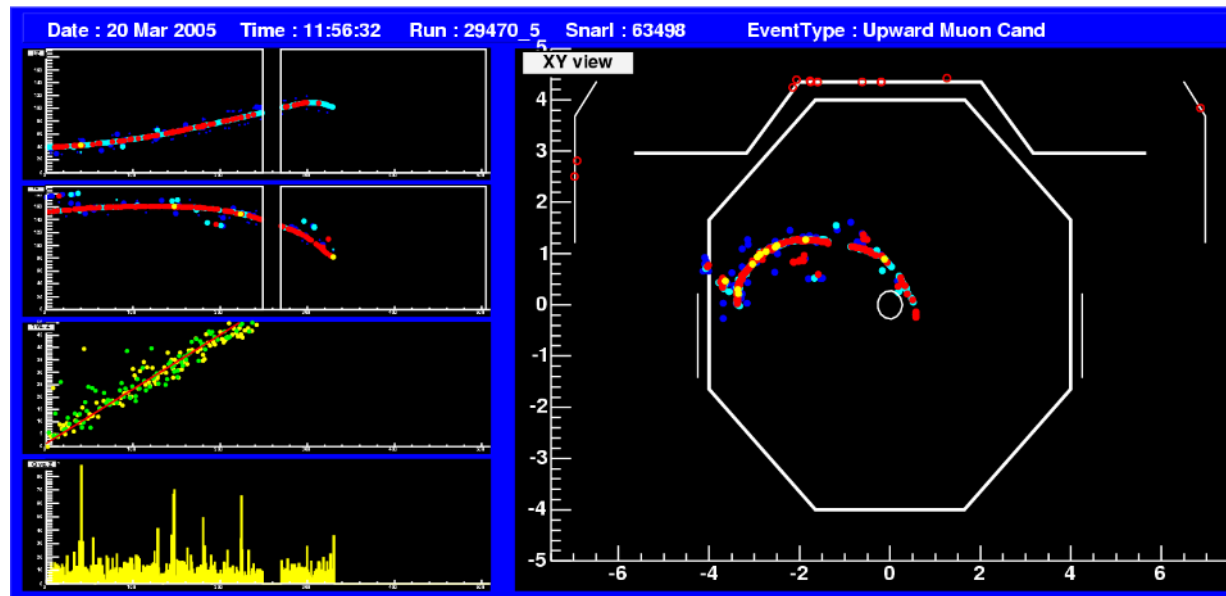
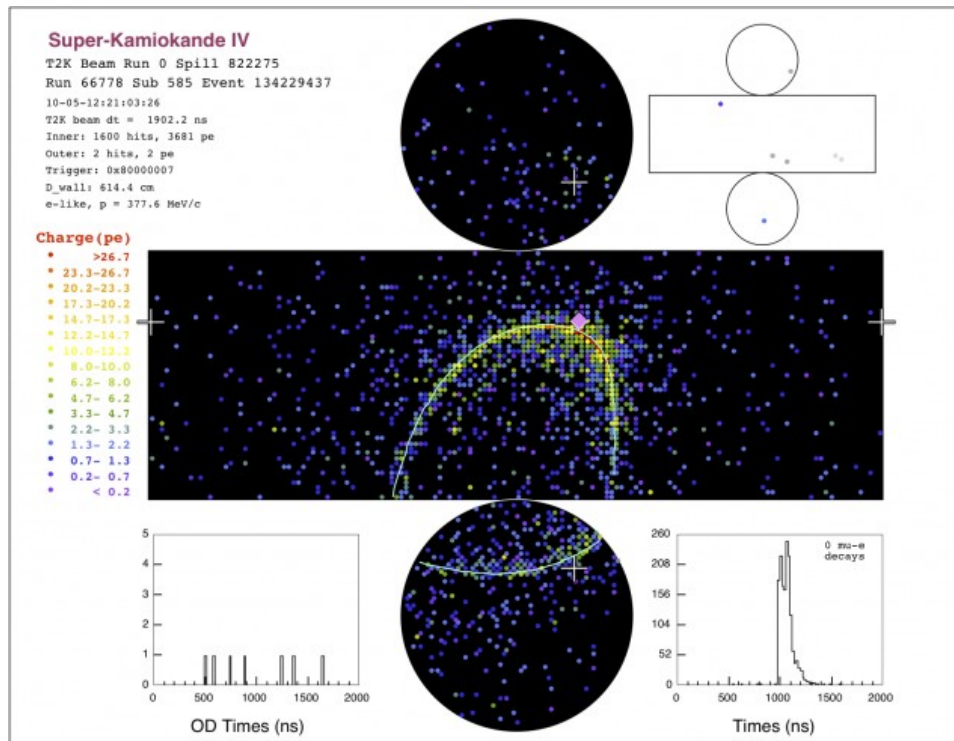
T2K & MINOS experiments



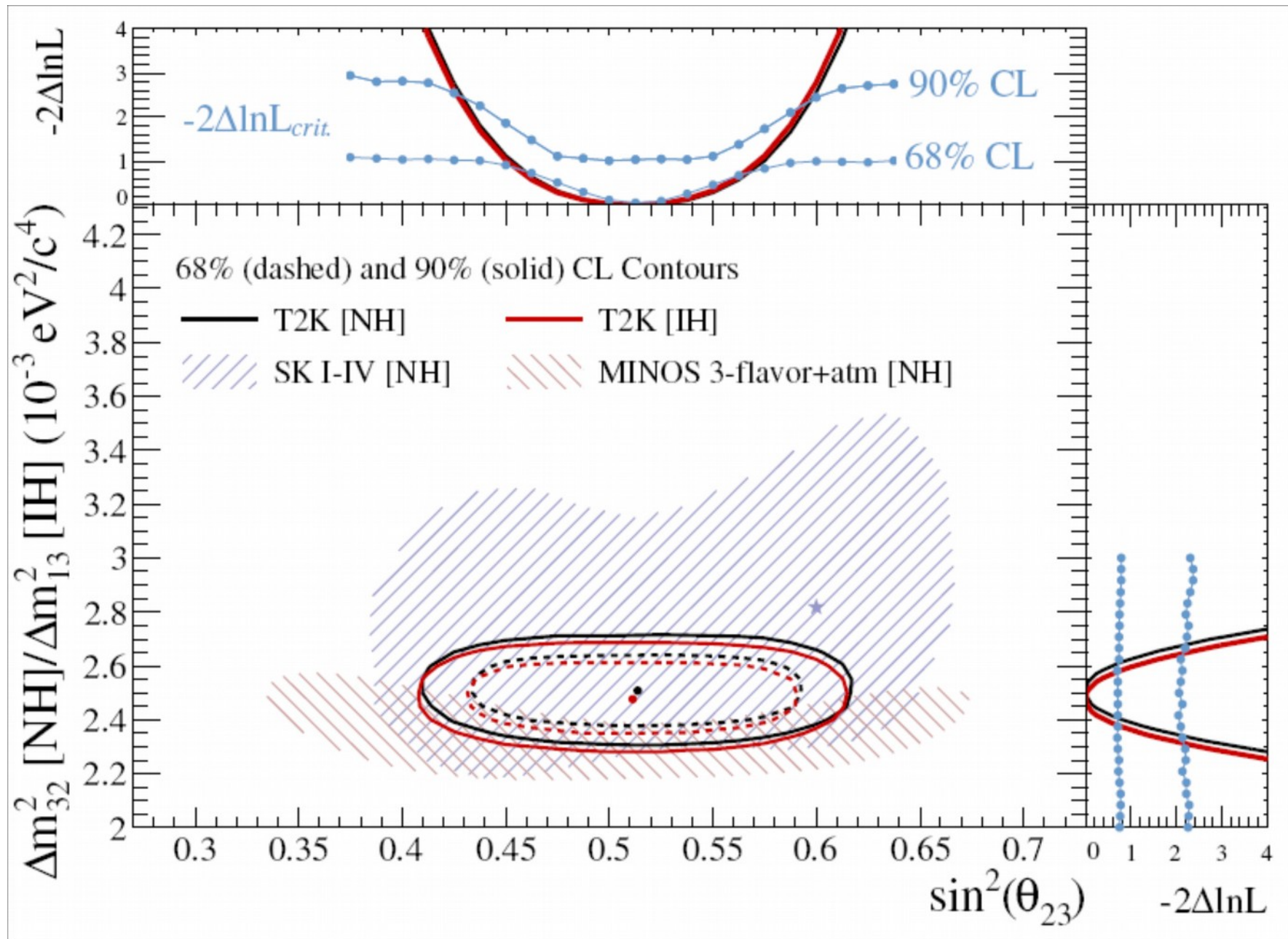
The MINOS Experiment



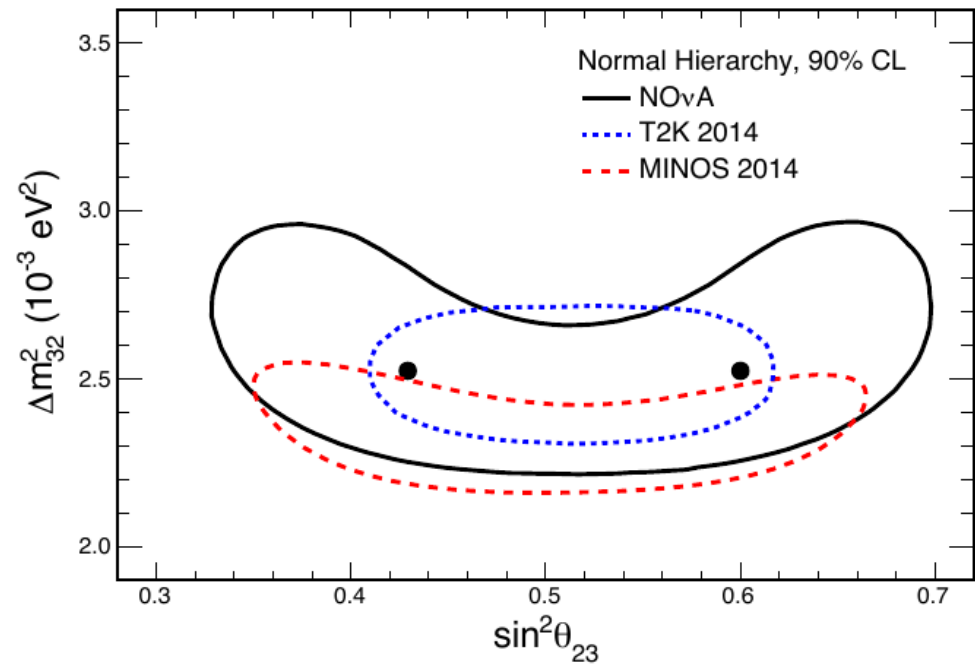
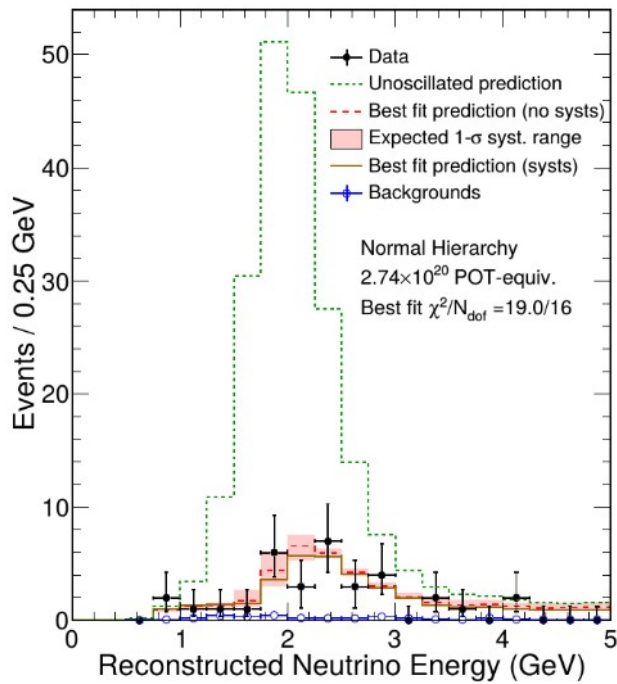
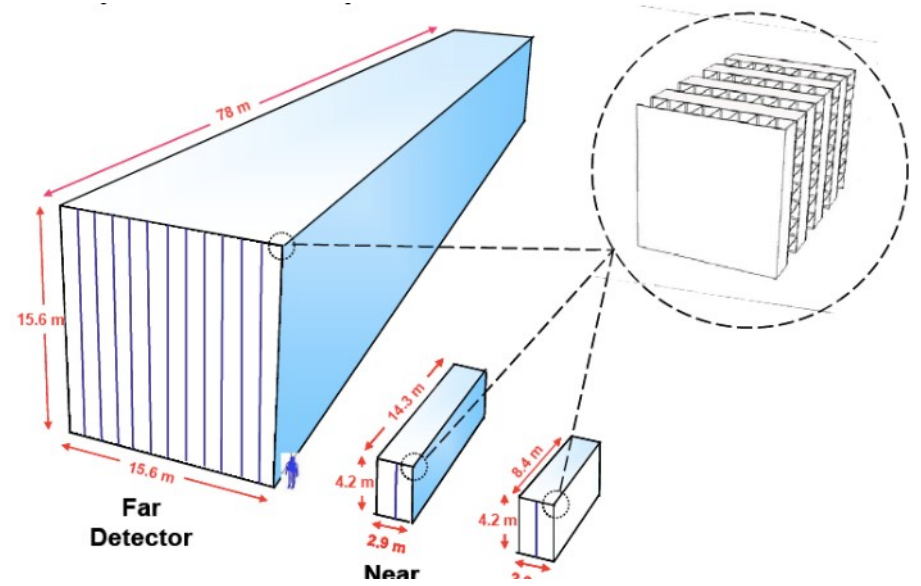
T2K & MINOS experiments



SK (atm) & T2K & MINOS

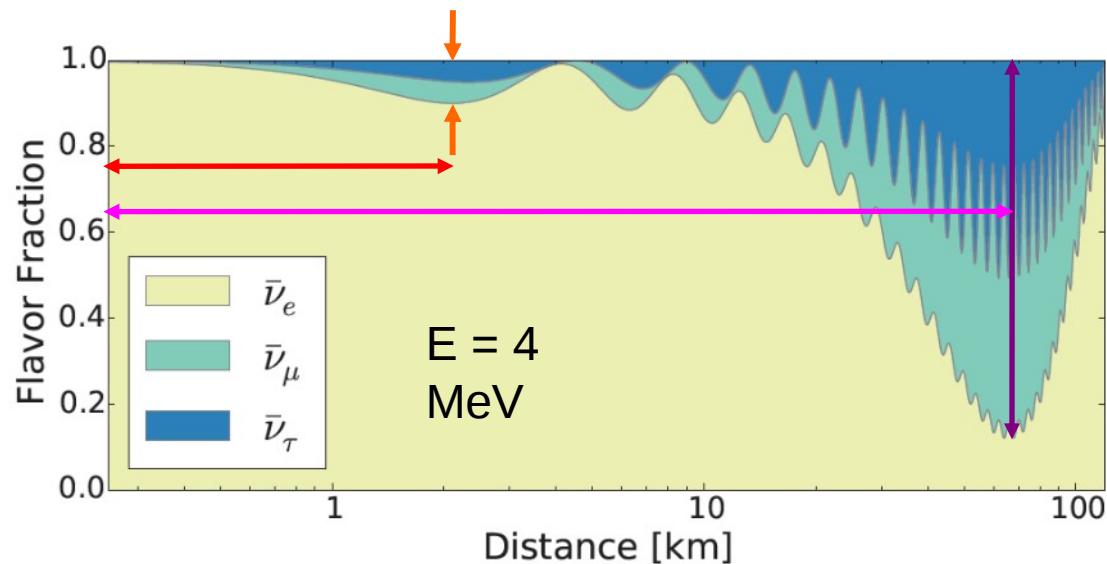


NOvA



Measurement of θ_{13}

Measurement of θ_{13} with reactors



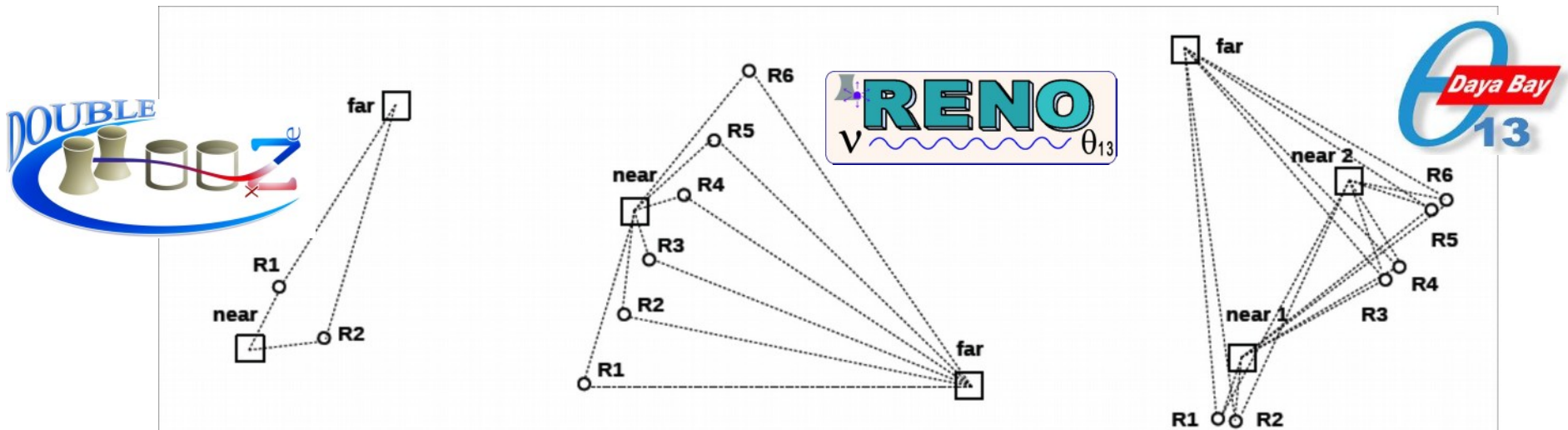
$$P_{ee}(L, E) = 1 - \cos^4(\theta_{13}) \sin^2(2\theta_{12}) \sin^2\left(\frac{\Delta m_{31}^2 L}{4E}\right) - \cos^2(\theta_{12}) \sin^2(2\theta_{13}) \sin^2\left(\frac{\Delta m_{31}^2 L}{4E}\right) - \sin^2(\theta_{12}) \sin^2(2\theta_{13}) \sin^2\left(\frac{\Delta m_{21}^2 L}{4E}\right)$$

- For baselines of ~ 1 km, the probability can be approximated by:

$$P_{ee}(L, E) \simeq 1 - \sin^2(2\theta_{13}) \sin^2\left(\frac{\Delta m_{31}^2 L}{4E}\right) \approx 1 - \sin^2(2\theta_{13}) \sin^2\left(1.27 \frac{\Delta m_{31}^2 [\text{eV}^2] L [\text{m}]}{E [\text{MeV}]}\right)$$

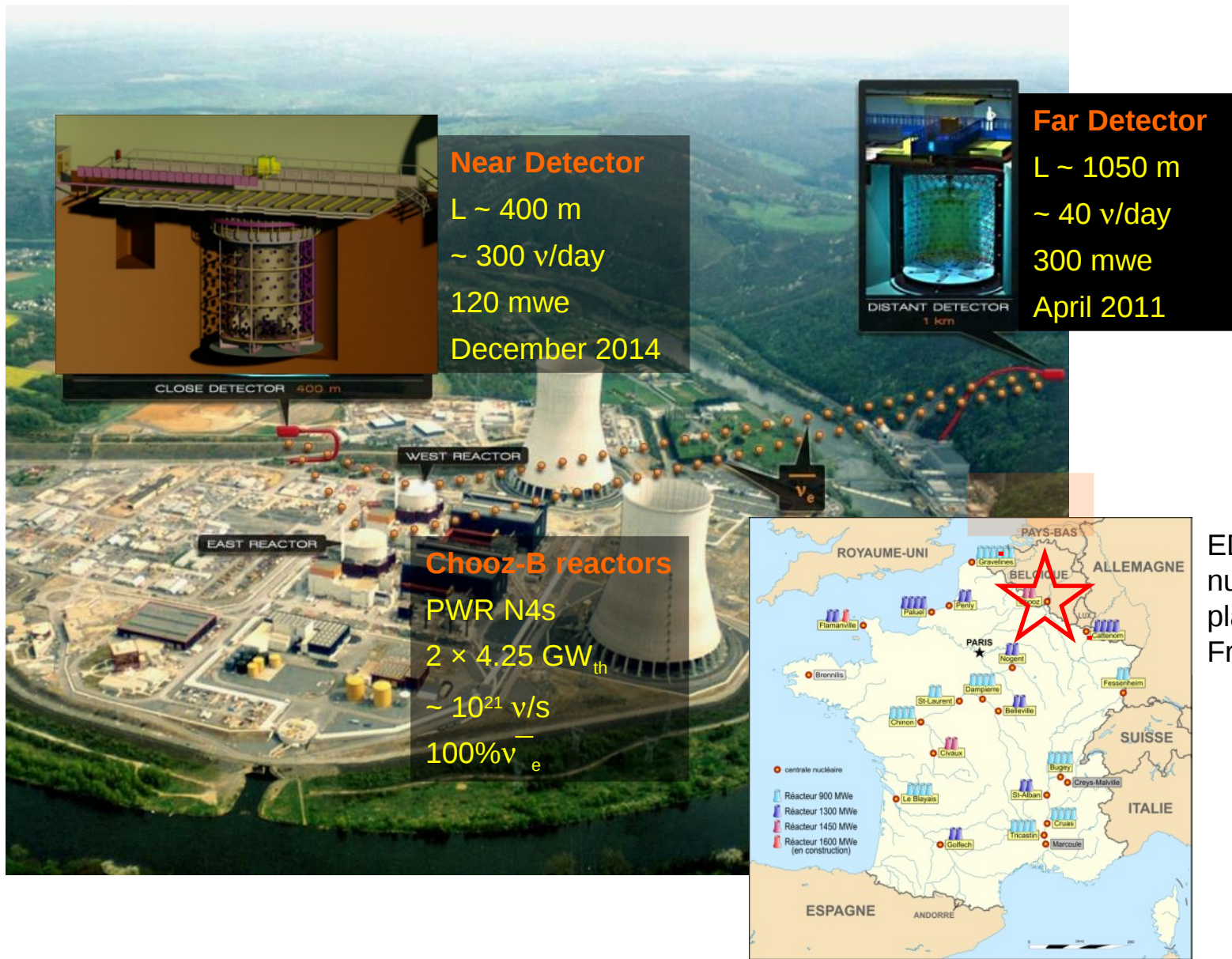
Measurement of θ_{13} with two-detector reactor experiments

- Antineutrinos detected by inverse β -decay: $\bar{\nu}_e + p \rightarrow e^+ + n$ on Gd-loaded liquid scintillator calorimeters.
- Reactor prediction and the antineutrino detection systematics can be reduced if **two identical detectors**, one near and one far from the reactors, are built.



Experiment	Reactor power (GW _{th})	Distance (m) Near / Far	Depth (mwe) Near / Far	Target mass (ton) × detectors
Double Chooz	8.5	400 / 1050	120 / 300	8 × 2
Daya Bay	17.4	470, 576 / 1648	260 / 860	20 × 8
RENO	16.5	294 / 1383	120 / 450	16 × 2

Double Chooz: a two-detector experiment



EDF's Chooz nuclear power plant (Ardennes, France)

Electron antineutrino detection

Inverse Beta Decay (IBD):

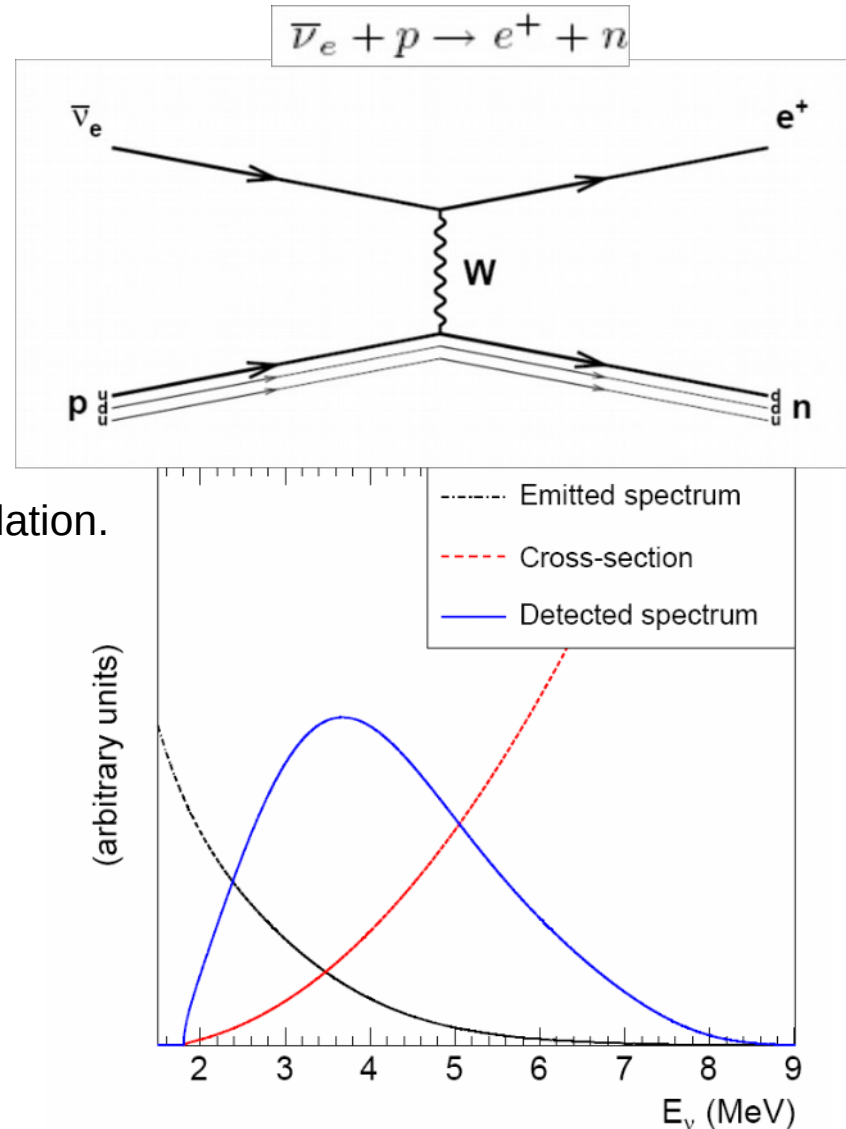
- Reaction threshold: $E_\nu \geq 1.806$ MeV.
- Disappearance experiment.
- Well known cross-section (0.2%).
- Coincidence of 2 signals: background suppression.

Prompt signal:

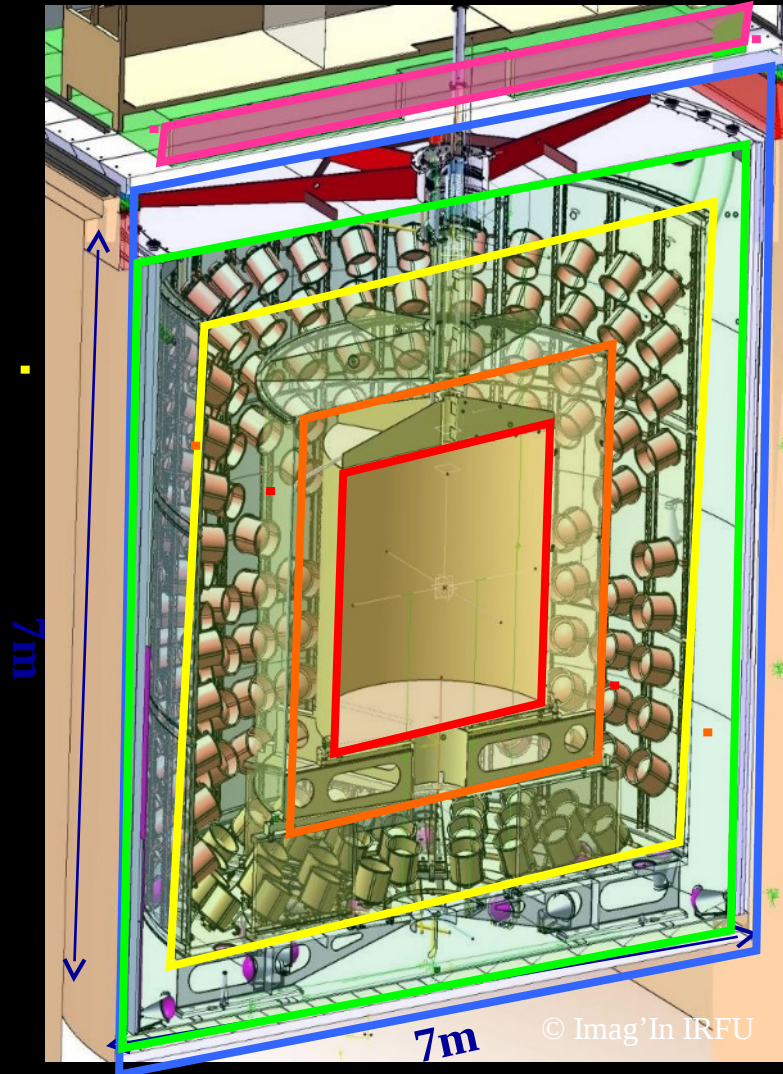
- Positron kinetic energy + γ 's from annihilation.
- $E_{\text{prompt}} \approx E_\nu - 0.782$ MeV
- $E_{\text{prompt}} \sim 1 - 9$ MeV

Delayed signal:

- γ 's from radiative neutron capture.
- **Gd**: $\Delta T \sim 30$ μs , $E_{\text{delayed}} \sim 8$ MeV.
- **H**: $\Delta T \sim 200$ μs , $E_{\text{delayed}} = 2.22$ MeV.



The Double Chooz Far Detector



Inner Detector:

- **Neutrino Target:** acrylic vessel (8 mm) with 10.3 m³ Gd-loaded (1 g/l) liquid scintillator.
- **Gamma-Catcher:** acrylic (12 mm) vessel with 22.5 m³ of liquid scintillator.
- **Buffer:** stainless steel (3 mm) vessel supporting 390 10" PMTs, with 110 m³ of non-scintillating mineral oil.

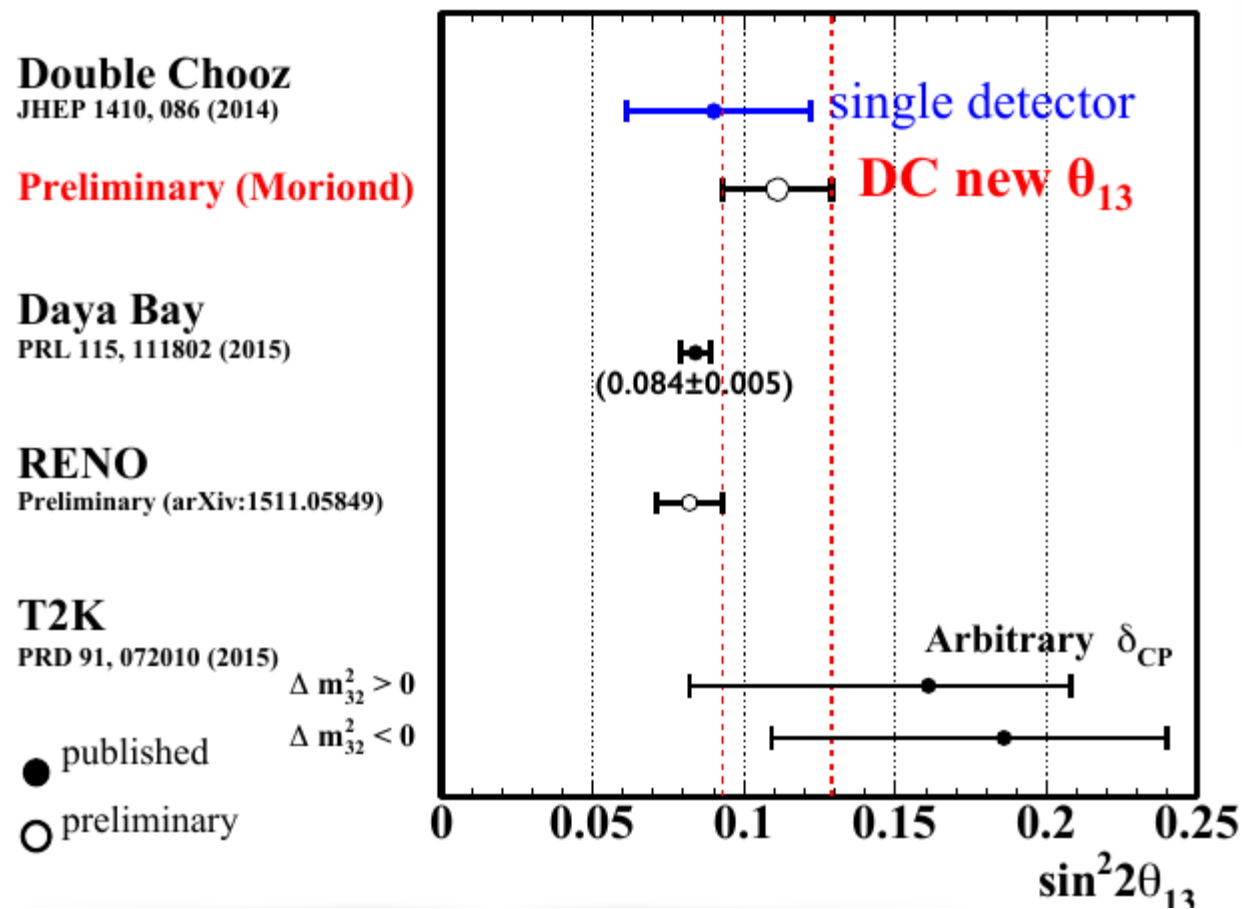
Outer Detector:

- **Inner Veto:** steel (10 mm) vessel supporting 78 8" PMTs, with 90 m³ of liquid scintillator.
- **Shielding:** 15 cm steel.
- **Outer Veto:** plastic scintillator strips.



Latests measurements of θ_{13}

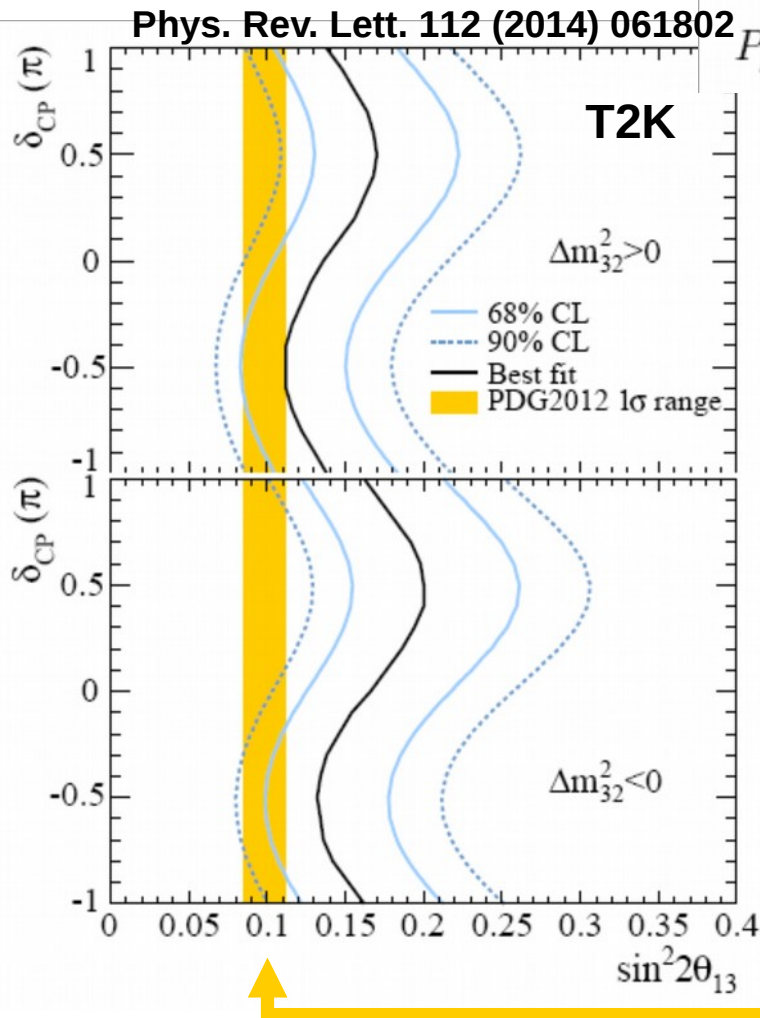
θ_{13} unknown until 2011. Huge progress in a few years.



A. Cabrera, FNAL seminar 03/25/2016

First glimpse of δ

- $\nu_\mu \rightarrow \nu_e$ depends on the mass hierarchy and CP-violating phase.



$$P_{\mu e}(L, E) = \frac{1}{(A-1)^2} \sin^2(2\theta_{13}) \sin^2(\theta_{23}) \sin^2[(A-1)\Delta] \\ \mp \frac{\alpha}{A(1-A)} \cos(\theta_{13}) \sin(2\theta_{12}) \sin(2\theta_{23}) \sin(2\theta_{13}) \times \\ \times \sin(\delta) \sin(\Delta) \sin(A\Delta) \sin[(1-A)\Delta] \\ + \frac{\alpha}{A(1-A)} \cos(\theta_{13}) \sin(2\theta_{12}) \sin(2\theta_{23}) \sin(2\theta_{13}) \times \\ \times \cos(\delta) \cos(\Delta) \sin(A\Delta) \sin[(1-A)\Delta] \\ + \frac{\alpha^2}{A^2} \cos^2(\theta_{23}) \sin^2(2\theta_{12}) \sin^2(A\Delta),$$

$$\alpha \equiv \Delta m_{21}^2 / \Delta m_{32}^2$$

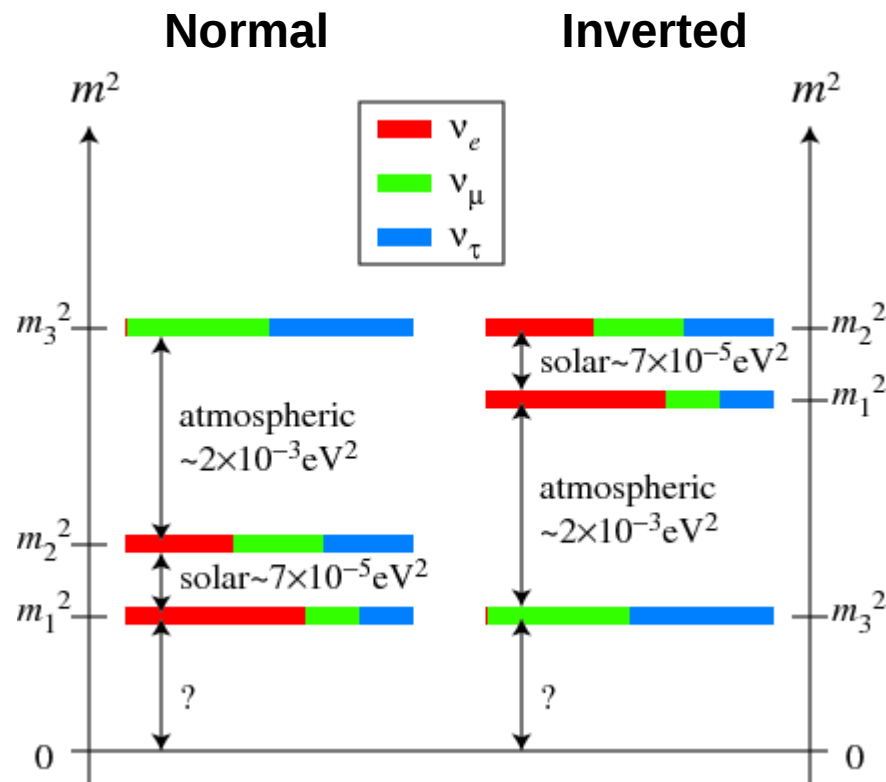
$$\Delta \equiv \frac{\Delta m_{32}^2 L}{4E}$$

$$A \equiv 2\sqrt{2}G_F N_e \frac{E}{\Delta m_{32}^2}$$

Critical input: Using the θ_{13} from the reactor experiments, the mass hierarchy and the CP-violating phase can be studied.

3 neutrinos: mass hierarchy

- 2 squared-mass differences
- But which is on top of which?
- The Solar + KamLAND experiments show that the mass eigenstate ν_2 is heavier than ν_1 .
- Which is the **lightest neutrino**? Two possibilities left:



Future: δ and mass hierarchy

- Both CP-violating phase and the mass hierarchy can be measured in a long-baseline accelerator experiment.
- Need a long baseline and a broad-energy beam to disentangle CP violation caused by matter effects (Earth is made only from matter) from the intrinsic CP violation.

